

# ECE 111: Handout #17

ECE 343: Signals & Systems, Fourier Transforms

Find  $y(t)$

$$Y = \left( \frac{20}{s+10} \right) X$$

$$x(t) = 2 + 3 \cos(4t) + 5 \sin(6t)$$

hint: use superposition and treat this as three separate problems

$$x_1(t) = 2$$

$$x_2(t) = 3 \cos(4t)$$

$$x_3(t) = 5 \sin(6t)$$

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hint: use superposition and treat this as three separate problems

**$s = 0$ :**

$$x(t) = 2$$

$$Y = \left( \frac{20}{s+10} \right)_{s=0} (2 + j0)$$

$$Y = (2)(2) = 4$$

$$y(t) = 4$$

**$s = j4$**

$$x(t) = 3 \cos(4t)$$

$$X = 3 + j0$$

$$Y = \left( \frac{20}{s+10} \right)_{s=j4} (3 + j0)$$

$$Y = 7.759 - j2.103$$

$$y(t) = 7.759 \cos(4t) + 2.103 \sin(4t)$$

**$s = j6$**

$$x(t) = 5 \sin(6t)$$

$$X = 0 - j5$$

$$Y = \left( \frac{20}{s+10} \right)_{s=j6} (0 - j5)$$

$$Y = -4.412 - j7.353$$

$$y(t) = -4.412 \cos(6t) + 7.353 \sin(6t)$$

**The total answer is then**

$$y(t) = 4 + 7.759 \cos(4t) + 2.103 \sin(4t) - 4.412 \cos(6t) + 7.353 \sin(6t)$$