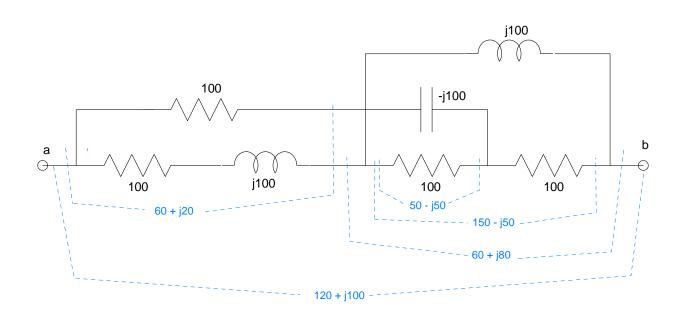
April 24, 2019

1) Determine the impedance Zab

$$Zab = 120 + j100$$



$$(100+j100)||(100) = 60+j20$$

$$100||-j100 = 50-j50$$

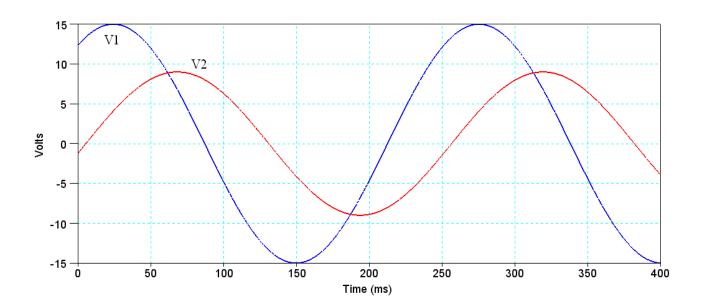
$$(50-j50)+100 = 150-j50$$

$$(150-j50)||(j100) = 60+j80$$

$$(60+j20)+(60+j80)=120+j100$$

2) Determine the frequency and phasor representation for V1 and V2

Frequency (Hz)	V1		V2	
	Amplitude (Vp)	Phase (degrees)	Amplitude (Vp)	Phase (degrees)
4.0 Hz	15.0 V	-36 deg	9.0 V	-100.8 deg



Period:

$$T = 255ms - 5ms - 250ms$$
$$f = \frac{1}{T} = \frac{1}{250ms} = 4Hz$$

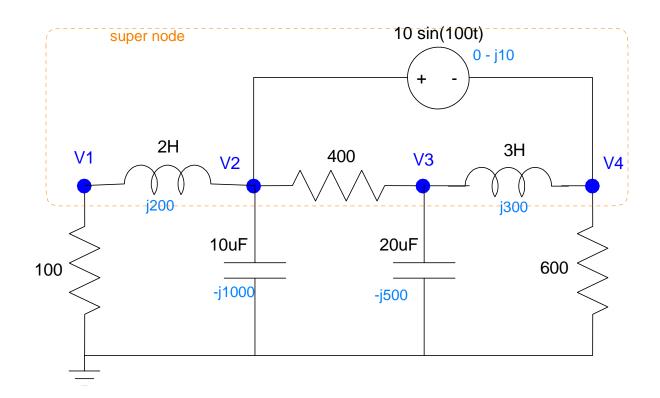
$$\phi_1 = - \! \left(\tfrac{25 ms \ delay \ to \ peak}{250 ms \ period} \right) \cdot 360^0$$

$$\phi_1 = -36^0$$

$$\phi_2 = - \left(\frac{\text{70ms delay to peak}}{\text{250ms period}} \right) \cdot 360^0$$

$$\phi_2 = -100.8^0$$

3) Write N equations to allow you to solve for the N unknown voltages



$$L \to j\omega L$$

$$C \to \frac{1}{j\omega C}$$

$$a\cos(\omega t) + b\sin(\omega t) \to a - jb$$

Equations:

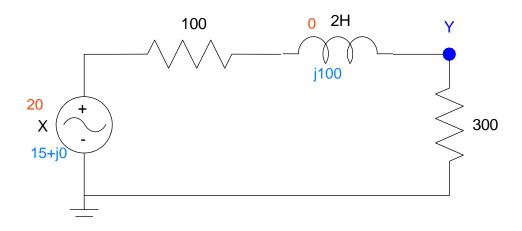
$$\begin{split} V_2 - V_4 &= -j10 \\ \left(\frac{V_1}{100}\right) + \left(\frac{V_1 - V_2}{j200}\right) &= 0 \\ \left(\frac{V_3 - V_2}{400}\right) + \left(\frac{V_3}{-j500}\right) + \left(\frac{V_3 - V_4}{j300}\right) &= 0 \\ \left(\frac{V_1}{100}\right) + \left(\frac{V_2}{-j1000}\right) + \left(\frac{V_3}{-j500}\right) + \left(\frac{V_4}{600}\right) &= 0 \end{split}$$

4) Assume

$$x(t) = 20 + 15\cos(50t)$$

Determine the voltage, y(t)

$$y(t) = 15 + 10.59\cos(50t) + 2.65\sin(50t)$$



$$L \to j\omega L = 0 \qquad L \to j\omega L = j100$$

$$Y = \left(\frac{300}{300+100}\right)20 \qquad 15\cos(50t) + 0\sin(50t) \to 15 - j0$$

$$Y = 15 \qquad Y = \left(\frac{300}{(300)+(100+j100)}\right)(15-j0)$$

$$Y = 10.59 - j2.65$$

$$y(t) = 15$$
 $y(t) = 10.59\cos(50t) + 2.65\sin(50t)$

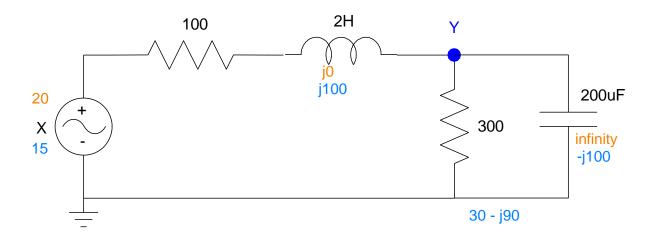
The total answer is the DC term plus the AC term

5) Assume

$$x(t) = 20 + 15\cos(50t)$$

Determine the voltage, y(t)

$$y(t) = 15 + 2.65\cos(50t) + 10.59\sin(50t)$$



DC (orange) AC (blue)
$$Y = \left(\frac{300}{300+100}\right) 20 \qquad L \to j\omega L = j100$$

$$Y = 15 \qquad C \to \frac{1}{j\omega C} = -j100$$

$$y(t) = 15 \qquad V \to 15 - j0$$

$$(300) | | (-j100) = 30 - j90$$

$$Y = \left(\frac{(30-j90)}{(30-j90)+(100+j100)}\right) (15-j0)$$

$$Y = 2.65 - j10.59$$

$$y(t) = 2.65 \cos(50t) + 10.59 \sin(50t)$$

The total answer is the DC plus the AC term

Bonus! Suggest one thing that the U.S. government could do to reduce income inequality (currently done in the U.S.A)

Make K-12 education free

• Victorian England: only the wealthy could afford to send their kids to school

Make college affordable (public universities)

• Land Grants like NDSU

Have a progressive tax system (people who make more pay a higher percentage)

- 0% tax rate if you make less than \$12,000 / year (standard deduction)
- *37% for income above \$510,000*

Have a minimum wage

• 1900's wages were 25 cents per day with 14 hour work days

Establish trade unions

- Check on management.
- Profits must be shared or else you get a strike

Have an inheritance tax

• Make it harder to accumulate massive wealth over generations

(currently done elsewhere)

Half of the board of trustees must be hourly workers (Germany, Iceland)

- Profits must be shared more equitably
- More prone to invest in a factory to keep jobs local than moving production over seas

Make college free (Germany, Norway, Spain, elsewhere)

• Everyone has a chance to go to college - regardless of how rich your parents are

(Other ideas being kicked around...)

Implent a salary cap (through the tax code: 90% income tax on income above \$10 million - Eisenhauer)

- No point in keeping all of a company's profits to yourself (90% tax rate).
- Profits have to go somewhere else, like investing in the company, paying employees more, investing in the community

Raise the inheritance tax on inheritances above \$10 million (Pommeroy)

- The greatest sin a person can do is to die rich. Andrew Carnigie.
- Do something with your wealth before you die: build a university, cure a disease, start a company...
- A voluntary tax: if you don't want to pay it, don't die rich.

Tax all income the same (capital gains are treated like other income)

- Most inventment income goes to the wealthy (people with money to invest).
- Currently the capital gains tax rate (20%) is about half of the income tax rate (37%)

Raise the minimum wage