

# ECE 321 - Final - Name \_\_\_\_\_

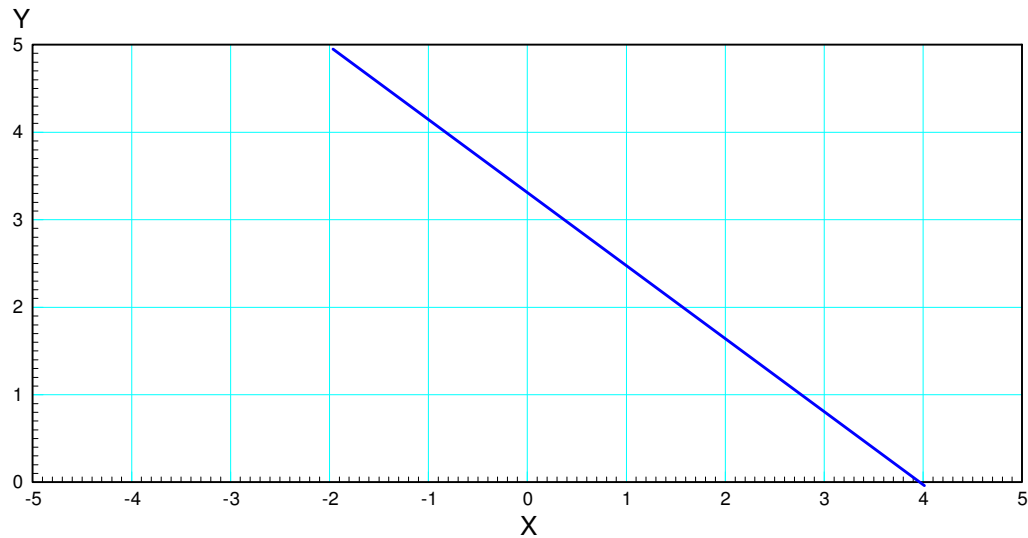
**R = 2140 ( Your Birth Month)\*1000 + (Your Birthdate)\*10**

- For example, Feb 14th would be R = 2140 Ohms.

## 1) Amplifiers

1a) Determine the equation for the line,  $Y = AX + B$

1b) Design an op-amp circuit to implement  $Y = f(X)$ . Include R in your answer somewhere (birth month & date)

