

ECE 320 - Homework #1

Matlab, PartSim, Solving $f(x) = 0$. Due Monday, August 29th

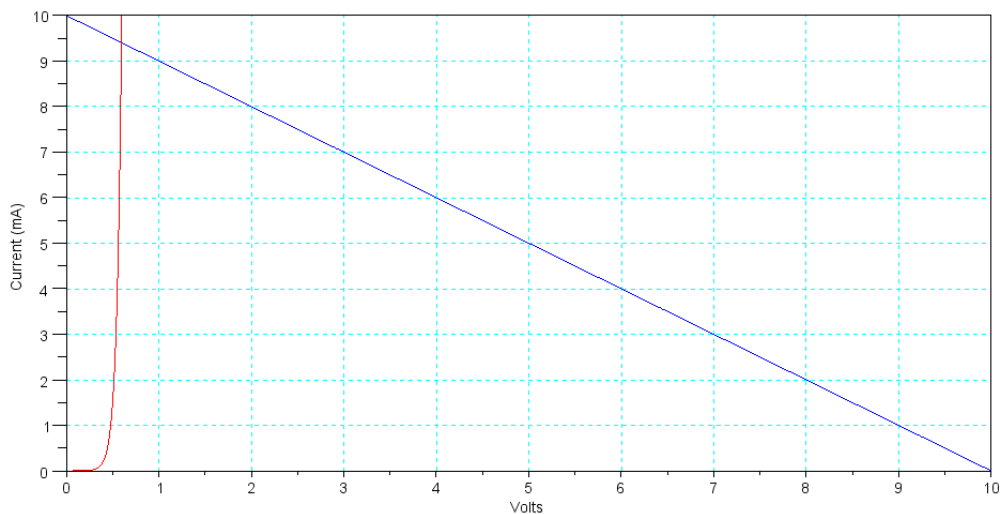
1) Given 2 equations with 2 unknowns

$$V = 10 - 1000I$$

$$V = 0.052 \cdot \ln(10^7 \cdot I + 1)$$

1a) Solve in Matlab using graphical methods

```
-->I = [0:0.001:1]' * 0.01;  
-->V1 = 10 - 1000*I;  
-->V2 = 0.052*log(1e7*I + 1);  
  
-->plot(V1,I*1000,V2,I*1000);  
-->xlabel('Volts');  
-->ylabel('Current (mA)');  
-->xgrid(4)
```



Solution: (0.7V, 9.4mA)

1b) Solve numerically to find V and I

Use *fminsearch()*

First, set up a function in Matlab to compute the error

```
function [ J ] = Probl( I )  
    V1 = 10 - 1000*I;  
    V2 = 0.052*log(1e7*I + 1);  
    E = V1 - V2;  
    J = E^2;  
end
```

Now solve using *fminsearch*(*).* Start with an initial guess of 9mA

```
>> Prob1(0.009)
```

```
0.1655
```

```
>> I = fminsearch('Prob1',0.009)
```

```
I =
```

```
0.0094
```

Check that the error is zero:

```
>> Prob1(I)
```

```
1.0962e-005
```

The solution is then

```
>> V = 10 - 1000*I
```

```
0.5922
```

answer: (0.5922V, 9.4mA)

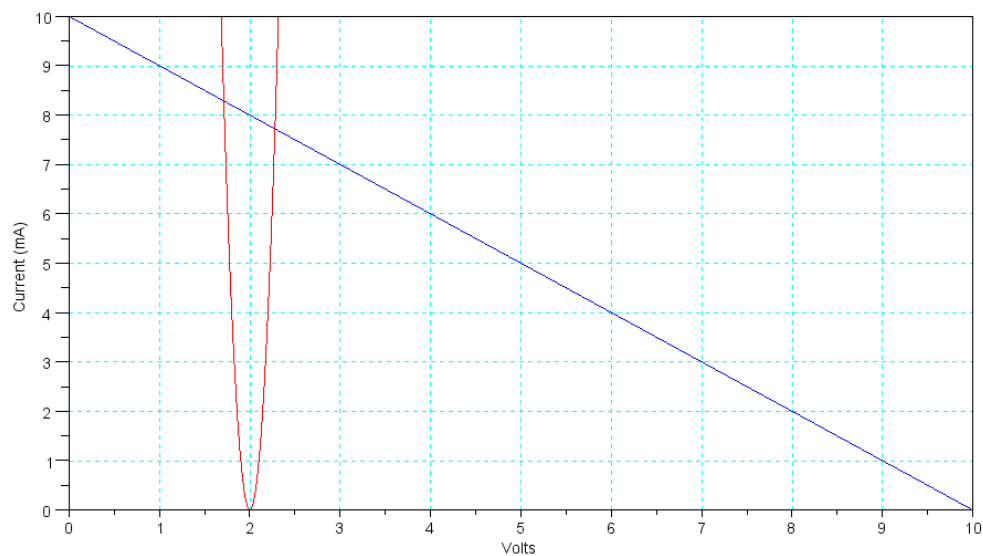
2) Given 2 equations with 2 unknowns

$$V = 10 - 1000I$$

$$I = 0.1 \cdot (V - 2)^2$$

2a) Solve in Matlab using graphical methods

```
-->V = [0:0.01:10]';  
-->I1 = (10 - V) / 1000;  
-->I2 = 0.1* ( (V - 2) .^ 2 );  
  
-->plot(V,I1*1000,V,I2*1000)  
-->xgrid(4);  
-->xlabel('Volts');  
-->ylabel('Current (mA)');
```



