

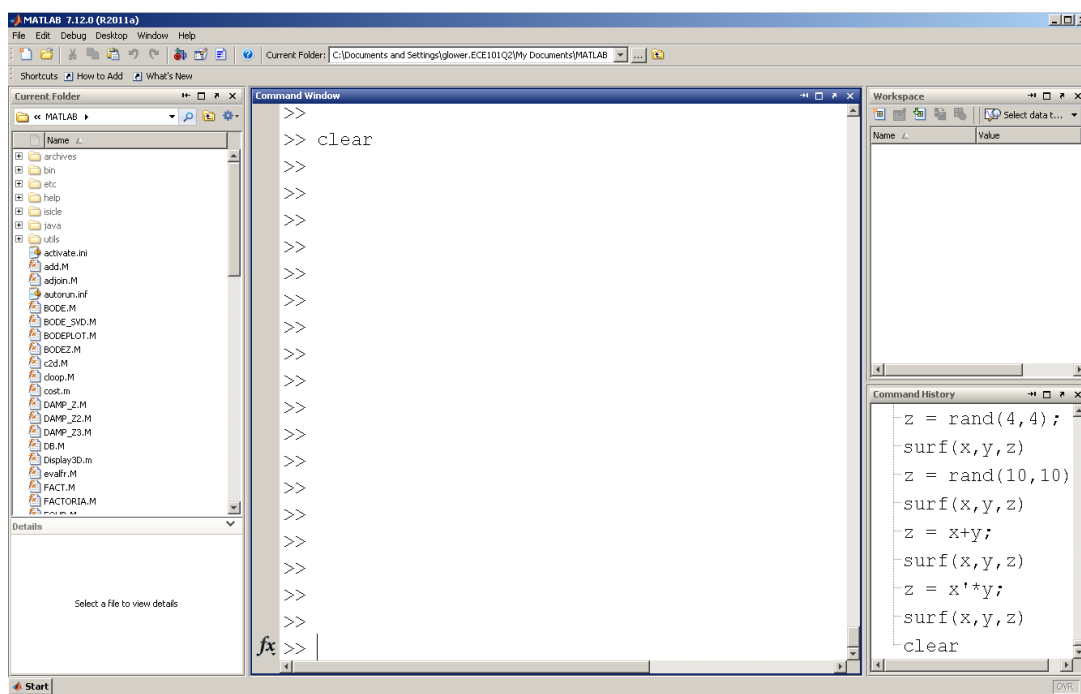
Introduction to Matlab

Becoming familiar with MATLAB

- The console
- The editor
- The graphics windows
- The help menu
- Saving your data (diary)

General environment and the console

When you start up Matlab, the screen should look something like this:



Usually, I close all of the windows except the Command Window. Matlab can be used like a calculator - with some of the command options listed in the appendix. For example, if you want to compute

$$(2 + 3) * 5$$

You type it the way it looks:

```
>> (2 + 3)*5
```

```
ans = 25
```

In Matlab, you can save the results and use them later - like the memory functions of your calculator. Valid names for your variables have to start with a letter. Note that Matlab is case sensitive. For example

```
>> a = (2+3)*5
a = 25
>> b = 1.3 * a^3
b = 2.0313e+004
```

Matrices in Matlab

Matlab is also a matrix language. An $n \times m$ matrix is an array of numbers arranged in n rows and m columns

$$A_{2 \times 3} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \end{bmatrix}$$

The syntax to input a matrix are:

```
[      start of a matrix
,      next column (a space also works)
;      next row
]      end of matrix.
```

For example, to input a 2×3 matrix for A:

```
A = [1,2,3 ; 4,5,6]

    1    2    3
    4    5    6
```

Matrix Addition: When adding matrices, each element gets added. You can only add matrices of like dimensions.

```
A = [1,2,3 ; 4,5,6]
```

```
    1    2    3
    4    5    6
```

```
B = [2,2,2 ; 3,3,3]
```

```
    2    2    2
    3    3    3
```

```
C = A + B
```

```
    3    4    5
    7    8    9
```

Matrix Multiplication: When multiplying matrices, the inner dimension must match

$$C_{mn} = A_{mx} B_{xn}$$

Element (i,k) of matrix C is computed as:

$$c_{ik} = \sum a_{ij} b_{jk}$$

Sample Matlab Code

If you terminate a line with a semi-colon, the result is computed but isn't displayed. If you leave off the semi-colon, the results is displayed. For example:

```
x = 2*pi;           % result is computed and stored in x but isn't displayed
x = 2*pi           % ditto but the result is displayed.

6.2832
```

If you want a different format for the display, you can use the 'short', 'long', and 'shorteng' commands:

```
format short
pi

3.1416

format long
pi

3.141592653589793

format shorteng
pi^30

821.2893e+012
```

Matrices

- [start of matrix
-] end of matrix
- , next element
- ; next row

```
A = [1, 2, 3]

1    2    3
```

```
B = [1, 2, 3; 4, 5, 6]

1    2    3
4    5    6
```

```
C = A'

1
2
3
```

```
D = zeros(1, 3)
```

0 0 0

E = rand(3,2)

0.5860 0.0835
0.2467 0.6260
0.6664 0.6609

for loops:

```
x = zeros(1,5);  
for i=1:5  
    x(i) = i*i;  
end  
x
```

x =

1 4 9 16 25

while

if

if else end

Plotting Functions in Matlab:

Matlab has some pretty good graphics capabilities.

Matlab Plot Command	x axis	y axis	type of function
<code>plot(x,y)</code>	linear	linear	$y = ax + b$
<code>semilogx(x,y)</code>	log()	linear	$y = a \cdot e^{bx}$
<code>semilogy(x,y)</code>	linear	log()	$y = a + b \ln(x)$
<code>loglog(x,y)</code>	log()	log()	$y = a \cdot b^x$
<code>subplot(abc)</code>	Create 'a' rows, 'b' columns of graphs. Starting at #c		

For example, plot the function

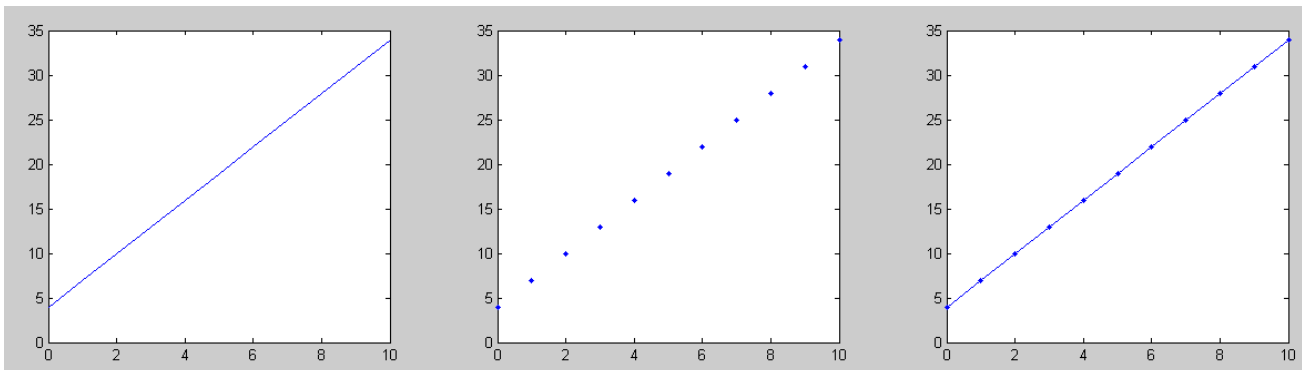
$$y = 3x + 4$$

```
x = [0:1:10]';
y = 3*x + 4;
```

```
subplot(131)
plot(x,y); % connect the points with a line
```

```
subplot(132)
plot(x,y, '.'); % plot a dot at each point
```

```
subplot(133);
plot(x,y, '-.');
```