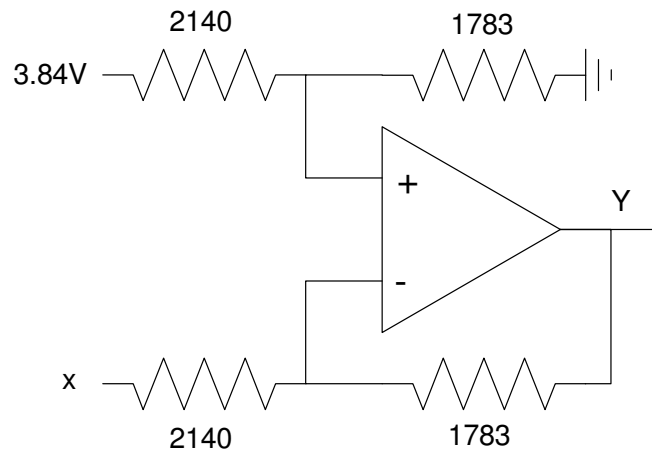


$$\text{slope} = \left( \frac{-5}{6} \right)$$

$$y = \frac{-5}{6}x + 3.2$$

Rewrite as

$$Y = \frac{5}{6}(3.84 - x)$$



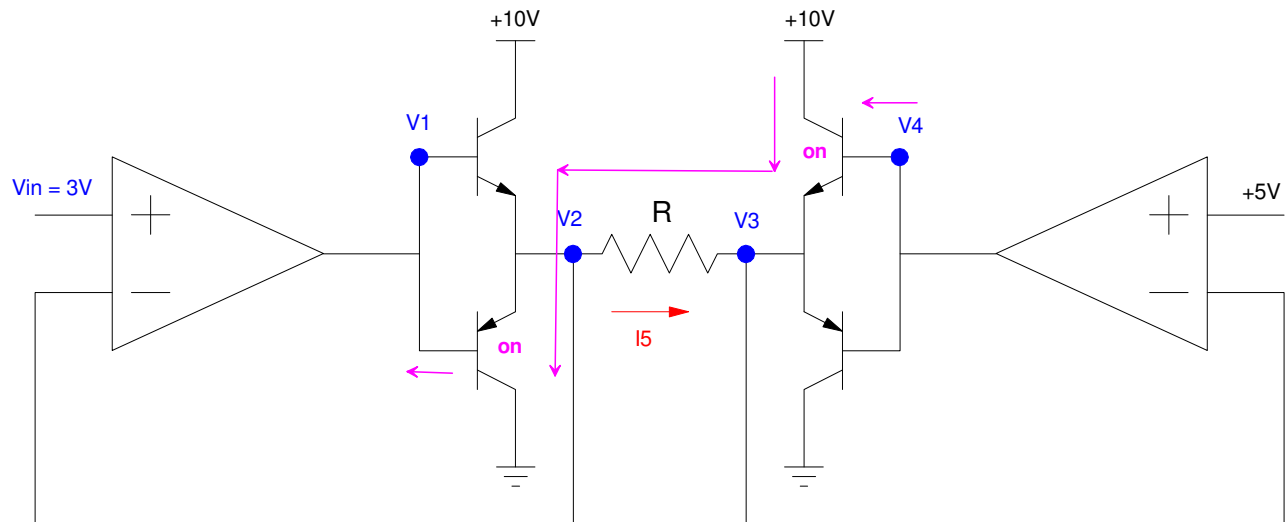
## 2) Push-Pull Amplifier

The following circuit can output -5V to +5V using only a single 10V power supply. Determine the voltages and currents when  $V_{in} = 3V$ . Assume 3904/3906 transistors

- $\beta = 200$
- $|V_{be}| = 0.7V$

R	V1	V2	V3	V4	I5
<b>2140</b>	<b>2.30V</b>	<b>3.00V</b>	<b>5.00V</b>	<b>5.70V</b>	<b>-934uA</b> 2V / 2140 Ohms

$R = \text{birth month} * 1000 + \text{birth day} * 10$ . Feb 14th = 2140 Ohms



### 3) Instrumentation Amplifier

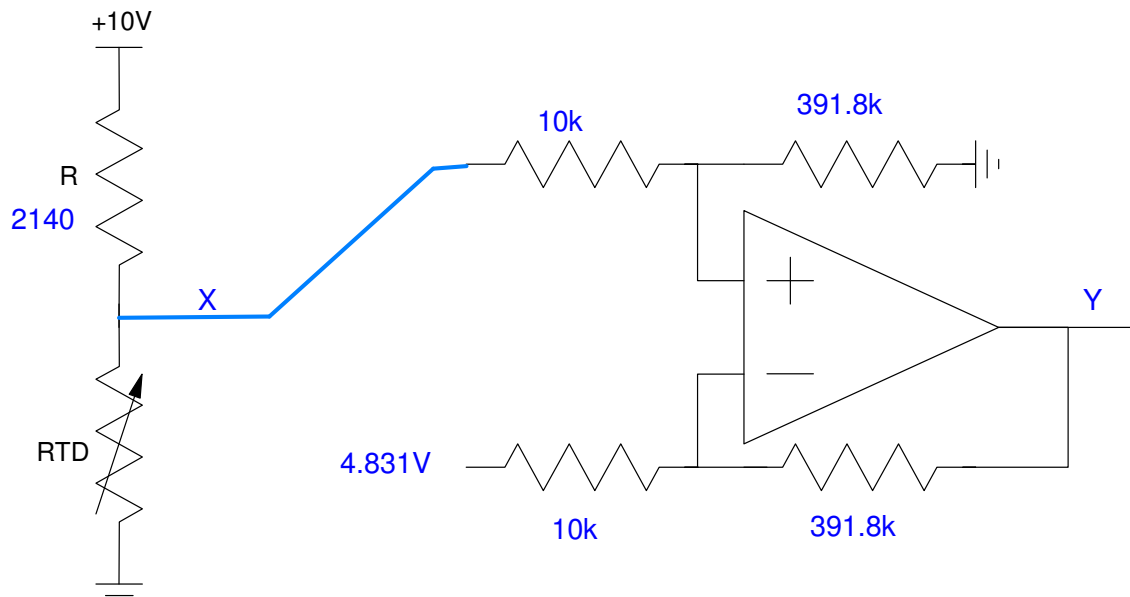
An RTD (type of temperature sensor) has a resistance - temperature relationship of

