## ECE 320 - Homework \#3

Ideal Diodes, LEDs, AC to DC Converters. Due Monday, January 31st

## Ideal Diodes:

1) Assume ideal sililcon diodes $(\mathrm{Vf}=0.7 \mathrm{~V})$. Determine the voltages and currents for the following circuit


The diode is probably on (more than 0.7 V is applied), meaning

$$
\begin{aligned}
& V_{d}=0.7 \mathrm{~V} \\
& I_{d}=\left(\frac{5 V-0.7 \mathrm{~V}}{50 \Omega}\right)=86.0 \mathrm{~mA}
\end{aligned}
$$

Note

- The results are close to what we found in homework \#2, but
- Ideal diode model is much easier to use

|  | Vd | Id |
| :---: | :---: | :---: |
| HW3: Ideal Diode | 700 mV | 86.00 mA |
| HW2) Graphical solution | 800 mV | 85 mA |
| HW2) Numeric Solution | 821.1 mV | 83.58 mA |
| HW2) Simulation (CircuitLab) | 779.1 mV | 84.42 mA |
| HW2) Lab (experimental) | 757 mV | 83.20 mA |

2) Assume ideal silicon diodes $(\mathrm{Vf}=0.7 \mathrm{~V})$. Determine the voltages and currents for the following circuit

- R1, R2, R3 are the same that you used in homework \#2


There are eight permutations of on \& off. Assume

- D1, D3 are on
- D2 is off
this gives

$$
\begin{aligned}
& V_{0}=5 \mathrm{~V} \\
& V_{1}=V_{0}-0.7 \mathrm{~V}=4.3 \mathrm{~V} \\
& V_{2}=V_{1}-0.7 \mathrm{~V}=3.6 \mathrm{~V} \\
& V_{3}=0.7 \mathrm{~V}
\end{aligned}
$$

Comparing to homework \#1

- The ideal diode model is close but a little off

|  | V 0 | V 1 | V 2 | V 3 |
| :---: | :---: | :---: | :---: | :---: |
| Ideal Diode | 5.00 V | 4.30 V | 3.60 V | 700 mV |
| Numeric Solution | 5.00 V | 4.1955 V | 3.4172 V | 801.8 mV |
| Simulation (CircuitLab) | 5.00 V | 4.229 V | 3.494 V | 758.5 mV |
| Lab (experimental) | 4.92 V | 4.14 V | 3.40 V | 755 mV |

## LEDs

The specifications for a Piranah RGB LED are

| Color | Vf @ 20mA | mcd @ 20mA |
| :---: | :---: | :---: |
| red | 2.0 V | 10,000 |
| green | 3.2 V | 10,000 |
| blue | 3.2 V | 10,000 |

3) Design a circuit to drive these LEDs with a 5 V source to produce olive green:

- $\operatorname{Red}=6901 \mathrm{mcd}(176 / 255)$
- $\quad$ Green $=7686 \mathrm{mcd}(196 / 255)$
- Blue $=2313 \mathrm{mcd}(59 / 255)$

Current is proportional to brightness

$$
\begin{aligned}
& I_{r}=\left(\frac{6901 \mathrm{mcd}}{10,000 \mathrm{mcd}}\right) 20 \mathrm{~mA}=13.802 \mathrm{~mA} \\
& R_{r}=\left(\frac{5 \mathrm{~V}-2.0 \mathrm{~V}}{13.802 \mathrm{~mA}}\right)=311.5 \Omega \\
& I_{g}=\left(\frac{7686 \mathrm{mcd}}{10,000 \mathrm{mcd}}\right) 20 \mathrm{~mA}=15.372 \mathrm{~mA} \\
& R_{g}=\left(\frac{5 \mathrm{~V}-3.2 \mathrm{~V}}{15.372 \mathrm{~mA}}\right)=117.1 \Omega \\
& I_{b}=\left(\frac{2313 \mathrm{mcd}}{10,000 \mathrm{mcd}}\right) 20 \mathrm{~mA}=4.626 \mathrm{~mA} \\
& R_{b}=\left(\frac{5 \mathrm{~V}-3.2 \mathrm{~V}}{4.626 \mathrm{~mA}}\right)=389.1 \Omega
\end{aligned}
$$


4) Design a circuit to drive these LEDs with a 5 V source producing salmon pink:

- $\operatorname{Red}=6666 \operatorname{mcd}(170 / 255)$
- Green $=3333$ mcd $(85 / 255)$
- $\quad$ Blue $=5490$ mcd $(140 / 255)$

$$
\begin{aligned}
& I_{r}=\left(\frac{6666 m c d}{10,000 \mathrm{mcd}}\right) 20 \mathrm{~mA}=13.333 \mathrm{~mA} \\
& R_{r}=\left(\frac{5 \mathrm{~V}-2.0 \mathrm{~V}}{13.333 \mathrm{~mA}}\right)=225.0 \Omega \\
& I_{g}=\left(\frac{3333 \mathrm{mcd}}{10,000 \mathrm{mcd}}\right) 20 \mathrm{~mA}=6.667 \mathrm{~mA} \\
& R_{g}=\left(\frac{5 \mathrm{~V}-3.2 \mathrm{~V}}{6.667 \mathrm{~mA}}\right)=270.0 \Omega \\
& I_{b}=\left(\frac{5490 \mathrm{mcd}}{10,000 \mathrm{mcd}}\right) 20 \mathrm{~mA}=10.98 \mathrm{~mA} \\
& R_{b}=\left(\frac{5 V-3.2 \mathrm{~V}}{10.980 \mathrm{~mA}}\right)=163.9 \Omega
\end{aligned}
$$