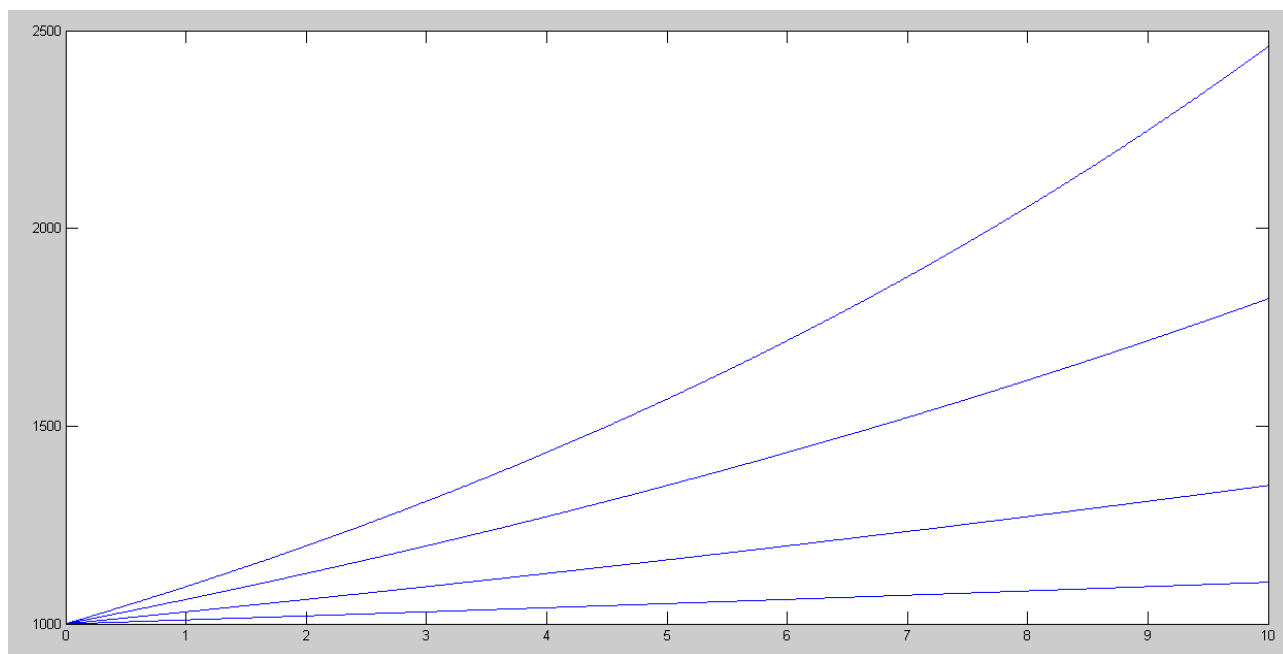
Multiple Plots on the same graph:

Plot how much money you'd have if you invested it for 10 years at

- 1% interest
- 3% interest
- 6% interest
- 9% interest

Three ways to do this:

```
t = [0:0.01:10]';  
y1 = 1000 * exp(0.01*t);  
y3 = 1000 * exp(0.03*t);  
y6 = 1000 * exp(0.06*t);  
y9 = 1000 * exp(0.09*t);  
  
% Method #1  
plot(t,y1,t,y3,t,y6,t,y9)  
  
% Method #2  
plot(t,[y1,y3,y6,y9])  
  
% Method #3  
plot(t,y1)  
hold on  
plot(t,y3)  
plot(t,y6)  
plot(t,y9)  
hold off
```



If you invest at 9% interest, you have almost 2.5x more money after 10 years than you'd have at 1% interest.

Polynomials

- `poly([a,b,c])` Give a polynomial with roots at (a, b, c)
- `roots([a,b,c,d])` Find the roots of the polynomial
 $ax^3 + bx^2 + cx + d = 0$

Example:

- Determine a polynomial with roots at (1, 2, 3)
- Plot that function,
- Verify that the roots are in fact at (1, 2, 3)

In Matlab:

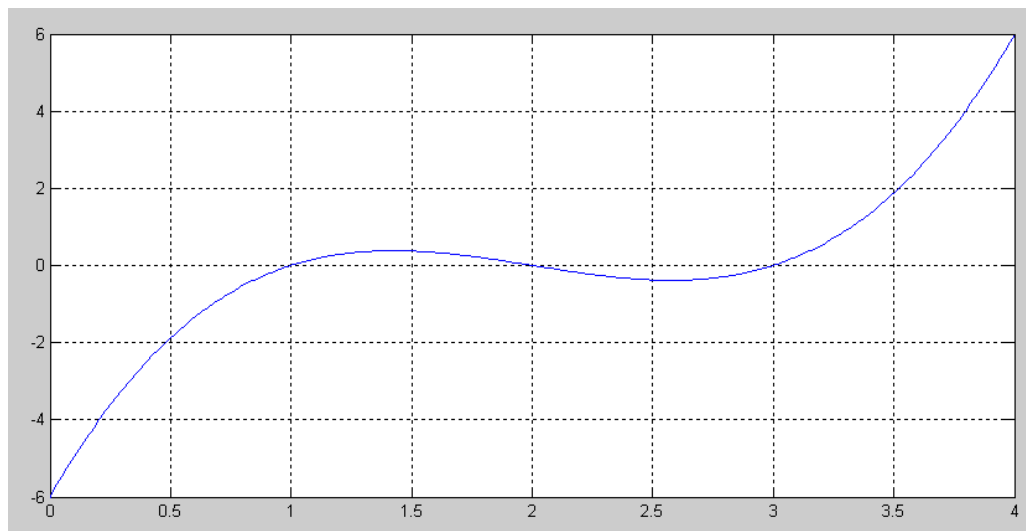
```
poly([1,2,3])  
1    -6    11    -6
```

meaning

$$y = x^3 - 6x^2 + 11x - 6 = (x-1)(x-2)(x-3)$$

```
roots([1,-6,11,-6])  
3.0000  
2.0000  
1.0000
```

```
x = [0:0.01:4]';  
y = x.^3 - 6*(x.^2) + 11*x - 6;  
plot(x,y);  
grid on
```



3-D Plots

```
mesh(z)
```

Draw a 3-d mesh for the array 'z' with the height being the value in the array.

Example

$$z = x^2 + y^2$$

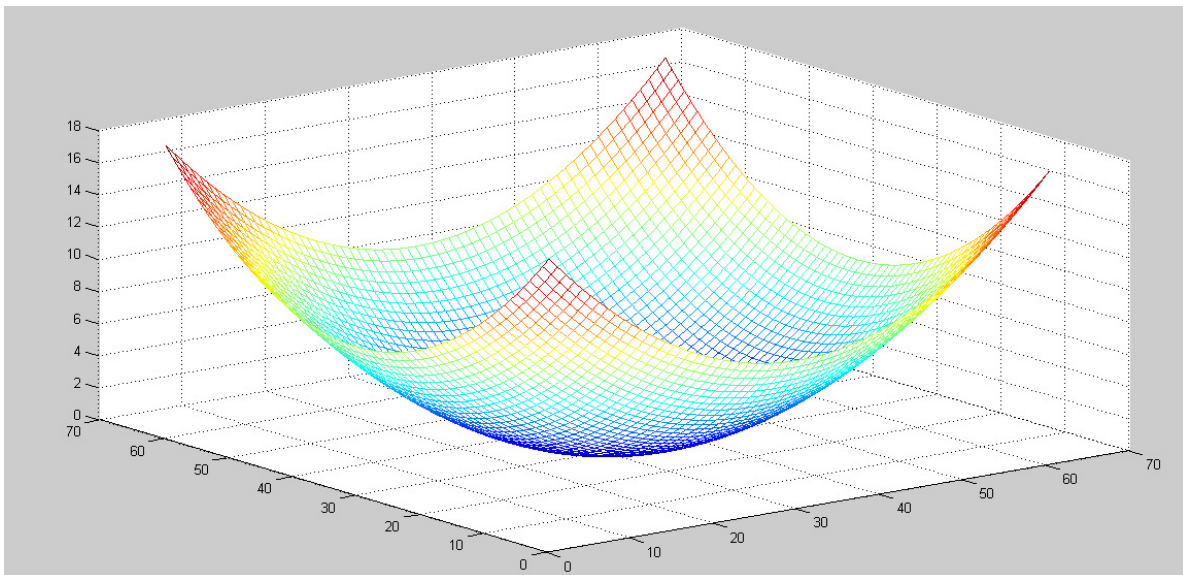
```
x = [-3:0.1:3]';  
y = [-3:0.1:3]';  
size(x)
```

```
ans =
```

```
61    1
```

```
z = zeros(61,61);  
for i=1:61  
    for j=1:61  
        z(i,j) = x(i)^2 + y(j)^2;  
    end  
end
```

```
mesh(z)
```