$$RTD = 2000 \cdot (1 + 0.0043T)\Omega$$

where T is the temperature in degrees C. Design a circuit which outputs

- 0V at 0C and
- 10V at +25C

Let R be your birth month \* 1000 + birth day \* 10. Feb 14th = 2140 Ohms



At 0C

- $RTD = 2000$
- $X = 4.831V$
- $Y = 0V$

At +25C

- $RTD = 2215 \text{ Ohms}$
- $X = 5.086V$
- $Y = 10V$

$$gain = \left( \frac{10V - 0V}{5.086V - 4.831V} \right) = 39.18$$

#### 4) Filter: Analysis

Assume X and Y are related by the following transfer function

$$Y = \left( \frac{500(s+2)}{(s+10)(s+30)} \right) X$$

a) What is the differential equation relating X and Y?

b) Determine y(t) assuming

$$x(t) = 5 + 2 \cos(\omega t) + 4 \sin(\omega t)$$

where  $\omega$  is your birth date (1..31)

DC:

$$s = 0$$

$$X = 5$$

$$Y = \left( \frac{500(s+2)}{(s+10)(s+30)} \right)_{s=0} \cdot (5 + j0)$$

$$Y = 16.67$$

$$y(t) = 16.67$$

AC: Feb 14th:

$$s = j14$$

$$X = 2 - j4$$

$$Y = \left( \frac{500(s+2)}{(s+10)(s+30)} \right)_{s=j14} \cdot (2 - j4)$$

$$Y = 26.879 - j48.580$$

$$y(t) = 26.879 \cos(14t) + 48.580 \sin(14t)$$

Total answer: DC + AC

$$y(t) = 16.67 + 26.879 \cos(14t) + 48.580 \sin(14t)$$

## 5) Filter: Design

Design a circuit so that the gain is

- $0.9 < \text{gain} < 1.1$  for frequencies below 10 rad/sec
- $\text{gain} < 0.3$  for frequencies above 15 rad/sec

Determine the gain of your final design at 10 and 15 rad/sec

Number of poles needed:

$$\left(\frac{10}{15}\right)^n < 0.3$$

$$n > 2.969$$

Let  $N = 4$

Assume a corner at 10 rad/sec

Assume a Chebychev filter

$$G(s) = \left( \frac{6387}{(s+7.2\angle\pm 38.5^\circ)(s+11.1\angle\pm 77.8^\circ)} \right)$$

In Matlab

```
p1 = 7.2*exp(j*38.5*pi/180);
p2 = conj(p1);
p3 = 11.1*exp(j*77.8*pi/180);
p4 = conj(p3);

G = zpk([], [-p1, -p2, -p3, -p4], abs(p1*p2*p3*p4))

-----
6387.2064
-----
(s^2 + 11.27s + 51.84) (s^2 + 4.691s + 123.2)

abs(evalfr(G, j*10))

ans =    0.995712822369479

abs(evalfr(G, j*15))

ans =    0.213292607621345
```

## 6) Filter Design

Design a circuit to implement the following filter:

$$Y = \left( \frac{10.000}{(s^2 + 10s + R)(s^2 + 20s + 2R)} \right) X$$

where R is your birth month \* 1000 + birth date \* 10. For example, Feb 14 = 2140

$$Y = \left( \frac{10.000}{(s^2 + 10s + 2140)(s^2 + 20s + 4280)} \right) X$$

$$Y = \left( \frac{10,000}{(s + 46.260 \angle \pm 83.79^\circ)(s + 65.42 \angle \pm 81.21^\circ)} \right)$$