Solution: (2.2V, 7.7mA) and (1.8V, 8.2mA)

2b) Solve numerically to find V and I

First, set up a cost function in Matlab:

```
function [ J ] = Prob2( V )  
  
    I1 = (10 - V) / 1000;  
    I2 = 0.1* ( (V - 2) .^ 2 );  
  
    E = I1 - I2;  
  
    J = E^2;  
  
end
```

Solve using *fminsearch()*

Start with a guess close to the right solution:

```
>> V = fminsearch('Prob2',2.2)
    2.2779
>> Prob2(V)
    1.1692e-013
>> I = (10 - V) / 1000
    0.0077
```

One solution is: **(2.2779V, 7.7mA)**

Now find the solution close to the left solution:

```
>> V = fminsearch('Prob2',1.8)
    1.7121
>> Prob2(V)
    4.4340e-014
>> I = (10 - V) / 1000
    0.0083
```

The other solution is **(1.7121V, 8.3mA)**

3) Solve using *fminsearch()* in Matlab

$$\left(\frac{V_1-10}{100}\right) + \left(\frac{V_1-V_2}{200}\right) + \left(\frac{V_1}{300}\right) + I_{d1} = 0$$

$$I_{d1} + \left(\frac{V_1-V_2}{200}\right) = I_{d2}$$

$$I_{d1} = 10^{-7} \cdot (e^{20(V_1-V_2)} - 1)$$

$$I_{d2} = 10^{-7} \cdot (e^{20V_2} - 1)$$

Create a cost function in Matlab:

```
function [ J ] = Prob3( Z )

V1 = Z(1);
V2 = Z(2);
I1 = Z(3);
I2 = Z(4);

E1 = (V1-10)/100 + (V1-V2)/200 + (V1/300) + I1;
E2 = I1 + (V1-V2)/200 - I2;
E3 = I1 - 1e-7*(exp(20*(V1-V2))-1);
E4 = I2 - 1e-7*(exp(20*V2)-1);

J = E1^2 + E2^2 + E3^2 + E4^2;

end
```

Solve using *fminsearch()*. Use problem #4 as a starting guess:

```
>> Z = fminsearch('Prob3',[1.4,0.7,0.01,0.01])
```

V1	V2	I1	I2
1.3594	0.6807	0.0784	0.0818

Check the error:

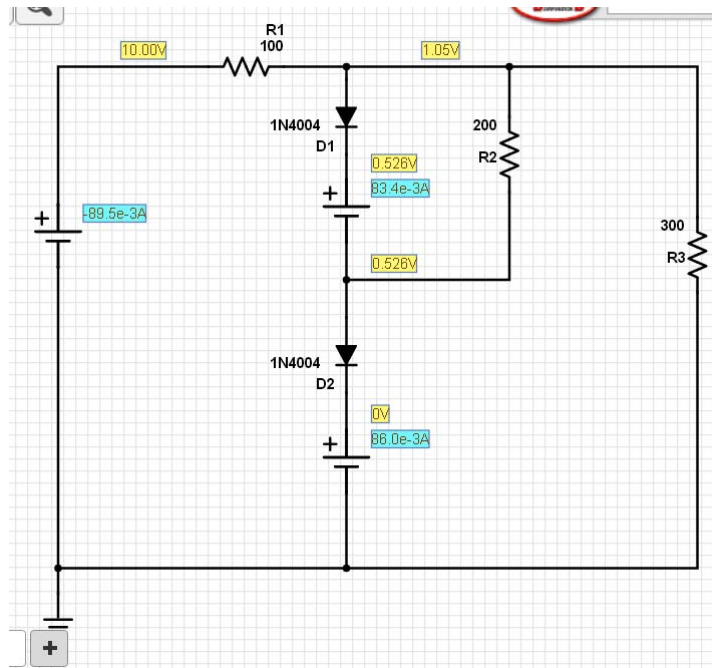
```
>> Prob3(Z)
```

```
2.8525e-009
```

Close to zero, so the solution above is almost correct.

4) Input this circuit into PartSim to solve for the node voltages

This took a little effort to get it to show the currents. Adding a 0V source in series with the diodes seemed to work:



The net results is

$$V1 = 1.05V$$

$$V2 = 0.526V$$

$$Id1 = 83.4mA$$

$$Id2 = 86.0mA$$