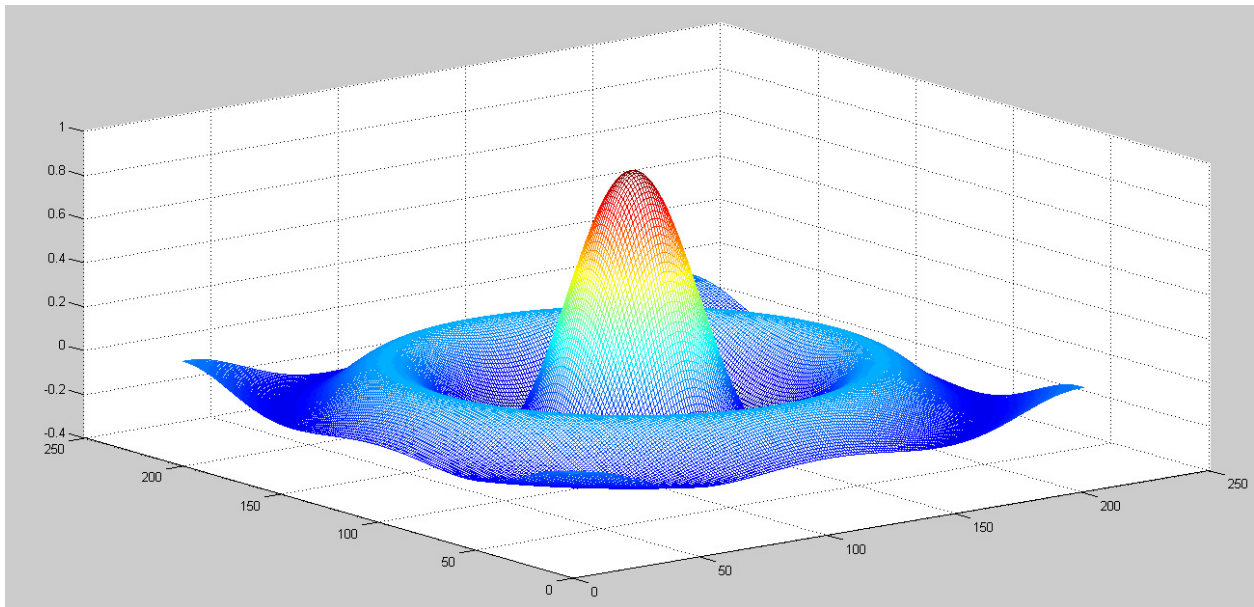


Another pretty plot:

$$r = \sqrt{x^2 + y^2}$$

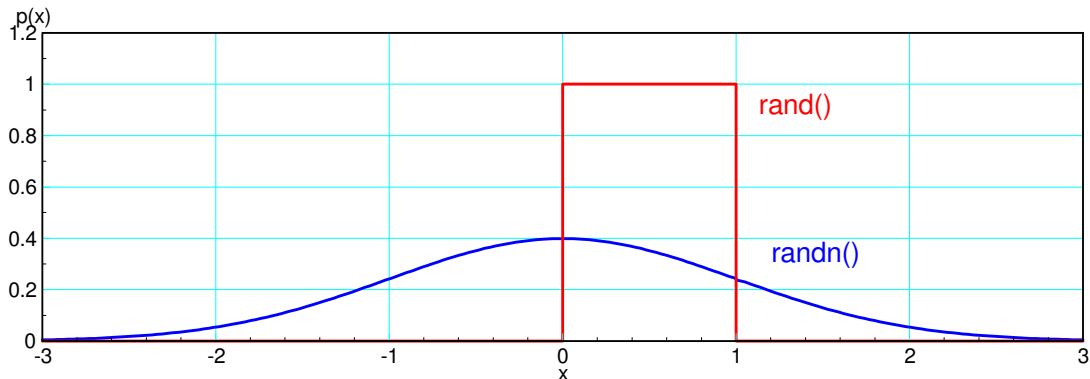
$$z(x, y) = \left(\frac{\sin(r)}{r} \right)$$

```
x = [-10:0.1:10]';  
y = [-10:0.1:10]';  
size(x)  
  
201    1  
  
z = zeros(201,201);  
for i=1:201  
    for j=1:201  
        r = sqrt(x(i)^2 + y(j)^2);  
        z(i,j) = sin(r) / (r + 0.000001);  
    end  
end  
mesh(z)
```



Random Numbers: Rolling Dice

```
rand          random number: (0,1)
randn        standard normal random #
```

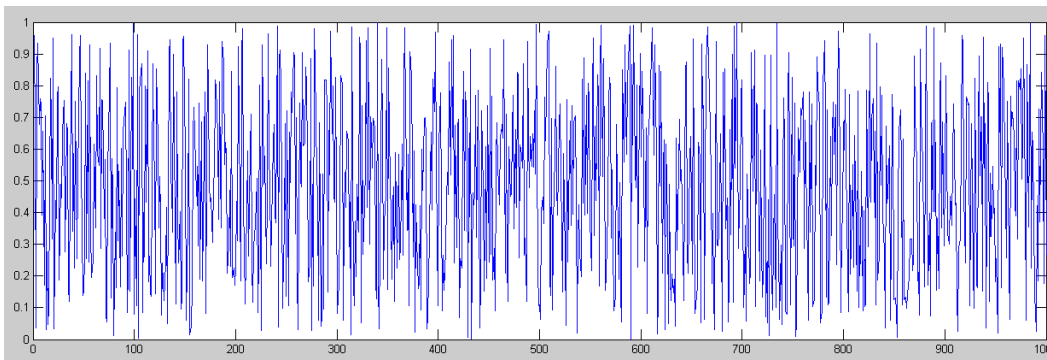


rand() produces a uniform distribution. randn() produces a Normal distribution

```
rand(1,5)          1x5 matrix of random #
ceil( 6*rand )     6-sided die
ceil( 8*rand(1,3) ) 3d8
sum( 6*rand(5,1) ) sum of 5d6 (level 5 fireball)
```

Example: Generate 1000 random numbers and plot them

```
x = rand(1,1000);
plot(x)
```

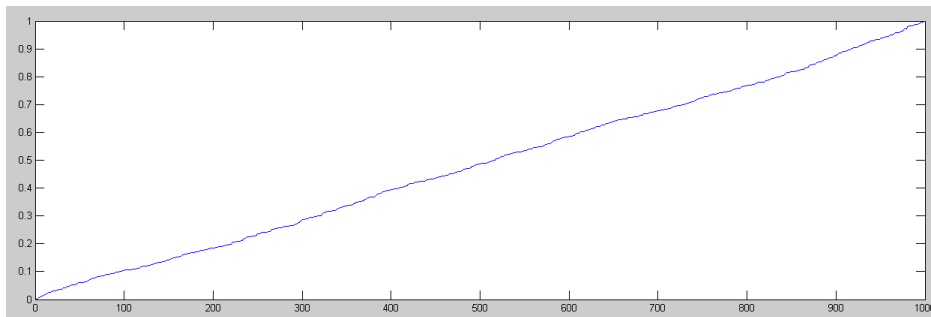


rand() produces a random number in the range of (0,1)

If you sort the numbers, you can see the cumulative distribution function

- approximately
- $(\text{rand} < 0.6)$ approximately 60% of the time

```
y = sort(x);
plot(y)
```



sorting the results of rand shows that 20% of the time, rand() produces a number less than 0.2

Matlab Scripts

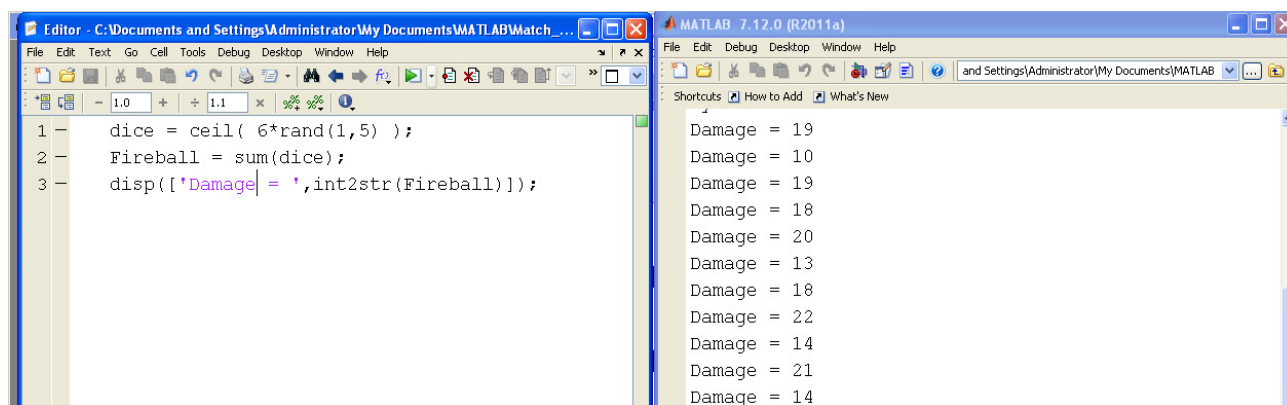
Instead of typing in the command window, you can use a Matlab Script. When executed, (green arrow in the icon bar), scripts act like you input those instructions in the command window.

This is useful

- It lets you build up your code
- It lets you modify existing code
- You can rerun the code over and over

For example,

- The window on the left (Matlab script) computes the damage for summing five 6-sided dice (i.e. a level 5 fireball for D&D fans).
- The window on the right (command window) shows the print-ports when the script is run
- Clicking on the run command (green arrow on the top of the script) results in the script executing several times.



Matlab Script (left) and Command (right).

