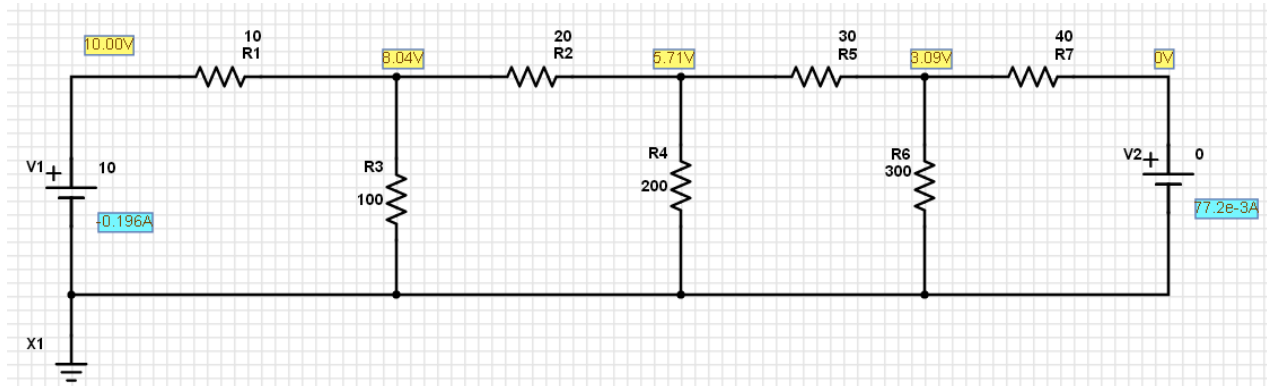


# EE 206: Homework #6

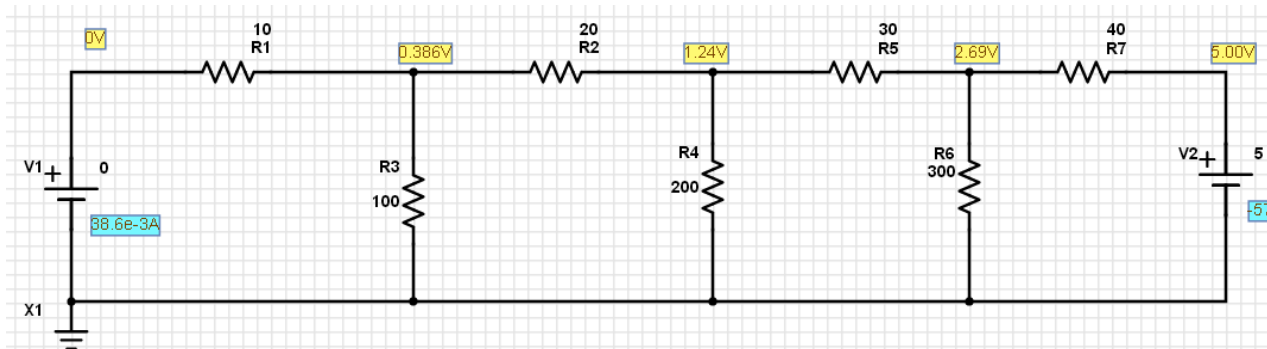
Superposition and Op Amps. Due Monday March 2nd

