## ECE 320 - Homework \#4

AC to DC Converters, Min/Max Circuits, Clipper Circuits. Due Monday, February 5th, 2018

## AC to DC Converters

1) (Analysis) For the following half-wave rectifier, determine the voltage atV1 and V2


V1:
$\max (\mathrm{V} 1)=19.3 \mathrm{~V}$
20 V peak -0.7 V across the diode
The current is approximately

$$
I \approx \frac{19.3 \mathrm{~V}}{1 \mathrm{k} \Omega+270}=15.2 \mathrm{~mA}
$$

The ripple is then

$$
\begin{aligned}
& I=C \frac{d V}{d t} \\
& 15.2 m A=100 \mu F \cdot \frac{d V}{1 / 60 \mathrm{~s}} \\
& d V=2.53 V_{p p}
\end{aligned}
$$

The average voltage at V 1 is then approximately the average of the max and min

$$
\begin{aligned}
& \max \left(V_{1}\right)=19.3 V \\
& \min \left(V_{1}\right)=19.3 V-2.53 V=16.78 V \\
& V_{1: D C}=\left(\frac{\max \left(V_{1}\right)+\min \left(V_{1}\right)}{2}\right)=18.03 \mathrm{~V}
\end{aligned}
$$

V2: DC Analysis:

$$
V_{2}=\left(\frac{1000}{1000+270}\right) V_{1}
$$

$$
\begin{aligned}
& V_{2}=\left(\frac{1000}{1000+270}\right) 18.03 \mathrm{~V} \\
& V_{2}=14.20 \mathrm{~V}
\end{aligned}
$$

AC Analysis

$$
\begin{aligned}
& \omega=2 \pi \cdot 60 \mathrm{~Hz}=3777 \mathrm{rad} \\
& L \rightarrow j \omega L=j 3770 \Omega \\
& V_{2}=\left(\frac{1000}{1000+3770+270}\right) \cdot 2.53 V_{p p} \\
& V_{2}=0.636 V_{p p} \quad \text { (angle doens't matter here) }
\end{aligned}
$$

|  | DC | AC $(60 \mathrm{~Hz})$ |
| :---: | :---: | :---: |
| $\mathrm{V} 1(\mathrm{t})$ | 18.03 V | 2.53 Vpp |
| $\mathrm{V} 2(\mathrm{t})$ | 14.20 V | 0.636 Vpp |

2) (Simulation) Simulate this circuit in PartSim to verify your calculations.


Zooming in on V1 and V2 after 3 cycles


|  | V1 (black) |  | V2 (green) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Calculated | Simulated | Calculated | Simulated |
| DC (Vavg) | 18.03 | 18.2 | 14.2 | 14.29 |
| AC (Vpp) | 2.53 Vpp | 2.17 Vpp | 0.636 Vpp | 0.418 Vpp |

3) (Validation) Build this circuit in lab to verify your simulations and calculations
4) Design a half-wave rectifier (i.e. specify R, L, C) to meet the following requirements:

Input: Wall transformer

- $20 \mathrm{Vp}, 60 \mathrm{~Hz}$, capable of 500 mA

Output: A load which draws 100 mA
Relationship:

- The ripple at V1 (across the capacitor) is 1 Vpp when the load draws 100 mA
- The ripple at V2 (across the load) is 0.1 Vpp when the load draws 100 mA

DC Voltage at V1

$$
\begin{aligned}
& \max (\mathrm{V} 1)=19.3 \mathrm{~V} \\
& \min (\mathrm{~V} 1)=18.3 \mathrm{~V} \quad(1 \mathrm{Vpp}) \\
& \operatorname{avg}(\mathrm{V} 1)=18.8 \mathrm{~V}
\end{aligned}
$$