For-Loops

```
for i=1:100
    statements
end
```

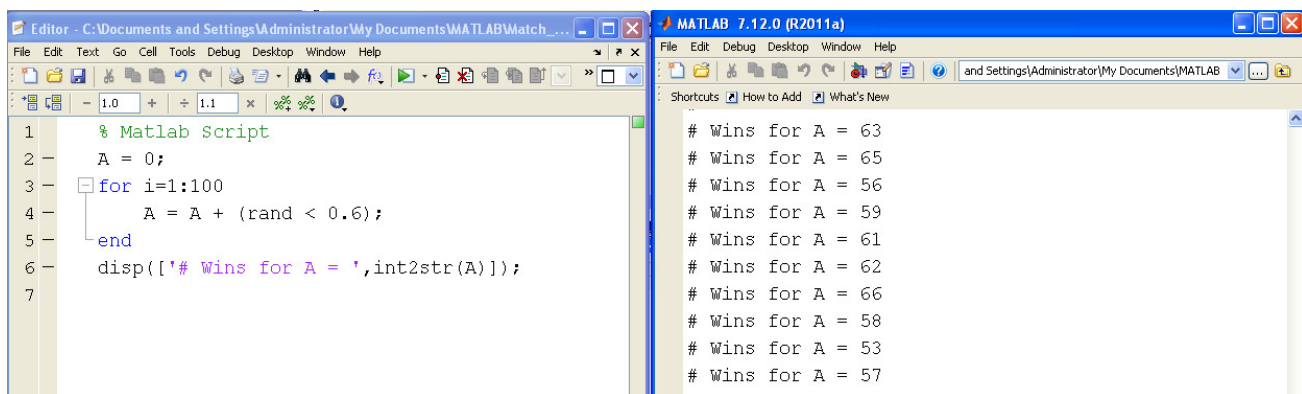
For-Loops repeat a set of instructions a fixed number of times. For example, assume A and B are playing a game.

- A has a 60% chance of winning any given game.
- How many games will A win in a 100 game match?

This can be done with a for-loop:

- $(\text{rand} < 0.6)$ is a boolean operation: it's 1 if true, 0 if false.
- Each game, A has a 60% chance of earning one point (a win)
- 100 games are played in each match (the for-loop).

The resulting Matlab code (in a script window) and results of executing it are as follows:



```
1 % Matlab Script
2 A = 0;
3 for i=1:100
4     A = A + (rand < 0.6);
5 end
6 disp(['# Wins for A = ',int2str(A)]);
7
```

```
# Wins for A = 63
# Wins for A = 65
# Wins for A = 56
# Wins for A = 59
# Wins for A = 61
# Wins for A = 62
# Wins for A = 66
# Wins for A = 58
# Wins for A = 53
# Wins for A = 57
```

For-Loop: $(\text{rand} < 0.6)$ is executed 100 times each pass.

Note:

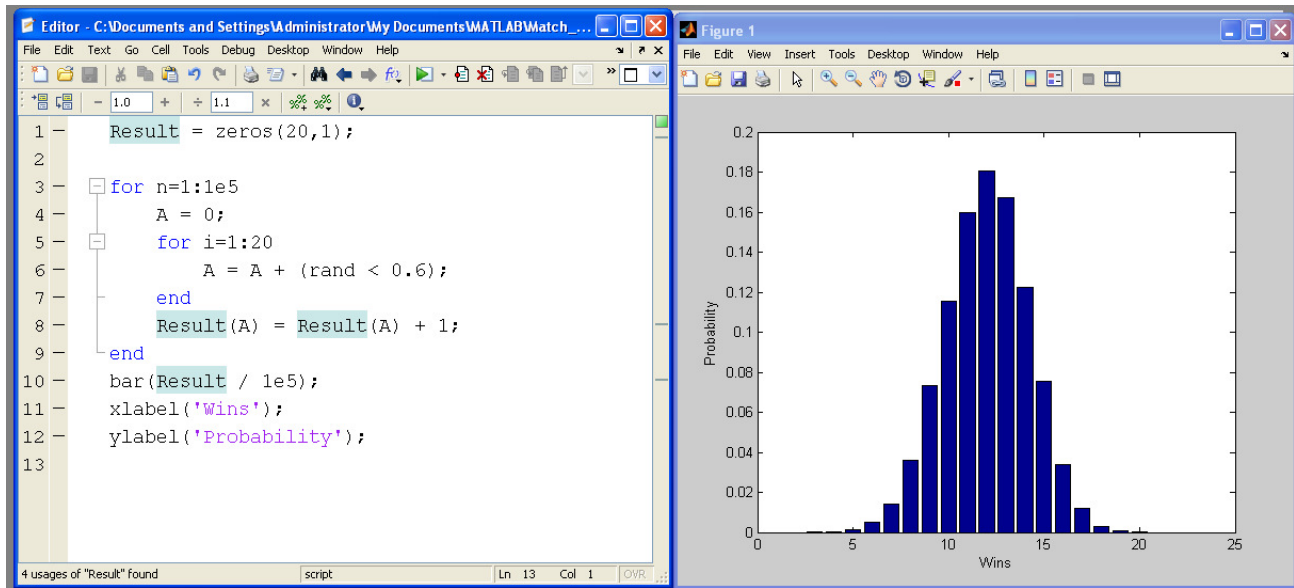
- 0 is false, 1 is true
- On average, A wins 60 games out of 100
- In any given match, A could win 0..100 games

For-Loops & Monte-Carlo Simulations: 20-game match

What is the probability of A winning X games in a 20 game match?

To solve this problem, change the for-loop from 100 to 20. Also keep track of how many times you won X games and then repeat this experiment 100,000 times (termed a Monte-Carlo simulation)

One Matlab program and it's results are as follows:



Monte-Carlo simulation: Repeat an experiment 100,000 times

Note: The resulting distribution is a bell-shaped curve. This is called a *Normal Distribution* and is something you'll see over and over and over again.

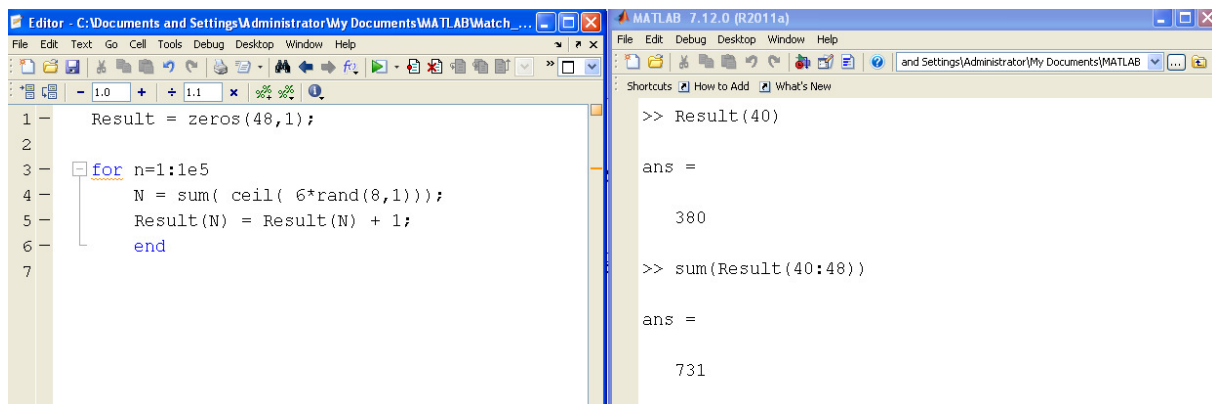
For-Loops: Level-8 Fireball

Using a similar technique, for-loops can determine the probability of

- Doing 40 damage with a level-8 fireball, or
- Doing 40+ damage with a level-8 fireball.

To solve these problems,

- First, cast a single level-8 fireball
- Determine if the damage was 40 or more than 40
- Then repeat 100,000 times, recording how many times the result was N



The resulting probability is (approximately)

- $p = 380 / 100,000$ to do 40 damage exactly
- $p = 731 / 100,000$ to do 40 or more damage.

If-Statements

```
if(boolean statement)
    statements to execute
end
```

If-statements allow you to execute a set of instructions based upon a condition. Valid boolean statements are as follows:

```
(N == 3)
(N > 3)
(N >= 3)
(N != 3)
(N >= 3) * (N <= 7)
((N < 3) | (N > 7))
```

If-statements are useful for checking what conditions hold. For example, suppose A and B are playing a match

- Each match consists of 5 games
- A has a 60% chance of winning any given game
- Whoever wins 3+ games wins the match

What is the chance that A wins the match?

