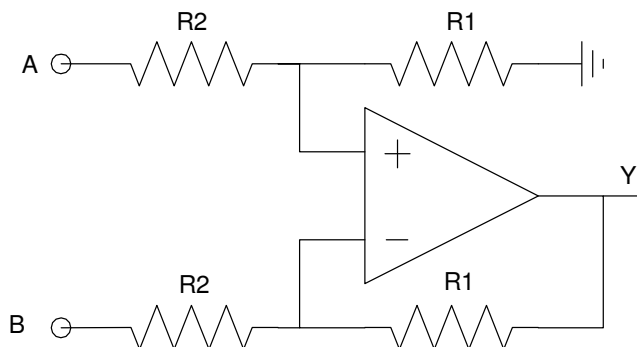


# Instrumentation Amplifiers

## Instrumentation Amplifiers

The transfer function for an instrumentation amplifier is



$$Y = \left(\frac{R_1}{R_2}\right) (A - B)$$

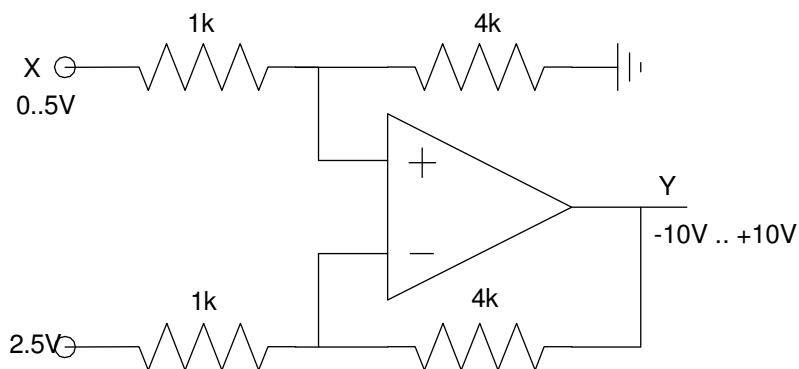
### Case 1: Voltage Amplification

Design a circuit to convert a 0.5V signal in to a +/- 10V signal.

- X = 0.5V analog
- Y = -10 .. +10V analog
- Y = 4X - 10

Solution: Rewrite this as

$$Y = 4(X - 2.5)$$



Level Shifter: 0.5V signal is amplified to -10V .. +10V

**Case 2:  $V = f(R)$** 

Assume R varies from 2000 Ohms to 2200 Ohms. Design a circuit which outputs

- -10V when R = 2000 Ohms
- +10V when R = 2200 Ohms

Solution: Convert R to a voltage using a voltage divider. Assume a 2100 Ohm resistor

R = 2000 Ohms:

$$V_x = \left( \frac{2000}{2000+2100} \right) 10V = 4.878V$$

$$Y = -10V$$

R = 2200 Ohms

$$V_x = \left( \frac{2200}{2200+2100} \right) 10V = 5.116V$$

$$Y = +10V$$

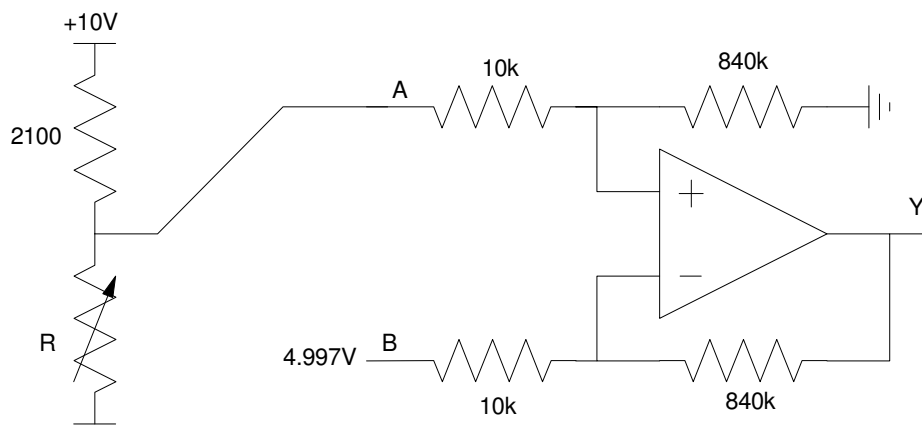
The gain you need is

$$gain = \left( \frac{\text{change in output}}{\text{change in input}} \right) = \left( \frac{10V - (-10V)}{5.116V - 4.878V} \right)$$

