

# ECE 111 - Homework #10

ECE 343 Signals & Systems- Due Tue 11am Tuesday, November 9th  
Please submit as a Word or pdf file and email to Jacob\_Glower@yahoo.com with header ECE 111 HW#10

1) A filter has the following transfer function

$$Y = \left( \frac{2s+50}{s^2+13s+40} \right) X$$

1a) What is the differential equation relating X and Y?

1b) Find  $y(t)$  assuming  $x(t) = 4$

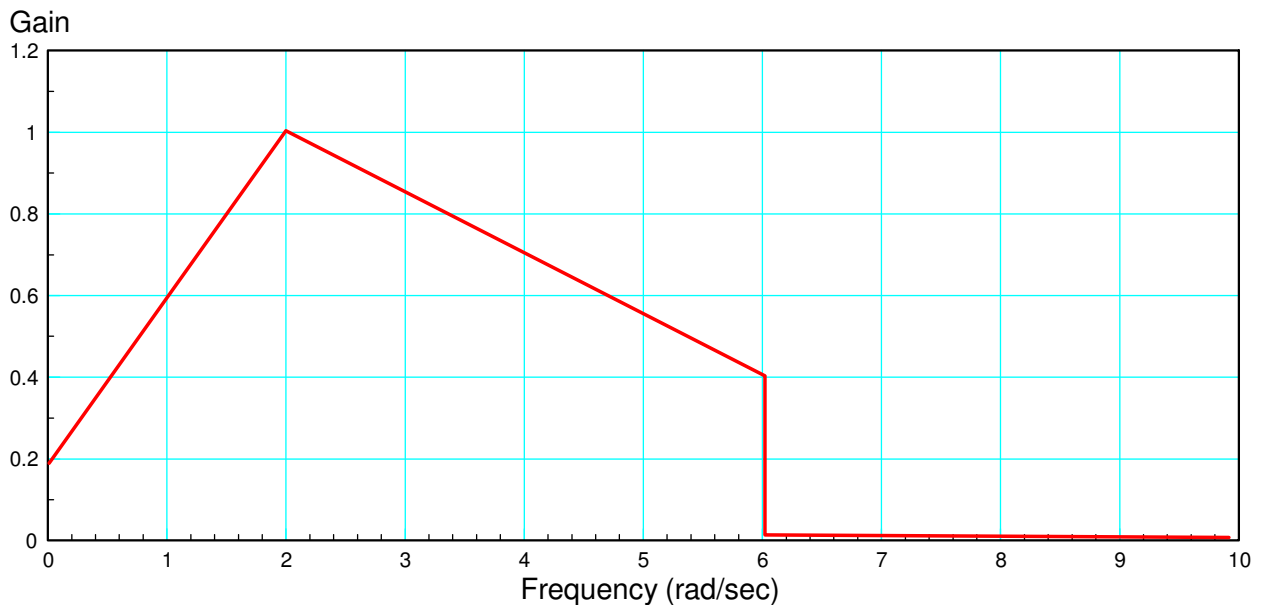
1c) Find  $y(t)$  assuming  $x(t) = 4 \cos(6t)$

2) Plot the gain vs. frequency for this filter from 0 to 50 rad/sec.

$$Y = \left( \frac{2s+50}{s^2+13s+40} \right) X$$

Problem 3-5) Design a filter of the following form so that the gain matches the graph below:

$$G(s) = \left( \frac{a(s+b)}{(s^2+cs+d)(s^2+es+f)} \right)$$



3) Write an m-file, cost.m, which

- Is passed a 5-element array, z, with each element representing (a, b, c, d, e)
- Computes the gain, G(s) for this value of (a, b, c, d, e)
- Computes the difference between the gain, G, and the target (above), and
- Returns the sum-squared error in the gain

4) Use your m-file to determine how 'good' the following filter is:

$$G(s) = \left( \frac{a(s+b)}{(s^2+cs+d)(s^2+es+f)} \right) = \left( \frac{20(s+1)}{(s^2+2s+5)(s^2+2s+17)} \right)$$

5) Use fminsearch() to find the 'best' filter of the form

$$G(s) = \left( \frac{a(s+b)}{(s^2+cs+d)(s^2+es+f)} \right)$$

5a) Give the resulting (a, b, c, d, e, f)

5b) Give the resulting filter, and

5c) Plot the 'optimal' filter's gain vs. frequency