Matlab Script

```
Wins = 0;
for n=1:1e5
    A = 0;
    for i=1:5
        if(rand < 0.6)
            A = A + 1;
        end
    end
    if(A >= 3)
        Wins = Wins + 1;
    end
end
disp(['# of wins for A = ',int2str(Wins)]);
```

Matlab Command Window

```
MATLAB 7.12.0 (R2011a)
File Edit Debug Desktop Window Help
and Settings\Administrator\My
Shortcuts How to Add What's New
# of wins for A = 68306
# of wins for A = 68355
# of wins for A = 68053
# of wins for A = 68254
# of wins for A = 68377
# of wins for A = 68442
# of wins for A = 68150
# of wins for A = 68335
# of wins for A = 67969
# of wins for A = 67977
# of wins for A = 68726
```

Solution:

- Monte-Carlo simulation of 100,000 matches
- A wins about 68% of the time

If-Statements (cont'd)

Player A casts a level-8 fireball (8d6)

- What is the chance of doing 40 damage?
- What is the chance of doing 40+ damage?

Solution:

- Monte-Carlo Simulation
- Cast 100,000 fireballs
- Count how many times you do 40 damage
- Count how many times you do 40+ damage

Matlab Script	Matlab Command Window
<pre> eq40 = 0; gt40 = 0; for n=1:1e5 A = sum(ceil(6*rand(8,1))); if(A == 40) eq40 = eq40 + 1; end if(A >= 40) gt40 = gt40 + 1; end end disp([eq40/1e5, gt40/1e5]) </pre>	

Note:

- There are multiple ways to solve any given problem

If-Elseif-Else Statements

```

if(boolean statement)
    instructions #1
elseif(boolean statement)
    instructions #2
else
    instructions #3
end

```

Execute a set of statements

- If the first condition is true, execute instructions #1 and skip the rest
- If the first condition is false, then check the second boolean statement
- If that is also false, execute instructions #3

Example: A and B play a game

- A has a 30% chance of winning (+1 point)
- A has a 50% chance of a tie (+1/2 point)
- A has a 20% chance of losing (0 points)

Matlab Script

```
Wins = 0;
X = rand;
if(X < 0.3)
    Wins = Wins + 1;
elseif(X < 0.8)
    Wins = Wins + 0.5;
else
    Wins = Wins + 0;
end
disp(['Wins = ', num2str(Wins)]);
```

Matlab Command Window

```
MATLAB 7.12.0 (R2011a)
File Edit Debug Desktop Window Help
and Settings\Administrat
Shortcuts How to Add What's New
Wins = 0.5
Wins = 0.5
Wins = 1
Wins = 0.5
Wins = 0.5
Wins = 1
Wins = 0.5
Wins = 0.5
Wins = 0.5
Wins = 0
Wins = 0.5
Wins = 0.5
Wins = 0.5
Wins = 0
Wins = 0
```

If-Else Statements (cont'd)

A die is loaded:

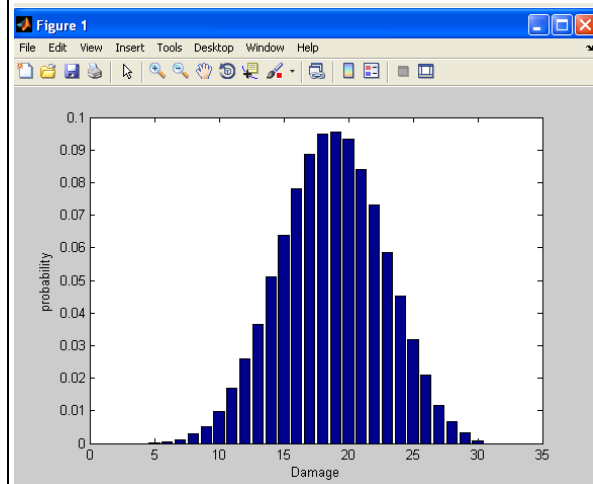
- 10% of the time, it always rolls a 6
- The rest of the time it's a fair die

What is the chance of doing X damage with a level-5 fireball?

Matlab Script

```
Damage = zeros(30,1);
for n=1:1e5
    X = 0;
    for i=1:5
        if(rand < 0.1)
            d6 = 6;
        else
            d6 = ceil(6*rand);
        end
        X = X + d6;
    end
    Damage(X) = Damage(X) + 1;
end
bar(Damage / 1e5);
xlabel('Damage');
ylabel('probability');
```

Matlab Plot Window



Note:

- Once again, the result is a bell-shaped curve
- This is *The Central Limit Theorem*
- Almost all distributions converge to this shape

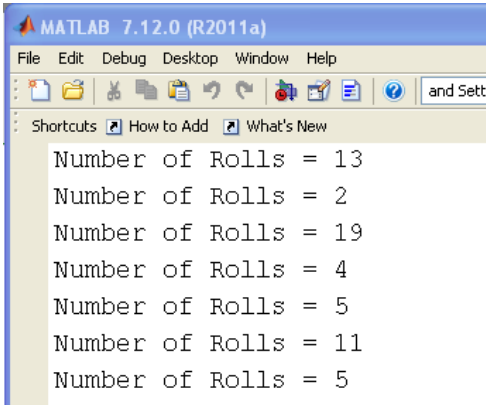
While-Loop

```
while(statement is true)
    do the following
end
```

While-loops are useful for keeping a program going until a condition is met. This can be

- Keep a simulation until time > 10 seconds,
- Keep playing a game until someone wins,
- Keep iterating until the error is less than 0.001

Example: Count how many times you roll a die until you get a 1

Matlab Script	Matlab Command Window
<pre>N = 0; d6 = 0; while(d6 ~= 1) d6 = ceil(6*rand); N = N + 1; end disp(['Number of Rolls = ',int2str(N)])</pre>	 <p>MATLAB 7.12.0 (R2011a)</p> <p>File Edit Debug Desktop Window Help</p> <p>Shortcuts How to Add What's New</p> <p>Number of Rolls = 13 Number of Rolls = 2 Number of Rolls = 19 Number of Rolls = 4 Number of Rolls = 5 Number of Rolls = 11 Number of Rolls = 5</p>

Note: in theory, N is unlimited. It could take millions of rolls until you get a 1.

While-Loop (cont'd)

What is the chance that it will take 7 or more rolls to get a 1?

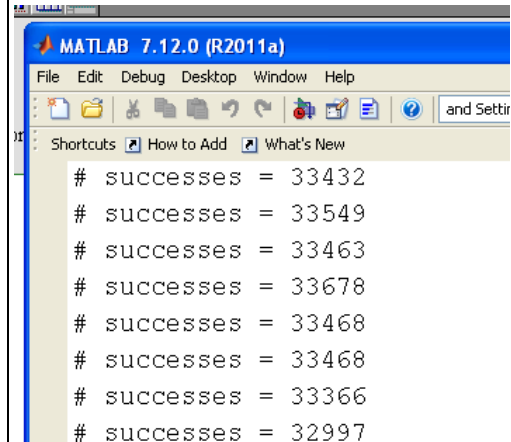
Solution:

- Count how many times you roll a die until you get a 1
- Keep track of the number of times this is 7 or more
- Repeat 100,000 times (i.e. run a Monte-Carlo Simulation)

Matlab Script

```
X = 0;
for n=1:1e5
    N = 0;
    d6 = 0;
    while(d6 ~= 1)
        d6 = ceil(6*rand);
        N = N + 1;
    end
    if(N >= 7)
        X = X + 1;
    end
end
disp(['# successes = ',int2str(X)])
```

Matlab Command Window



```
# successes = 33432
# successes = 33549
# successes = 33463
# successes = 33678
# successes = 33468
# successes = 33468
# successes = 33366
# successes = 32997
```

In 100,000 trials

- It took 7 or more rolls 33,343 times
- There is about a 33.34% chance it will take 7 or more rolls to get a 1

While-Loop (cont'd)

Player A and B are playing a match

- Player A has a 60% chance of winning any given game
- When a player is up 3 games, the match is over

What is the chance player A wins the match?