## Superposition

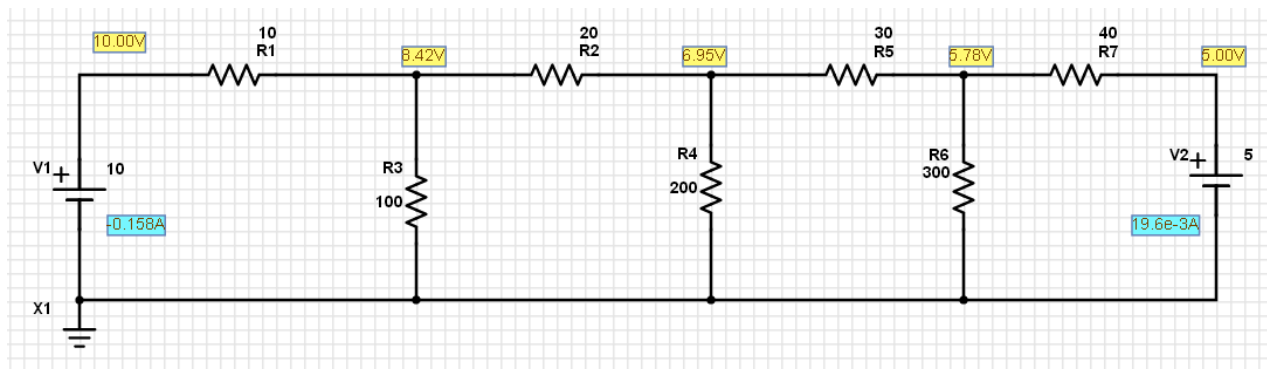
1) Use PartSim to determine the voltage at Y assuming  $V_a = 10V$ ,  $V_b = 0V$ .



2) Use PartSim to determine the voltage at Y assuming  $V_a = 0V$ ,  $V_b = 5V$ .



3) Use PartSim to determine the voltage at Y assuming  $V_1 = 10V$ ,  $V_b = 5V$



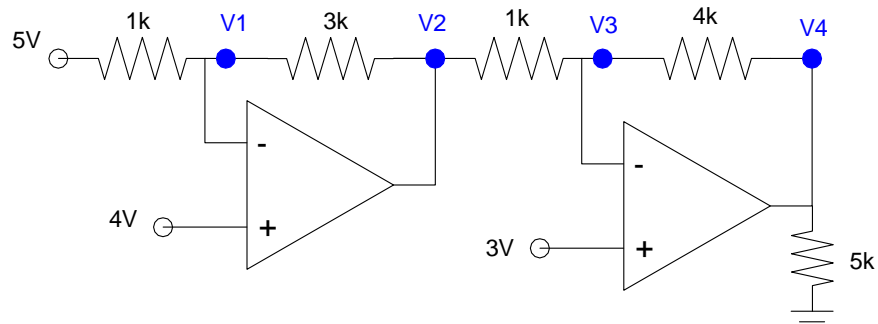
Does problem 1 + problem 2 = problem 3?

	Va	V1	V2	V3	Vb
Va = 10V Vb = 0V	10.00V	8.04 V	5.71 V	3.09 V	0.00 V
Va = 0V Vb = 5V	0.00 V	0.386 V	1.24 V	2.69 V	5.00 V
Va = 10V Vb = 5V	10.00 V	8.42 V	6.95 V	5.78 V	5.00 V

Yes, problem 1 + problem 2 = problem 3

## Op Amps

- 4) Write the voltage node equations for the following op-amp circuit. Assume ideal op-amps.
- Solve for  $V_1$ ,  $V_2$ ,  $V_3$ , and  $V_4$



Start with  $V_+ = V_-$

$$V_1 = 4V$$

$$V_3 = 3V$$

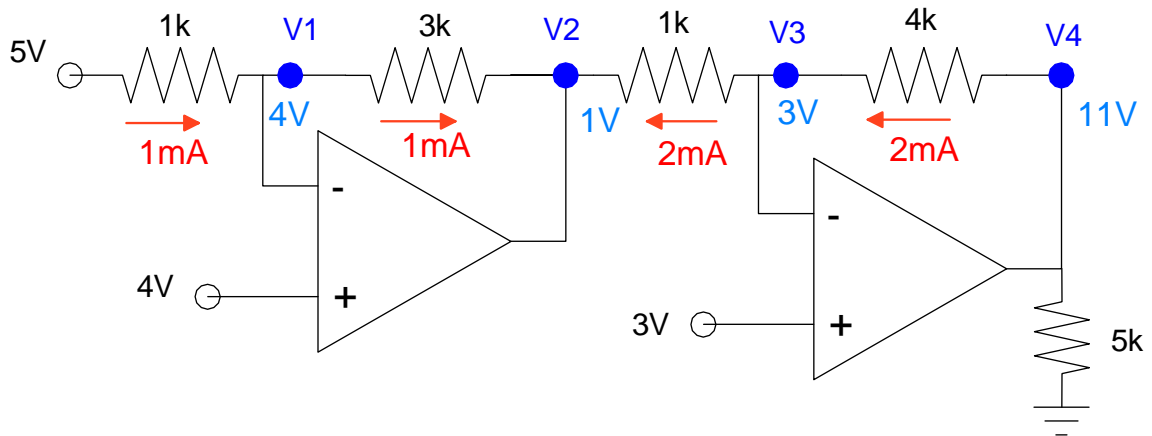
Write the voltage node equation at  $V_1$  and  $V_3$

$$\left(\frac{V_1 - 5}{1k}\right) + \left(\frac{V_1 - V_2}{3k}\right) = 0$$

$$\left(\frac{V_3 - V_2}{1k}\right) + \left(\frac{V_3 - V_4}{4k}\right) = 0$$

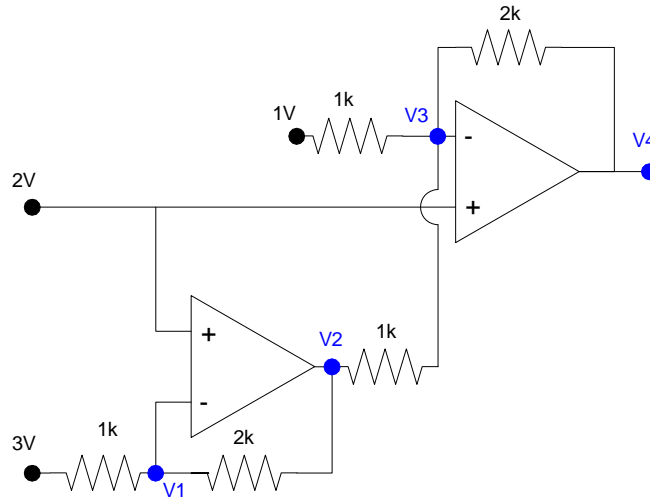
Solving:

- $V_1 = 4V$
- $V_2 = -5V$
- $V_3 = 3V$
- $V_4 = 35V$



5) Write the voltage node equations for the following op-amp circuit. Assume ideal op-amps.