$$gain = 83.95$$

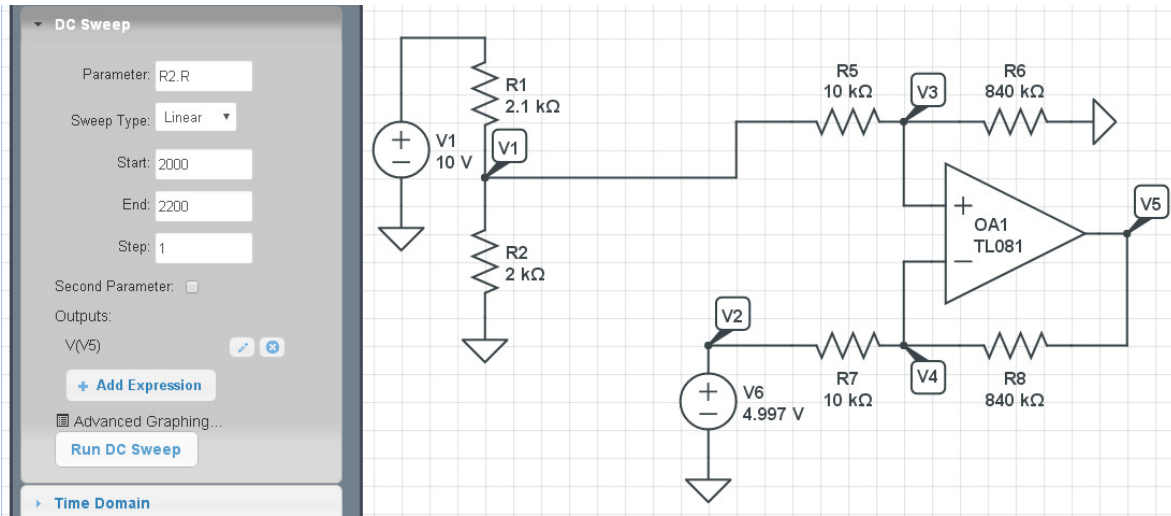
The output should be 0V (midband) when the input is midband