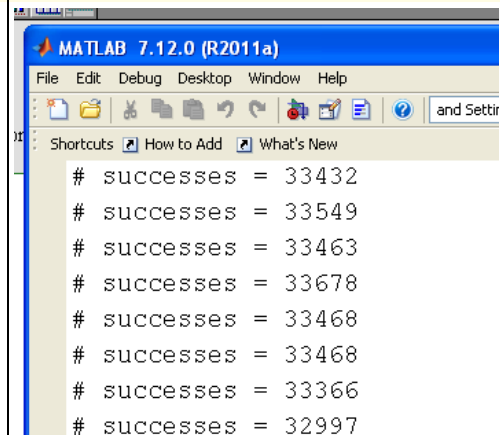
Solution: Play a single match

- If A wins, A gains 1 point.
- If A loses, A loses 1 point.
- Keep playing until A is up 3 or down 3

Matlab Script

```
A = 0;
while(abs(A) < 3)
    if(rand < 0.6)
        A = A + 1;
    else
        A = A - 1;
    end
end
if(A == 3)
    Wins = 1;
else
    Wins = 0;
end
disp(['Wins = ',int2str(Wins)])
```

Matlab Command Window



```
# successes = 33432
# successes = 33549
# successes = 33463
# successes = 33678
# successes = 33468
# successes = 33468
# successes = 33366
# successes = 32997
```

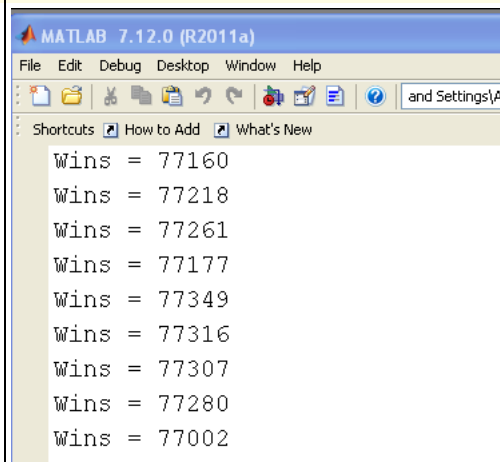
Now play 100,000 matches

- A wins about 77% of the time with this format
- TV hates this format since a match can take a very long time

Matlab Script

```
Wins = 0;
for n=1:1e5
    A = 0;
    while(abs(A) < 3)
        if(rand < 0.6)
            A = A + 1;
        else
            A = A - 1;
        end
    end
    if(A == 3)
        Wins = Wins + 1;
    end
end
disp(['Wins = ',int2str(Wins)])
```

Matlab Command Window



```
MATLAB 7.12.0 (R2011a)
File Edit Debug Desktop Window Help
Shortcuts How to Add What's New
Wins = 77160
Wins = 77218
Wins = 77261
Wins = 77177
Wins = 77349
Wins = 77316
Wins = 77307
Wins = 77280
Wins = 77002
```

Sort Command

Sort data in either

- Ascending order (default), or
- Descending order

Return

- The sorted data (one returned parameter)
- The sort order (two returned parameters)

Matlab Command Window

```
X = rand(1,5)
X =    0.1744    0.7055    0.4435    0.1654    0.0592

a = sort(X)
a =    0.0592    0.1654    0.1744    0.4435    0.7055

a = sort(X, 'descend')
a =    0.7055    0.4435    0.1744    0.1654    0.0592

[a,b] = sort(X)
a =    0.0592    0.1654    0.1744    0.4435    0.7055
b =         5         4         1         3         2
```

Sort Command & Poker

Shuffle a deck of 52 playing cards

Deal out 5 cards (poker hand)

- Hand is the card number (1..52)
- Value is Ace..King (1..13)
- Suit is Club / Diamond / Heart / Spade (1...4)

Result:

- {4s, Jh, 3s, 7h, 6s}
- {4h, Jh, Ac, Jc, 5d}

Matlab Script	Matlab Command Window				
<pre>Deck = rand(1,52); [a,b] = sort(Deck); Hand = b(1:5) Value = mod(Hand, 13) + 1 Suit = ceil(Hand / 13)</pre>	<pre>Hand = 42 36 41 32 44 Value = 4 11 3 7 6 Suit = 4 3 4 3 4</pre>				
<pre>Hand = 29 36 13 10 17 Value = 4 11 1 11 5 Suit = 3 3 1 1 2</pre>	<pre>Hand = 29 36 13 10 17 Value = 4 11 1 11 5 Suit = 3 3 1 1 2</pre>				

Check for a Full-House

Problem: Determine if your hand is a full-house.

Solution:

- Count how many Aces, twos, etc. are in your hand (variable P)
- Sort P to determine the frequency of pairs in descending order

Matlab Script	Matlab Command Window				
<pre>Deck = rand(1,52); [a,b] = sort(Deck); Hand = b(1:5); Value = mod(Hand, 13) + 1; Suit = ceil(Hand / 13); P = zeros(1,13); for i=1:13 P(i) = sum(Value == i); end P = sort(P, 'descend');</pre>	<pre>----- V 2 2 10 7 4 P 2 1 1 1 0 ----- V 11 5 5 12 4 P 2 1 1 1 0 ----- V 4 3 1 12 8 P 1 1 1 1 1 ----- V 4 4 1 4 2 P 3 1 1 0 0</pre>				
<pre>disp('-----') disp(Value); disp(P(1:5));</pre>	<pre>----- V 4 4 1 4 2 P 3 1 1 0 0</pre>				

Note:

- Hand #1 has a pair of 2's
- Hand #2 has a pair of 5's
- Hand #3 has no pairs
- Hand #4 has three 4's

Now checkI

- if $P(1) = 3$ (three of a kind) and $P(2) = 2$ (pair) then you have a full-house

Matlab Script	Matlab Command Window
<pre>FH = 0; for n=1:1e5 Deck = rand(1,52); [a,b] = sort(Deck); Hand = b(1:5); Value = mod(Hand, 13) + 1; Suit = ceil(Hand / 13); P = zeros(1,13); for i=1:13 P(i) = sum(Value == i); end P = sort(P, 'descend'); if ((P(1)==3) * (P(2)==2)) FH = FH + 1; end end disp(['Full House = ',int2str(FH)])</pre>	<pre>Full House = 141 Full House = 133 Full House = 162 Full House = 124 Full House = 119 Full House = 154</pre>

Note:

- The number of full-houses you get in 100,000 hands of poker changes each time you run the Monte Carlo simulation (it's a random process)

With this, you can answer questions, such as

- What is the range in numbers I'll get?
- What is the actual probability of getting a full house?

This is something covered in ECE 341 Random Processes and week #12 in ECE 111.

Summary

Matlab is a fairly friendly computer language

You can use the command window as a calculator

- Adds, subtracts, multiplies, divides

Scripts allow you to try & modify code as you write it

For-loops let you run code multiple times

- Monte-Carlo simulations...

If-statements allow you to check for conditions

- If the sum is 25 or more...

While-loops let you run code until an event happens

- repeat until you roll a 1

Matlab Commands

Display

- `format short` display results to 4 decimal places
- `format long` display results to 13 decimal places
- `format short e` display using scientific notation
- `format long e` display using scientific notation

Polynomials

- `poly(x)`
- `roots(x)`
- `conv(x,y)`

Analysis

- `sqrt(x)` square root of x
- `log(x)` log base e
- `log10(x)` log base 10
- `exp(x)` e^x
- `exp10(x)` 10^x
- `abs(x)` $|x|$
- `round(x)` round to the nearest integer
- `floor(x)` round down (integer value of x)
- `ceil(x)` round up to the next integer
- `real(x)` real part of a complex number
- `imag(x)` imaginary part of a complex number
- `abs(x)` absolute value of x, magnitude of a complex number
- `angle(x)` angle of a complex number (answer in radians)
- `unwrap(x)` remove the discontinuity at pi (180 degrees) for a vector of angles
- `sum(x)` sum the columns of x
- `prod(x)` multiply the columns of x

Trig Functions

- `sin(x)` `sin(x)` where x is in radians
- `cos(x)` `cos()`
- `tan(x)` `tan()`
- `asin(x)` `arcsin(x)`
- `acos(x)` `arccos(x)`
- `atan(x)` `arctan(x)`
- `atan2(y,x)` angle to a point (x,y)

Probability and Statistics

- `factorial(x)` `x!`
- `gamma(x)` `x!`
- `rand(n,m)` create an nxm matrix of random numbers between 0 and 1
- `randn(n,m)` create an nxm matrix of random numbers with a normal distribution
- `length(x)` return the dimensions of x
- `mean(x)` mean (average) of the columns of x
- `std()` standard deviation of the columns of x

Display Functions

- `plot(x)` plot x vs sample number
- `plot(x,y)` plot x vs. y

Rolling Dice:

- `rand` generate a random number in the range of (0, 1)
- `rand(1,5)` generate a 1x5 matrix of random numbers in the range of (0, 1)
- `randn` generate a random number with a normal distribution with mean=0, std=1