Other colors can be obtained from
https://www.rapidtables.com/web/color/color-wheel.html


## AC to DC Converters

For the circuit below:
5) Determine the votlages at V1 and V2 (DC and AC)


V1:

$$
\begin{aligned}
& \max (\mathrm{V} 1)=19.3 \mathrm{~V} \\
& I \approx\left(\frac{19.3 V}{80 \Omega+15 \Omega}\right)=203.2 m A \quad \text { worst case } \\
& I=C \frac{d V}{d t} \\
& 203.2 m A=2000 \mu F \cdot\left(\frac{d V}{1 / 60 s}\right) \\
& d V=1.6930 \mathrm{~V} \\
& V_{1}(A C)=1.6930 V_{p p} \\
& V_{1}(D C)=19.3 \mathrm{~V}-\frac{1}{2} V_{1 p p}=18.45 \mathrm{~V}
\end{aligned}
$$

V2:

$$
\begin{aligned}
& V_{2}(D C)=\left(\frac{80 \Omega}{80 \Omega+15 \Omega}\right) \cdot V_{1}(D C) \\
& V_{2}(D C)=15.5398 V \\
& V_{2}(A C)=\left(\frac{(9.5607-\mathrm{j} 25.9509)}{(9.5607-j 25.9509)+(15+j 169.6460)}\right) \cdot V_{1}(A C) \\
& \left|V_{2}(A C)\right|=0.3232 V_{p p}
\end{aligned}
$$

6) Build the circuit in CircuitLab (or similar program) and verify your calculations for problem \#5

From CiruitLab

- $\max (\mathrm{V} 1)=19.11 \mathrm{~V}$
- $\min (\mathrm{V} 1)=17.62 \mathrm{~V}$
- $\quad \max (\mathrm{V} 2)=15.56 \mathrm{~V}$
- $\min (\mathrm{V} 2)=15.37 \mathrm{~V}$
$\mathrm{DC}=(\max +\min ) / 2$
$\mathrm{AC}=(\max -\min ) \mathrm{Vpp}$

|  | V1 |  | V 2 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | DC | AC | DC | AC |
| Calculated | 18.45 V | 1.693 Vpp | 15.5398 V | 0.3232 Vpp |
| Simulated | 18.365 V | 1.490 Vpp | $15,465 \mathrm{~V}$ | 0.190 Vpp |





Problem 6: CircuitLab Simulation
7) Determine C 1 and C 2 so that AC voltages are: $\mathrm{V} 1=2 \mathrm{Vpp}$ and $\mathrm{V} 2=250 \mathrm{mVpp}$.

$$
\begin{aligned}
& V_{1}(A C)=2 V_{p p} \\
& \max (\mathrm{~V} 1)=19.3 \mathrm{~V} \\
& V_{1}(D C)=19.3 V-\frac{1}{2} V_{1}(A C) \\
& V_{1}(D C)=18.3 V \\
& I=\left(\frac{18.3 V}{80 \Omega+15 \Omega}\right)=192.6 m A \\
& I=C \frac{d V}{d t} \\
& 192.6 m A=C_{1}\left(\frac{2 V_{p p}}{1 / 60 s}\right) \\
& C_{1}=1605 \mu F
\end{aligned}
$$

Assume C2 $=0$

$$
\begin{aligned}
& V_{2}(A C)=\left(\frac{80 \Omega}{(80 \Omega)+(15+j 169.64)}\right)\left(2 V_{p p}\right) \\
& \left|V_{2}(A C)\right|=822.9 m V_{p p}
\end{aligned}
$$

For the ripple to be 250 mVpp

$$
\begin{aligned}
& \left|\frac{1}{j \omega C_{2}}\right| \approx\left(\frac{250 \mathrm{mV}}{822.9 \mathrm{mV}}\right) \cdot 80 \Omega=24.3037 \Omega \\
& C_{2}=109.1 \mu F
\end{aligned}
$$


8) Build this circuit in CircuitLab (or similar program) and verify your calculations for problem \#7

From CircuitLab

- $\quad \max (\mathrm{V} 1)=19.12 \mathrm{~V}$
- $\min (\mathrm{V} 1)=17.30 \mathrm{~V}$
- $\quad \max (\mathrm{V} 2)=15.44 \mathrm{~V}$
- $\min (\mathrm{V} 2)=15.24 \mathrm{~V}$

|  | V1 |  | V2 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | DC | AC | DC | AC |
| Calculated | 18.30 V | 2.000 Vpp | 15.41 V | 250 mVpp |
| Simulated | 18.21 V | 1.820 Vpp | 15.34 V | 200 mVpp |