$$V_b = \left( \frac{4.878V + 5.116V}{2} \right) = 4.997V$$

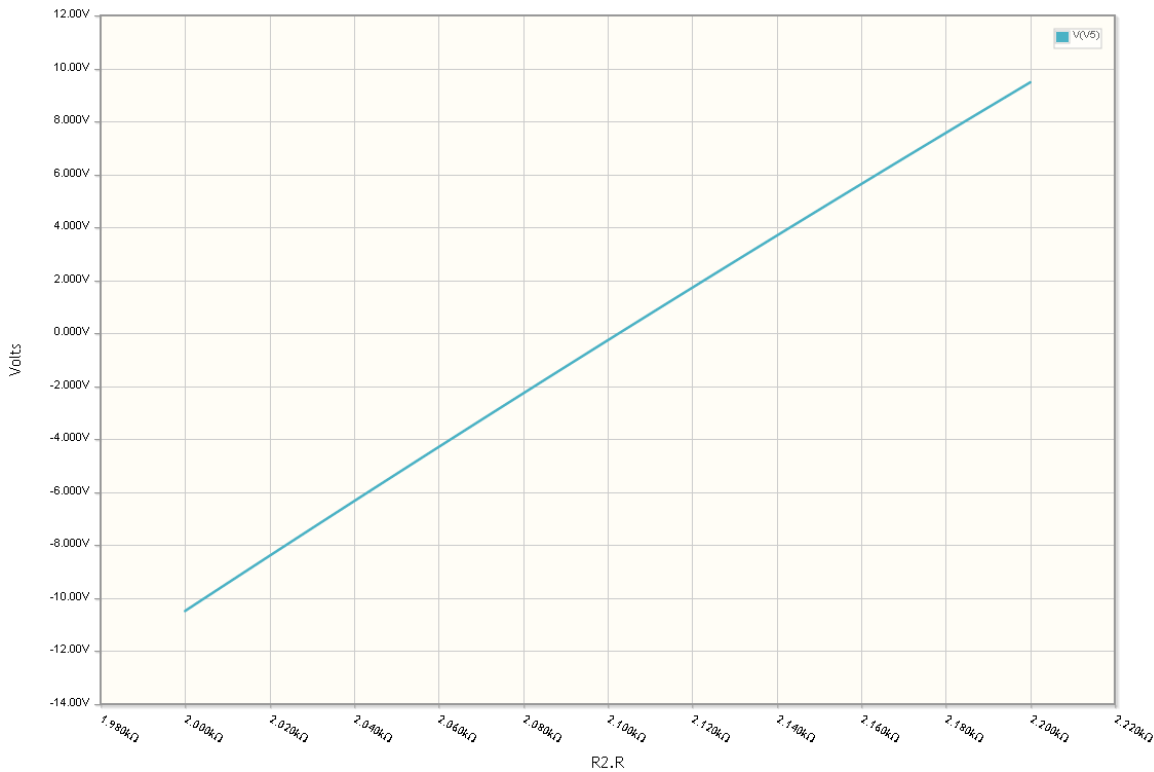


Instrumentation Amplifier: Y goes from -10V to +10V as R goes from 2000 to 2200 Ohms

In CircuitLab you can check by doing a DC Sweep on R2



This results in the output voltage shown below. Note that the range isn't *quite* 0V to 10V. This is due to the loading of R5 and R6 on V1 (the larger R5 and R6 are, the less the loading).



Output voltage as R sweeps from 2000 to 2200 Ohms

### Case 3: RTD Temperature Sensor.

The temperature-resistance relationship of an RTD is

$$R = 1000 \cdot (1 + 0.0043T) \Omega$$

where T is the temperature in degrees celsius. Design a circuit which outputs

- 0V at 0C
- +10V at +100C

Solution: Assume a voltage divider with a 1000 Ohm resistor.

At 0C

- R = 1000 Ohms
- $V_a = 5.00$  V
- $V_y = 0.00$  V

At +100C

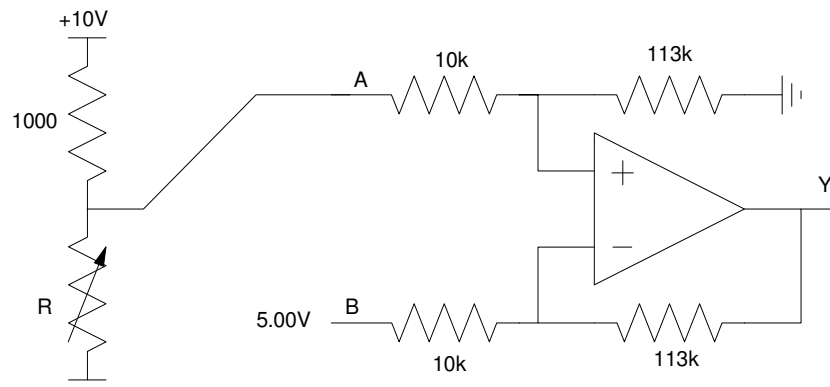
- R = 1430 Ohms
- $V_a = 5.885$  V
- $V_y = +10.00$  V

As the input voltage increases, the output voltage increases. Connect the voltage divider to A.