Example: Generate a random number between 0 and 1:

```
rand
    0.8147

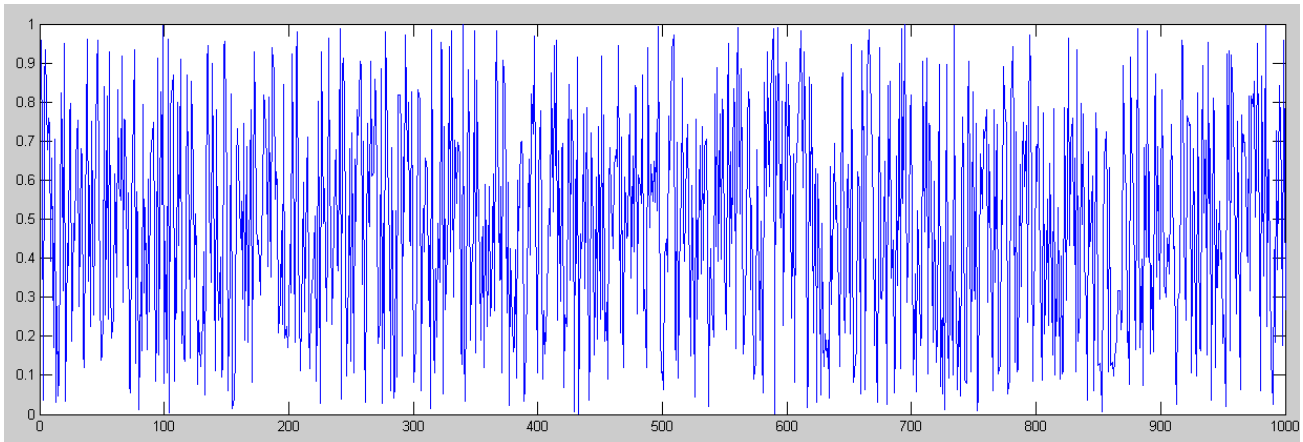
rand
    0.9058
```

Generate 5 random numbers between 0 and 1

```
rand(1,5)
    0.8003    0.1419    0.4218    0.9157    0.7922
```

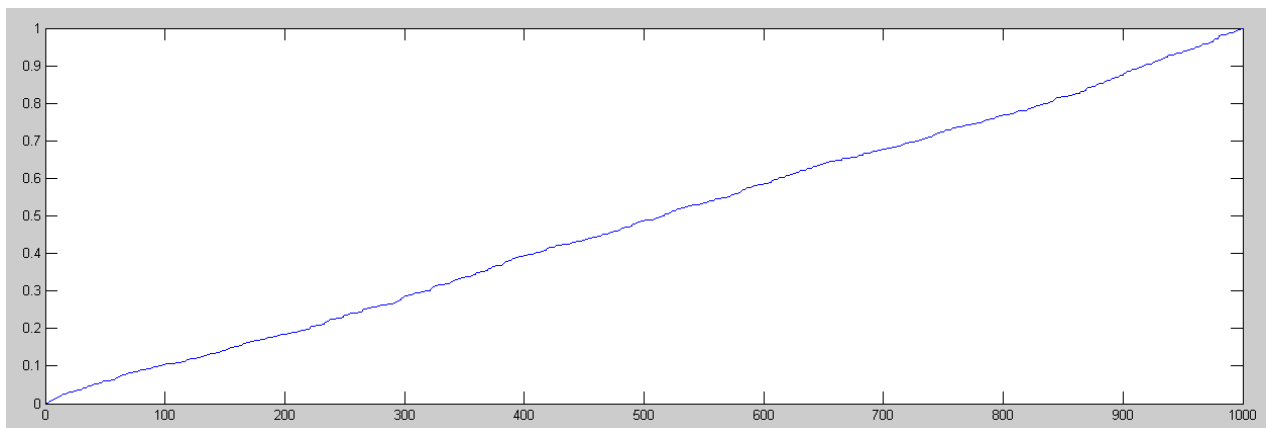
Generate 1000 random numbers and plot them

```
x = rand(1,1000);
plot(x)
```



If you sort the numbers, you can see the probability distribution function (approximately)

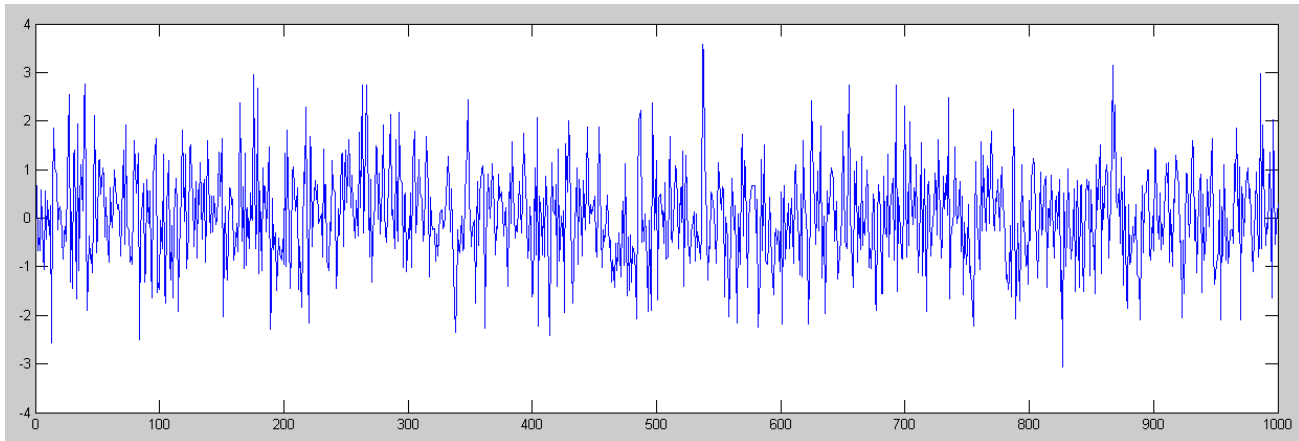
```
y = sort(x);
plot(y)
```



Each number from (0, 1) should have the same likelihood of coming up, meaning when you sort the numbers, the result should be a straight line

Compare this to a Normal distribution

```
x = randn(1,1000);  
plot(x)
```



This is more what you'd see for

- Stock prices
- Temperatures
- Height of people,
- etc.

You have to watch which random number generator you're using. *rand()* is different from *randn()*

With this you can have fun with rolling dice:

Problem: Find the sum of rolling five six-sided dice. (5d6)

Solution: Generate five random numbers in the range of (0,1)

```
rand(1,5)  
0.7298    0.8908    0.9823    0.7690    0.5814
```

Looks right. Now generate five random integers in the range of (1,6)

```
dice = ceil( 6*rand(1,5) )  
3     6     2     4     4  
  
dice = ceil( 6*rand(1,5) )  
1     4     3     1     3
```

Looks right. Now, find the total:

```
sum( ceil( 6*rand(1,5) ) )
```

8

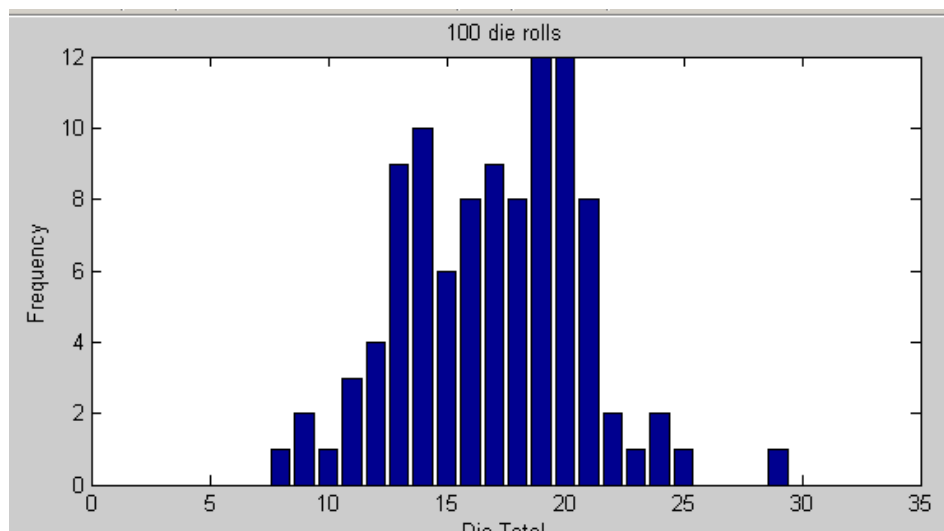
```
sum( ceil( 6*rand(1,5) ) )
```

16

Each time you roll the dice, you get a different answer. It's random.