- Solve for V1, V2, V3, and V4 assuming ideal op-amps



Start with  $V_+ = V_-$

$$V_1 = 2V$$

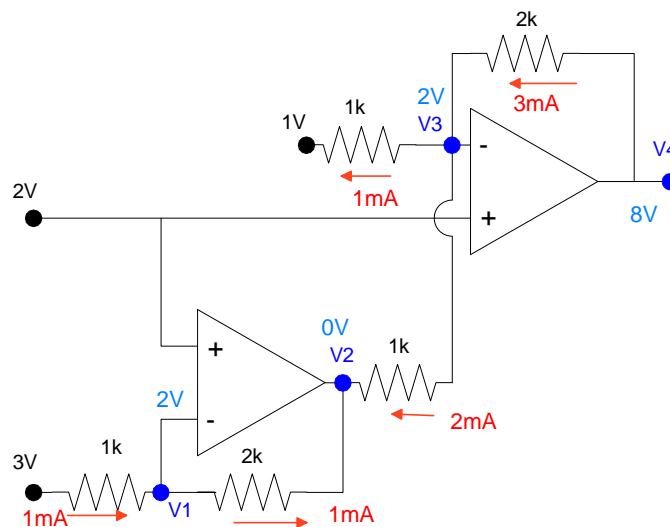
$$V_3 = 2V$$

Write the voltage node equations at V1 and V3

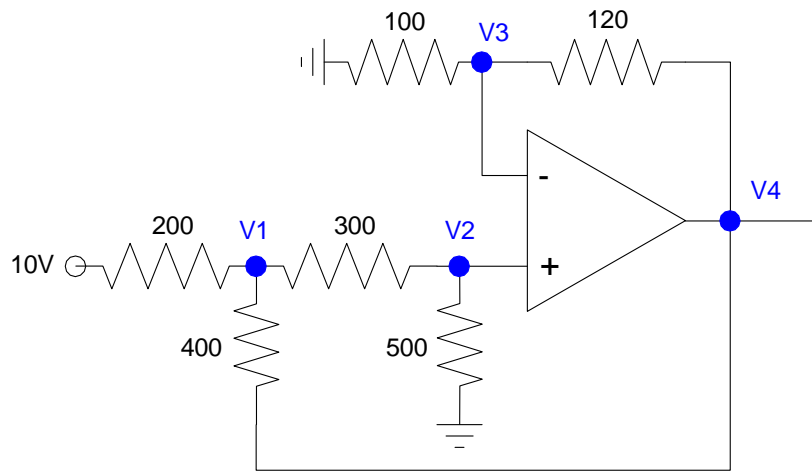
$$\left(\frac{V_1 - 3}{1k}\right) + \left(\frac{V_1 - V_2}{2k}\right) = 0$$

$$\left(\frac{V_3 - 1}{1k}\right) + \left(\frac{V_3 - V_2}{1k}\right) + \left(\frac{V_3 - V_4}{2k}\right) = 0$$

Solving



- 6) Write the voltage node equations for the following op-amp circuit. Assume ideal op-amps.
- Solve for  $V_1$ ,  $V_2$ ,  $V_3$ , and  $V_4$  assuming ideal op-amps



Start with  $V_+ = V_-$

$$V_2 = V_3$$

Write the voltage node equations at  $V_1$ ,  $V_2$ , and  $V_3$

$$\left( \frac{V_1 - 10}{200} \right) + \left( \frac{V_1 - V_2}{300} \right) + \left( \frac{V_1 - V_4}{400} \right) = 0$$

$$\left( \frac{V_2 - V_1}{300} \right) + \left( \frac{V_2}{500} \right) = 0$$

$$\left( \frac{V_3}{100} \right) + \left( \frac{V_3 - V_4}{120} \right) = 0$$

Solve...

Group terms

$$V_2 - V_3 = 0$$

$$\left(\frac{1}{200} + \frac{1}{300} + \frac{1}{400}\right)V_1 - \left(\frac{1}{300}\right)V_2 - \left(\frac{1}{400}\right)V_4 = \left(\frac{10}{200}\right)$$

$$-\left(\frac{1}{300}\right)V_1 + \left(\frac{1}{300} + \frac{1}{500}\right)V_2 = 0$$

$$\left(\frac{1}{100} + \frac{1}{120}\right)V_3 - \left(\frac{1}{120}\right)V_4 = 0$$

Place in matrix form

$$\begin{bmatrix} 0 & 1 & -1 & 0 \\ \left(\frac{1}{200} + \frac{1}{300} + \frac{1}{400}\right) & \left(\frac{-1}{300}\right) & 0 & \left(\frac{-1}{400}\right) \\ \left(\frac{-1}{300}\right) & \left(\frac{1}{300} + \frac{1}{500}\right) & 0 & 0 \\ 0 & 0 & \left(\frac{1}{100} + \frac{1}{120}\right) & \left(\frac{-1}{120}\right) \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \\ V_4 \end{bmatrix} = \begin{bmatrix} 0 \\ \left(\frac{10}{200}\right) \\ 0 \\ 0 \end{bmatrix}$$

Solve using Matlab

```
A = [0,1,-1,0];  
A = [A ; 1/200+1/300+1/400, -1/300, 0, -1/400];  
A = [A ; -1/300, 1/300+1/500, 0, 0];  
A = [A ; 0, 0, 1/100+1/120, -1/120]  
  
0. 1. - 1. 0.  
0.0108333 - 0.0033333 0. - 0.0025  
- 0.0033333 0.0053333 0. 0.  
0. 0. 0.0183333 - 0.0083333
```

```
B = [0;10/200;0;0]
```

```
0.  
0.05  
0.  
0.
```

```
V = inv(A)*B
```

```
v1 9.4117647  
v2 5.8823529  
v3 5.8823529  
v4 12.941176
```