The output is 0V when  $V_a = 5.00$  V. Make B = 5.00V

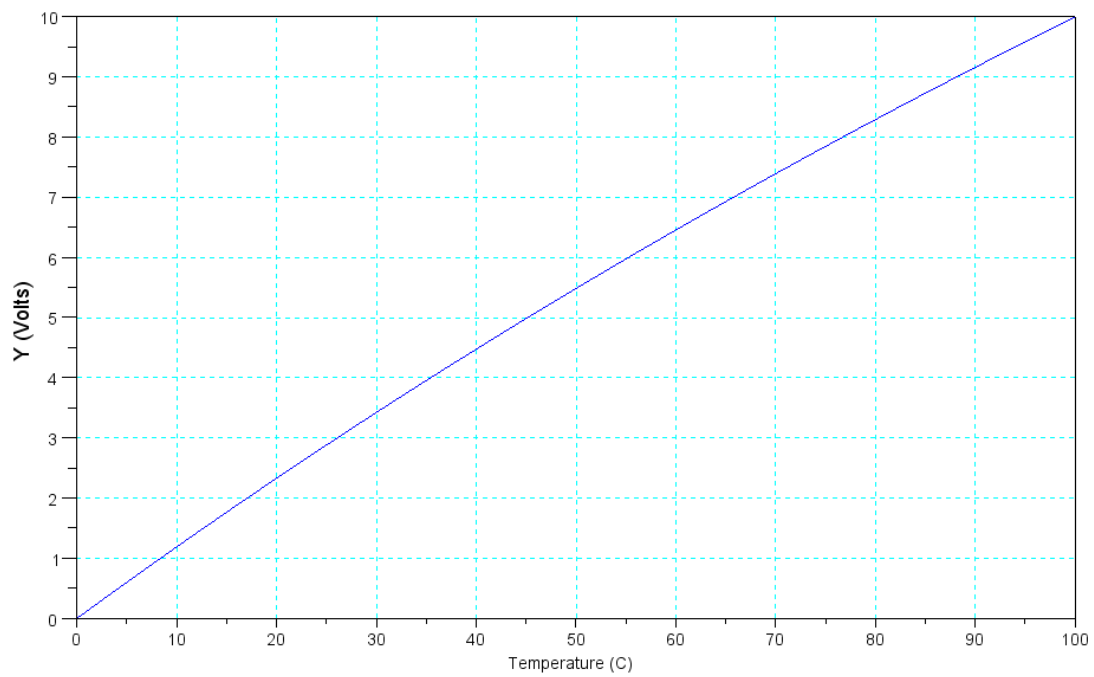
The gain needed is

$$gain = \left( \frac{\text{change in output}}{\text{change in input}} \right) = \left( \frac{10V-0V}{5.885V-5.00V} \right) = 11.30$$



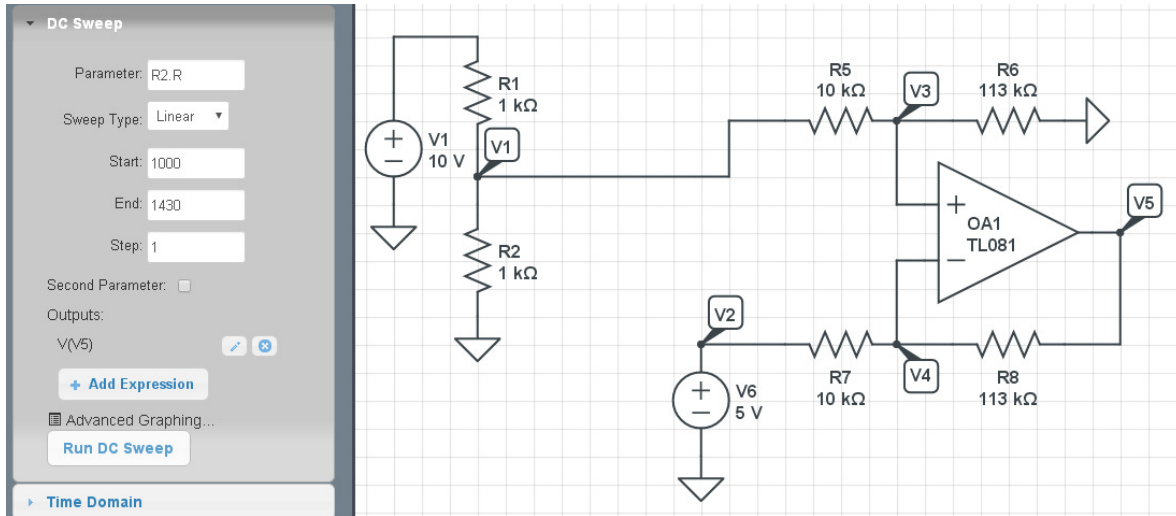
Checking the results in Matlab:

```
T = [0:0.1:100]';  
R = 1000 * (1 + 0.0043*T);  
Va = R ./ (1000 + R) * 10;  
Y = 11.3 * (Va - 5.00);  
  
plot(T,Y);  
  
xlabel('Temperature (C)');  
ylabel('Y (Volts)');
```