With an ideal inductor ( $\mathrm{RL}=0$ ), this is also the DC voltage at V 2

R (Load)

$$
R=\frac{18.8 \mathrm{~V}}{100 \mathrm{~mA}}=188 \Omega
$$

C:

$$
I=C \frac{d V}{d t}
$$

$$
100 m A=C \frac{1 V_{p p}}{1 / 60 s}
$$


$C=1,667 \mu F$

L:
The ripple at V2 is 10x smaller than the ripple at V1

$$
|j \omega L| \approx 10 R
$$

$$
\omega L=1880
$$

$$
L=\frac{1880}{377}=4.98 H
$$

5) Check your design for problem \#4 with a simulation using PartSim (or similar program)


Let the simulation run for 20 cycles to reach stedy-state


Zoom in on the last three cycles


|  | V1 (blue) |  | V2 (black) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Calculated | Simulated | Calculated | Simulated |
| DC (Vavg) | 18.8 | 18.68 | 18.8 V | 18.65 V |
| AC (Vpp) | 1.00 Vpp | 0.914 Vpp | 100 mVpp | 64 mVpp |

## Min/Max Circuits

Assume ideal silicon diodes.
6) Determine the voltages for the following max $/ \mathrm{min}$ circuit with $\mathrm{R} 2=10 \mathrm{k}$
7) What logic function does this circuit implement?

$$
\begin{aligned}
& \mathrm{Y}=\mathrm{f}(\mathrm{~A}, \mathrm{~B}, \mathrm{C}, \mathrm{D}) \\
& \mathrm{Y}=\max (\min (\mathrm{A}, \mathrm{~B}), \min (\mathrm{C}, \mathrm{D})) \\
& \mathrm{Y}=\mathrm{AB}+\mathrm{CD}
\end{aligned}
$$



## Clipper Circuits

8) Design a clipper circuit which can drive a 100 k Ohm load to approximate the following function


Region 1: Slope $=1.5$
Add an amplifier with a gain of 1.5
Add a 1 k resistor at the output so that you can drive a 1 M load

Region 2: Slope $=0.68$

$$
\begin{aligned}
& \left(\frac{R_{1}}{R_{1}+1000}\right) \cdot 1.5=0.68 \\
& \left(\frac{R_{1}}{R_{1}+1000}\right)=0.453 \\
& R_{1}=\left(\frac{0.453}{1-0.453}\right) \cdot 1000=829 \Omega
\end{aligned}
$$

Turn on voltage is when $\mathrm{Y}=1.5 \mathrm{~V}$

$$
\mathrm{Vz1}=1.5 \mathrm{~V}
$$

Region 3: Slope $=0.37$

$$
\begin{aligned}
& \left(\frac{R_{12}}{R_{12}+1000}\right) \cdot 1.5=0.37 \\
& \left(\frac{R_{12}}{R_{12}+1000}\right)=0.246 \\
& R_{12}=\left(\frac{0.246}{1-0.246}\right) \cdot 1000=327 \Omega
\end{aligned}
$$

$$
\begin{aligned}
& R_{12}=R_{1} \| R_{2}=327 \Omega \\
& R_{2}=541 \Omega
\end{aligned}
$$

Turn on voltage is when $\mathrm{Y}=3.0 \mathrm{~V}$

$$
\mathrm{Vz2}=3.0 \mathrm{~V}
$$

Region 3: slope $=0.18$

$$
\begin{aligned}
& \left(\frac{R_{123}}{R_{123}+1000}\right) \cdot 1.5=0.18 \\
& \left(\frac{R_{123}}{R_{123}+1000}\right)=0.12 \\
& R_{123}=\left(\frac{0.12}{1-0.12}\right) \cdot 1000=136 \Omega \\
& R_{123}=R_{1}\left\|R_{2}\right\| R_{3} \\
& R_{3}=234 \Omega
\end{aligned}
$$

Turn on voltage for region 3 is when $\mathrm{Y}=4.2 \mathrm{~V}$

$$
\mathrm{Vz3}=4.2 \mathrm{~V}
$$

Net Design:


