## EE 206 Test \#3 - Name

April 24, 2019

1) Determine the impedance Zab

## Zab = 120 + $\mathbf{j 1 0 0}$


$120+j 100$

$$
\begin{array}{ll}
(100+j 100) \|(100)=60+j 20 & 100 \|-j 100=50-j 50 \\
& (50-j 50)+100=150-j 50 \\
& (150-j 50) \|(j 100)=60+j 80
\end{array}
$$

$$
(60+j 20)+(60+j 80)=120+j 100
$$

2) Determine the frequency and phasor representation for V1 and V2

| Frequency <br> $(\mathrm{Hz})$ | V 1 |  | V 2 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Amplitude $(\mathrm{Vp})$ | Phase (degrees) | Amplitude $(\mathrm{Vp})$ | Phase (degrees) |
| $\mathbf{4 . 0 ~ H z}$ | $\mathbf{1 5 . 0} \mathrm{V}$ | $\mathbf{- 3 6} \mathbf{~ d e g}$ | $\mathbf{9 . 0} \mathrm{V}$ | $\mathbf{- 1 0 0 . 8 ~ d e g}$ |



Period:

$$
T=255 m s-5 m s-250 m s
$$

$$
f=\frac{1}{T}=\frac{1}{250 \mathrm{~ms}}=4 \mathrm{~Hz}
$$

$$
\phi_{1}=-\left(\frac{25 \mathrm{~ms} \text { delay to peak }}{250 \mathrm{~ms} \mathrm{period}}\right) \cdot 360^{0}
$$

$$
\phi_{1}=-36^{0}
$$

$$
\phi_{2}=-\left(\frac{70 \mathrm{~ms} \text { delay to peak }}{250 \mathrm{~ms} \text { period }}\right) \cdot 360^{0}
$$

$$
\phi_{2}=-100.8^{0}
$$

3) Write N equations to allow you to solve for the N unknown voltages


$$
\begin{aligned}
& L \rightarrow j \omega L \\
& C \rightarrow \frac{1}{j \omega C}
\end{aligned}
$$

$$
a \cos (\omega t)+b \sin (\omega t) \rightarrow a-j b
$$

Equations:

$$
\begin{aligned}
& V_{2}-V_{4}=-j 10 \\
& \left(\frac{V_{1}}{100}\right)+\left(\frac{V_{1}-V_{2}}{j 200}\right)=0 \\
& \left(\frac{V_{3}-V_{2}}{400}\right)+\left(\frac{V_{3}}{-j 500}\right)+\left(\frac{V_{3}-V_{4}}{j 300}\right)=0 \\
& \left(\frac{V_{1}}{100}\right)+\left(\frac{V_{2}}{-j 1000}\right)+\left(\frac{V_{3}}{-j 500}\right)+\left(\frac{V_{4}}{600}\right)=0
\end{aligned}
$$

4) Assume

$$
x(t)=20+15 \cos (50 t)
$$

Determine the voltage, $\mathrm{y}(\mathrm{t})$

$$
y(t)=15+10.59 \cos (50 t)+2.65 \sin (50 t)
$$



DC (orange)

$$
\begin{array}{ll}
L \rightarrow j \omega L=0 & L \rightarrow j \omega L=j 100 \\
Y=\left(\frac{300}{300+100}\right) 20 & 15 \cos (50 t)+0 \sin (50 t) \rightarrow 15-j 0 \\
Y=15 & Y=\left(\frac{300}{(300)+(100+j 100)}\right)(15-j 0) \\
& Y=10.59-j 2.65 \\
y(t)=15 & y(t)=10.59 \cos (50 t)+2.65 \sin (50 t)
\end{array}
$$

The total answer is the DC term plus the AC term
5) Assume

$$
x(t)=20+15 \cos (50 t)
$$

Determine the voltage, $\mathrm{y}(\mathrm{t})$
$y(t)=15+2.65 \cos (50 t)+10.59 \sin (50 t)$


DC (orange)

$$
\begin{aligned}
& Y=\left(\frac{300}{300+100}\right) 20 \\
& Y=15 \\
& y(t)=15
\end{aligned}
$$

AC (blue)

$$
\begin{aligned}
& L \rightarrow j \omega L=j 100 \\
& C \rightarrow \frac{1}{j \omega C}=-j 100 \\
& \quad V \rightarrow 15-j 0 \\
& (300) \|(-j 100)=30-j 90 \\
& Y=\left(\frac{(30-j 90)}{(30-j 90)+(100+j 100)}\right)(15-j 0) \\
& Y=2.65-j 10.59 \\
& y(t)=2.65 \cos (50 t)+10.59 \sin (50 t)
\end{aligned}
$$

The total answer is the DC plus the AC term

Bonus! Suggest one thing that the U.S. government could do to reduce income inequality ( currently done in the U.S.A )
Make K-12 education free

- Victorian England: only the wealthy could afford to send their kids to school

Make college affordable ( public universities )

- Land Grants like NDSU

Have a progressive tax system (people who make more pay a higher percentage)

- $0 \%$ tax rate if you make less than $\$ 12,000 /$ year (standard deduction)
- $37 \%$ for income above $\$ 510,000$

Have a minimum wage

- 1900's wages were 25 cents per day with 14 hour work days

Establish trade unions

- Check on management.
- Profits must be shared or else you get a strike

Have an inheritance tax

- Make it harder to accumulate massive wealth over generations
( currently done elsewhere )
Half of the board of trustees must be hourly workers ( Germany, Iceland )
- Profits must be shared more equitably
- More prone to invest in a factory to keep jobs local than moving production over seas

Make college free ( Germany, Norway, Spain, elsewhere )

- Everyone has a chance to go to college - regardless of how rich your parents are
( Other ideas being kicked around... )
Implent a salary cap ( through the tax code: $90 \%$ income tax on income above $\$ 10$ million - Eisenhauer )
- No point in keeping all of a company's profits to yourself ( $90 \%$ tax rate ).
- Profits have to go somewhere else, like investing in the company, paying employees more, investing in the community
Raise the inheritance tax on inheritances above $\$ 10$ million (Pommeroy )
- The greatest sin a person can do is to die rich. Andrew Carnigie.
- Do something with your wealth before you die: build a university, cure a disease, start a company...
- A voluntary tax: if you don't want to pay it, don't die rich.

Tax all income the same ( capital gains are treated like other income )

- Most inventment income goes to the wealthy (people with money to invest).
- Currently the capital gains tax rate (20\%) is about half of the income tax rate (37\%)

Raise the minimum wage