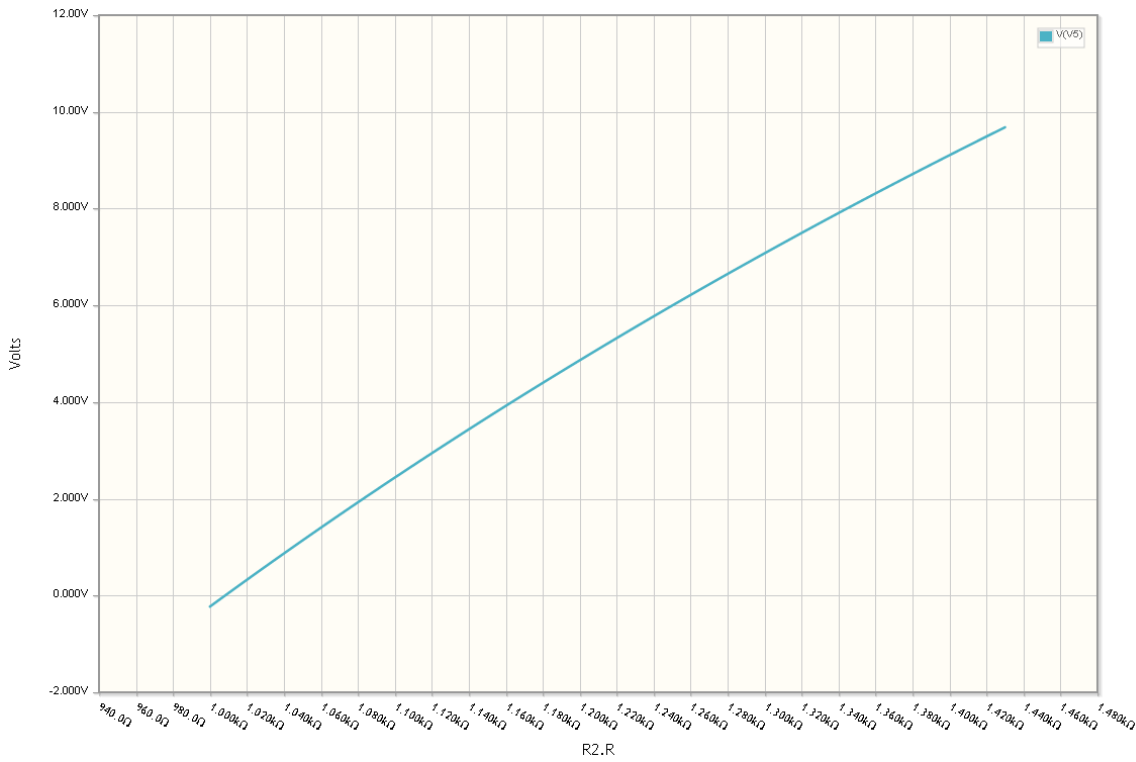


Checking the results in CircuitLab, note that

- The output voltage is slightly off
- This is due to the loading of R5 and R6 on V1



A DC Sweep us run with R2 varying frm 1000 to 1430 Ohms ( 0C < T < 100C )



Resulting Output Voltage as R varies from 1000 to 1430 Ohms

### Case 4: Thermistor Temperature Sensor.

The temperature-resistance relationship of a thermistor is

$$R \approx 1000 \exp\left(\frac{3905}{T+273} - \frac{3905}{298}\right) \Omega$$

where T is the temperature in degrees celsius. Design a circuit which outputs

- 0V at 0C
- +10V at +40C

Solution: Assume a voltage divider with a 1000 Ohm resistor.

At 0C

- $R = 3320.125$  Ohms
- $V_b = 7.6853$  V
- $V_y = 0.00$ V

At +40C

- $R = 533.664$  Ohms
- $V_b = 3.4797$ V
- $V_y = +10.00$ V

As the input voltage decreases, the output voltage increases. Connect the voltage divider to B.