Problem: Roll 5d6 one-hundred times and record how many rolls you get for each total:

```
X = zeros(30,1);  
for i=1:100  
    D = sum( ceil( 6*rand(1,5) ) );  
    X(D) = X(D) + 1;  
end  
bar(X)  
xlabel('Die Total');  
ylabel('Frequency');  
title('100 die rolls')
```

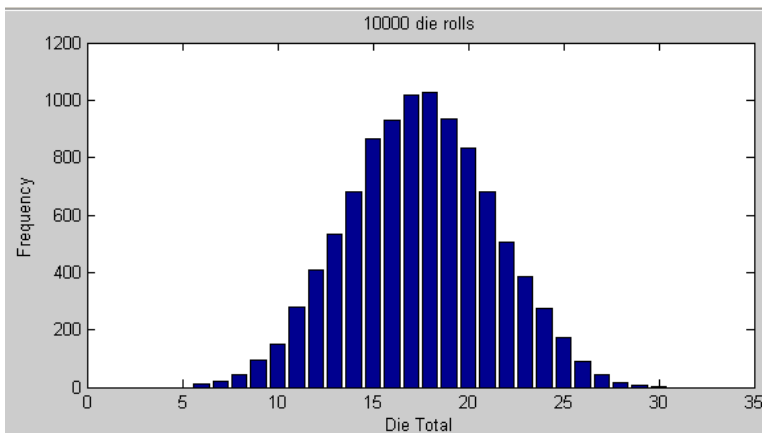


This looks pretty erratic. If you roll the dice 10,000 times, it becomes much better behaved:

Roll 5d6 10,000 times and record the frequency of each outcome:

```
X = zeros(30,1);  
for i=1:10000  
    D = sum( ceil( 6*rand(1,5) ) );  
    X(D) = X(D) + 1;  
end  
bar(X)
```

```
xlabel('Die Total');
ylabel('Frequency');
title('10000 die rolls')
```



This is the *Central Limit Theorem*. As the sample size goes to infinity, you get a Normal distribution.

Problem: What's the probability of rolling a 25 or higher with 5d6?

Solution: Toss the dice 1,000,000 times and count the number of times you got 25 or higher. The probability is then approximately this result divided by 1,000,000

```
X = 0;
for i=1:1000000
    D = sum( ceil( 6*rand(1,5) ) );
    if (D >= 25)
        X = X + 1;
    end
end
```

X

32348

X / 1e6

0.0323

There is approximately a 3.23% chance of rolling a 25 or higher with 5d6

Problem: Instead of adding the total of five 6-sided dice (5d6), add d6 + d8 + d10 + d12 + d20. What's the distribution look like?

Solution: Roll the dice once

```
d6 = ceil(6*rand);
d8 = ceil(8*rand);
```

```
d10 = ceil(10*rand);
d12 = ceil(12*rand);
d20 = ceil(20*rand);

[d6,d8,d10,d12,d20]

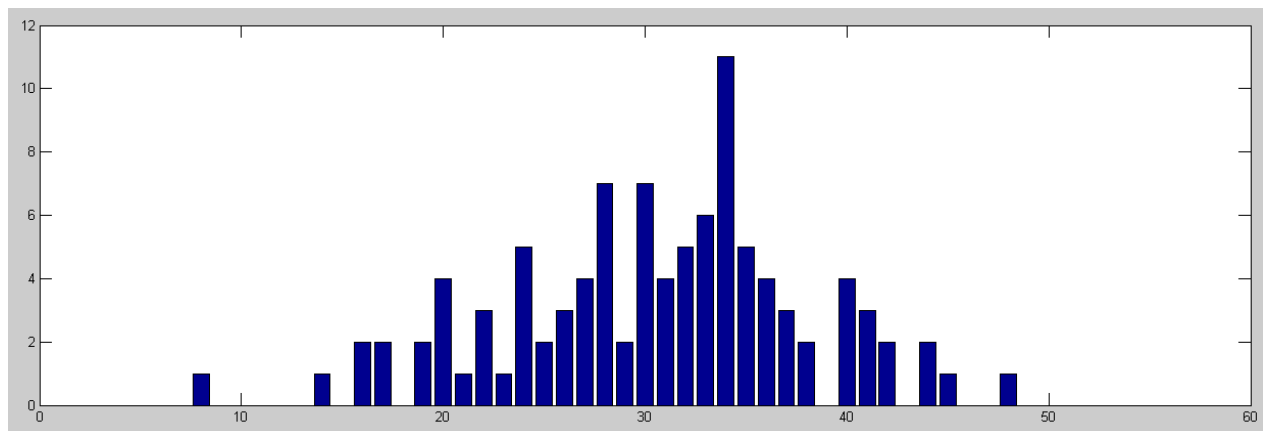
     1     5     4     1     2

ROLL = sum([d6,d8,d10,d12,d20])

    13
```

Now do it 100 times

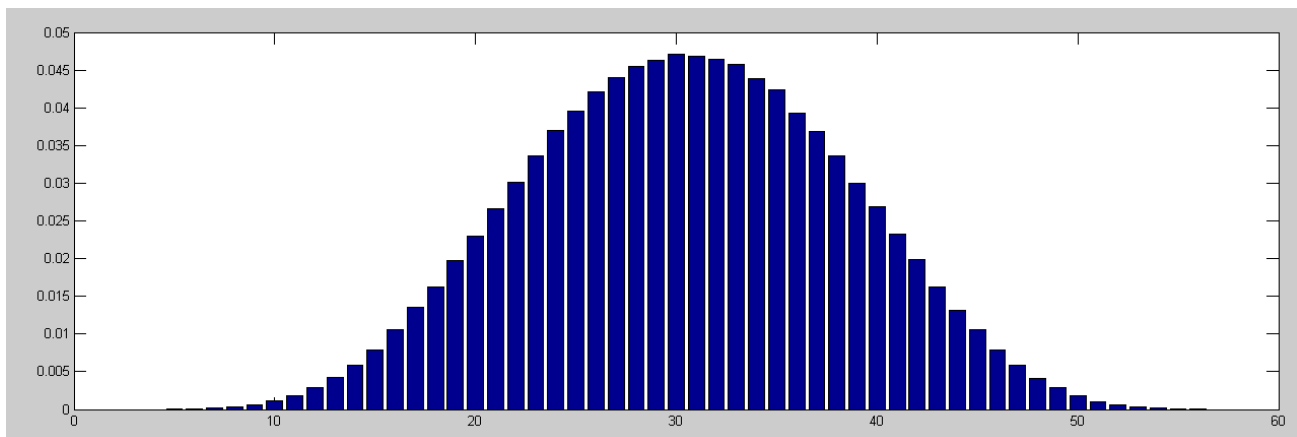
```
RESULT = zeros(56,1);
for i=1:100
    d6 = ceil(6*rand);
    d8 = ceil(8*rand);
    d10 = ceil(10*rand);
    d12 = ceil(12*rand);
    d20 = ceil(20*rand);
    ROLL = sum([d6,d8,d10,d12,d20]);
    RESULT(ROLL) = RESULT(ROLL) + 1;
end
bar(RESULT)
```



This is pretty erratic. To get a smoother plot, use the Central Limit theorem and roll the dice a lot more (1,000,000 times):

```
RESULT = zeros(56,1);
for i=1:1000000
    d6 = ceil(6*rand);
    d8 = ceil(8*rand);
    d10 = ceil(10*rand);
    d12 = ceil(12*rand);
    d20 = ceil(20*rand);
    ROLL = sum([d6,d8,d10,d12,d20]);
    RESULT(ROLL) = RESULT(ROLL) + 1;
end

bar(RESULT / 1000000)
```



What's the probability of rolling a 17?

```
RESULT(17) / 1e6
```

```
0.0135
```

There's a 1.35% chance of rolling a 17.

What's the probability of rolling a 50 or higher?

```
sum(RESULT(50:56)) / 1e6
```

```
0.0040
```

There's a 0.40% chance of rolling a 50 or higher.

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- `prod(x)` multiply the columns of x
- `sort(x)` sort the columns of x from smallest to largest

-
- `length(x)` return the dimensions of x
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Display Functions

- `plot(x)` plot x vs sample number
- `plot(x,y)` plot x vs. y
- `semilogx(x,y)` log(x) vs y
- `semilogy(x,y)` x vs log(y)
- `loglog(x,y)` log(x) vs log(y)
- `mesh(x)` 3d plot where the height is the value at x(a,b)
- `contour(x)` contour plot
- `bar(x,y)` draw a bar graph
- `xlabel('time')` label the x axis with the word 'time'
- `ylabel()` label the y axis
- `title()` put a title on the plot
- `grid()` draw the grid lines

Useful Commands

- `hold on` don't erase the current graph
- `hold off` do erase the current graph
- `diary` create a text file to save whatever goes to the screen
- `linspace(a, b, n)` create a 1xn array starting at a, increment by b
- `logspace(a,b,n)` create a 1xn array starting at 10^a going to 10^b , spaced logarithmically
- `subplot()` create several plots on the same screen
- `disp('hello')` display the message *hello*

Utilities

- `format` set the display format
- `zeros(n,m)` create an nxm matrix of zeros
- `eye(n,m)` create an nxm matrix with ones on the diagonal
- `ones(n,m)` create an nxm matrix of ones
- `help` help using different functions
- `pause(x)` pause x seconds (can be a fraction). Show the graph as well
- `clock` the present time
- `etime` the difference between to times
- `tic` start a stopwatch
- `toc` the number of seconds since tic