The output is 0V when  $V_a = 7.6853$ V. Make  $A = 7.6853$ V

The gain needed is

$$gain = \left(\frac{10V-0V}{3.4797V-7.6853V}\right) = -2.3778$$

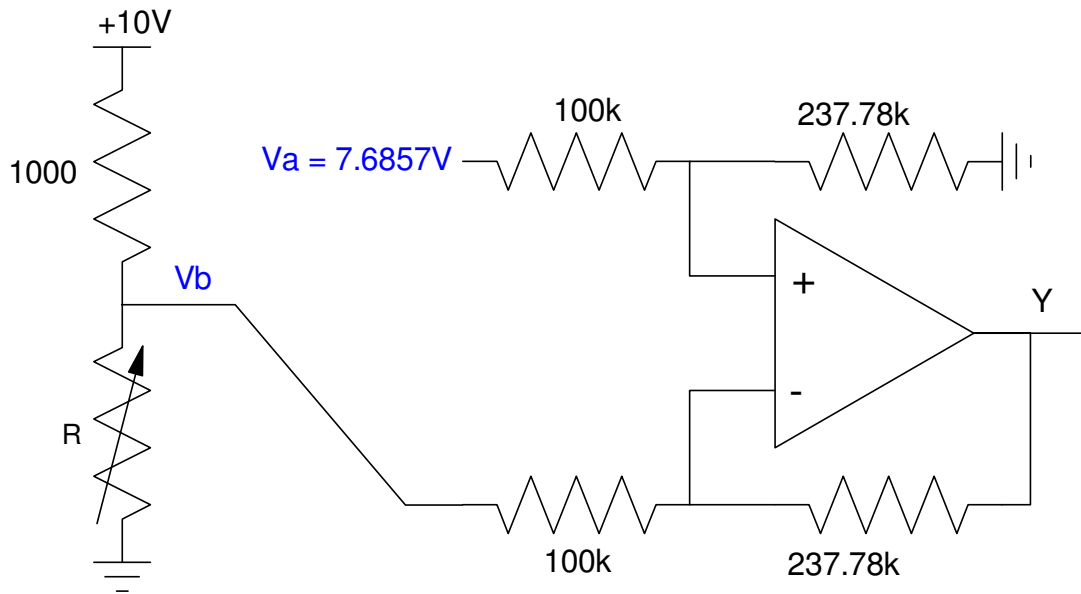
The minus sign is taken care of by connecting to the minus input (B).

The gain comes from the resistor ratio

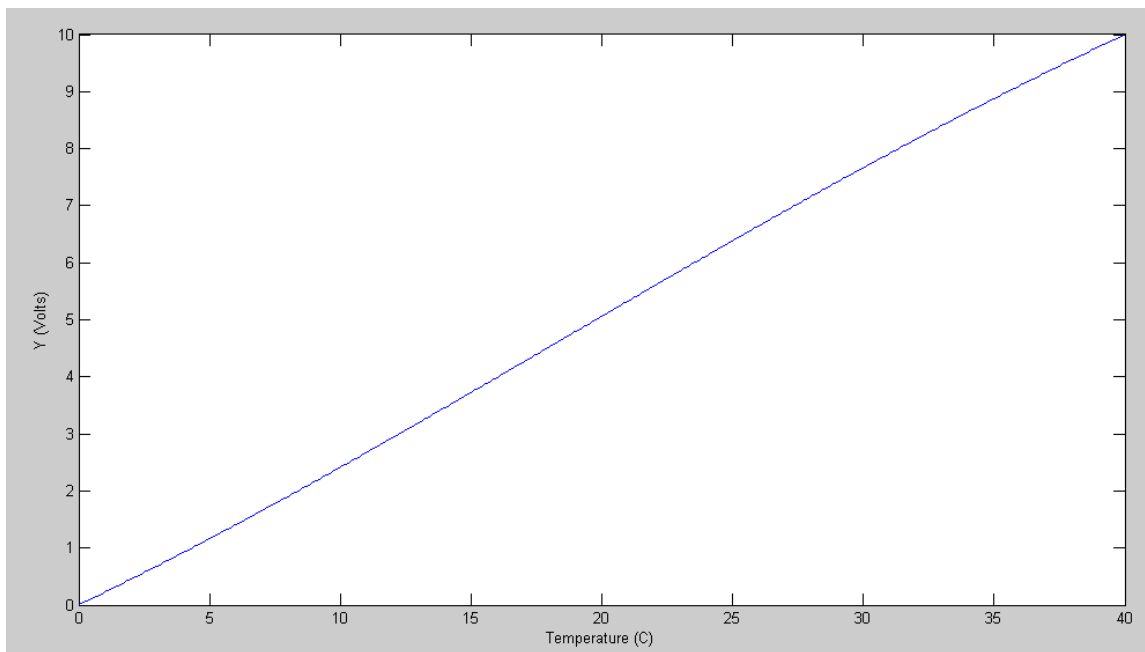
$$\text{Let } R_1 = 100k, R_2 = 237.78k$$

Note: You can check your results in Matlab.

```
T = [0:0.1:40]';
R = 1000 * exp( 3905 ./ (T + 273) - 3905/298 );
Va = R ./ (1000 + R) * 10;
Y = 2.3778 * (7.6853 - Va);
plot(T,Y);
xlabel('Temperature (C)');
ylabel('Y (Volts)');
```



Instrumentation Amplifier to output 0V @ 0C, 10V @ 40C



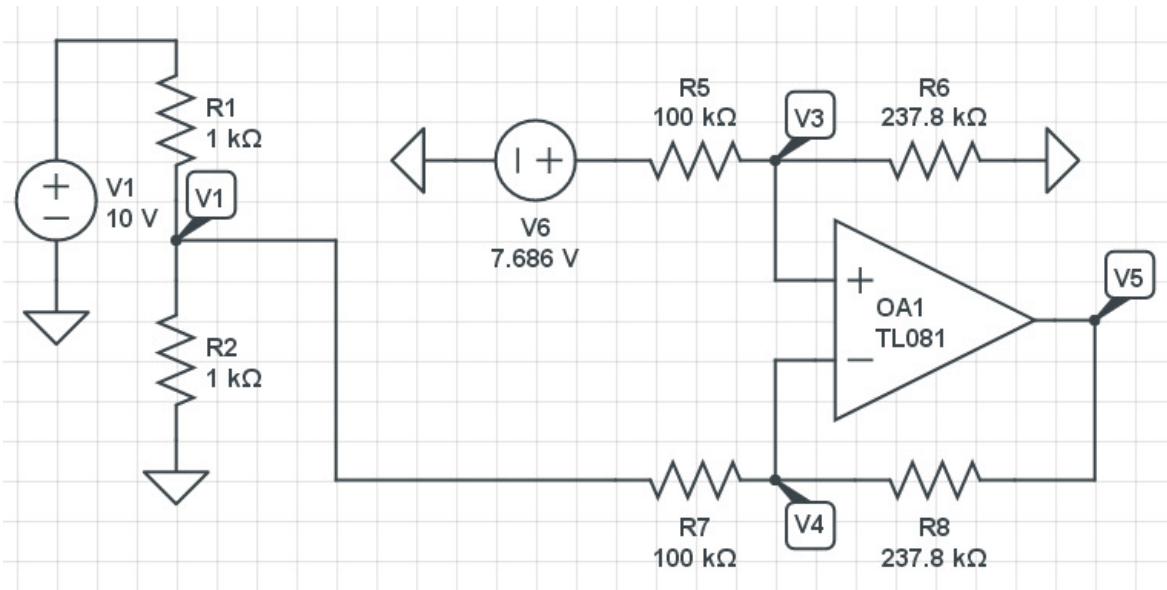
Output Voltages vs. Temperature

Note that the output goes from 0V to 10V as temperature goes from 0C to +40C as desired.



In CircuitLab, check

- The left endpoint (0C or  $R_2 = 3320.125 \text{ Ohms}$ )
- The midpoint (20C or  $R_2 = 1250.593 \text{ Ohms}$ )
- The right endpoint (40C or  $R_2 = 533.664 \text{ Ohms}$ )



V(V1)	7.688 V	<input type="text"/>	<input type="text"/>
V(V3)	5.410 V	<input type="text"/>	<input type="text"/>
V(V4)	5.410 V	<input type="text"/>	<input type="text"/>
V(V5)	42.32 mV	<input type="text"/>	<input type="text"/>

Output (V5) at 0C = 0.04232V (0V ideally)

V(V1)	5.556 V	<input type="text"/>	<input type="text"/>
V(V3)	5.410 V	<input type="text"/>	<input type="text"/>
V(V4)	5.410 V	<input type="text"/>	<input type="text"/>
V(V5)	5.064 V	<input type="text"/>	<input type="text"/>

Output (V5) at +20C = 5.064V (5.000V ideally)

V(V1)	3.486 V	<input type="text"/>	<input type="text"/>
V(V3)	5.410 V	<input type="text"/>	<input type="text"/>
V(V4)	5.410 V	<input type="text"/>	<input type="text"/>
V(V5)	9.985 V	<input type="text"/>	<input type="text"/>

Output (V5) at +40C = 9.985V (10.000V ideally)