For the first stage

$$\frac{1}{RC} = 46.260$$

$$R = 100k, C = 216nF$$

$$3 - k = 2 \cos(83.79^\circ)$$

$$k = 2.784$$

For the second stage

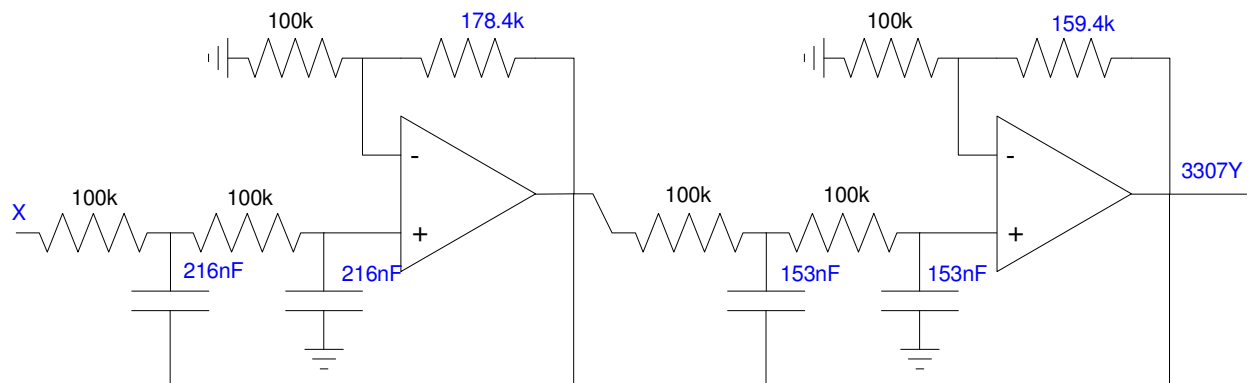
$$\frac{1}{RC} = 65.42$$

$$R = 100k, C = 153nF$$

$$3 - k = 2 \cos(81.21^\circ)$$

$$k = 2.594$$

- The DC gain should be 0.002184.
- It's actually  $k_1 * k_2 = 7.222$
- The output is  $3307 * y$



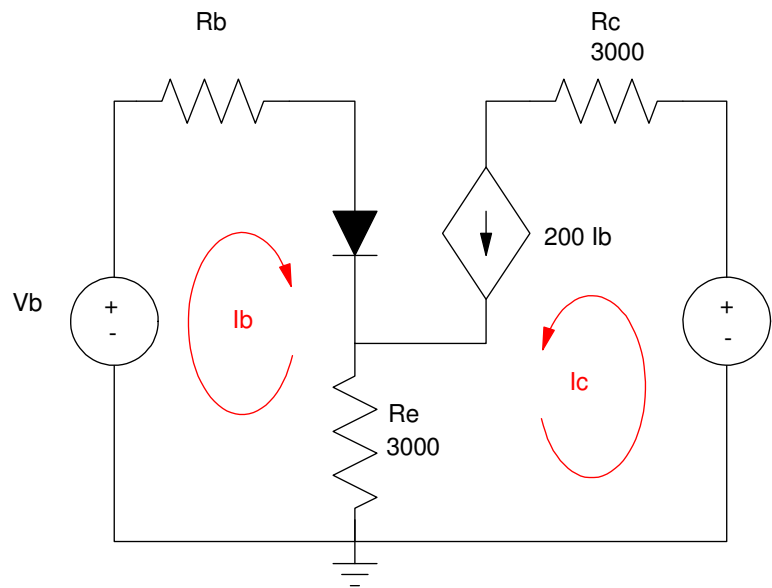
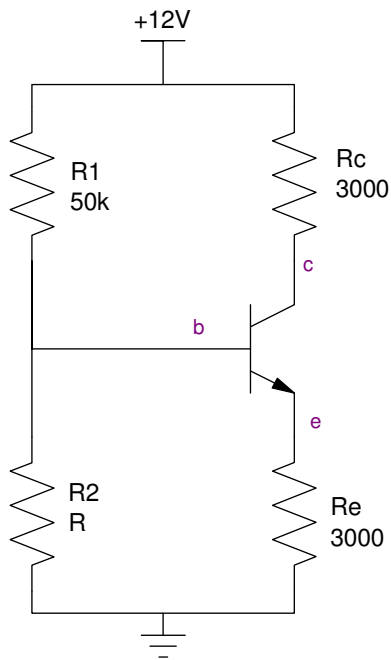
## 7) CE Amplifier (DC)

Determine the Q-point ( $V_c$ ,  $R_c$ ) for the following transistor circuit. Assume a 3904 transistor

- $\beta = 200$
- $|V_{be}| = 0.7$

R	$V_b$	$R_b$	$V_{ce}$	$I_c$
<b>7140</b>	<b>1.4811V</b>	<b>6171</b>	<b>10.4575V</b>	<b>256.4mA</b>

$R = \text{birth month} * 1000 + \text{birth day} * 10$ . For example, Feb 14th = 2140 Ohms



$$R_b = R_1 || R = 6171 \Omega$$

$$V_b = \left( \frac{R}{R+50k} \right) 12V = 1.4811V$$

$$I_b = \left( \frac{1.4811V - 0.7V}{6171 + 201(3000)} \right) = 1.2822 \mu A$$

$$I_c = 200 I_b = 256.4 mA$$

$$V_{ce} = 12 - 6000 I_c - 3000 I_b = 10.4575V$$

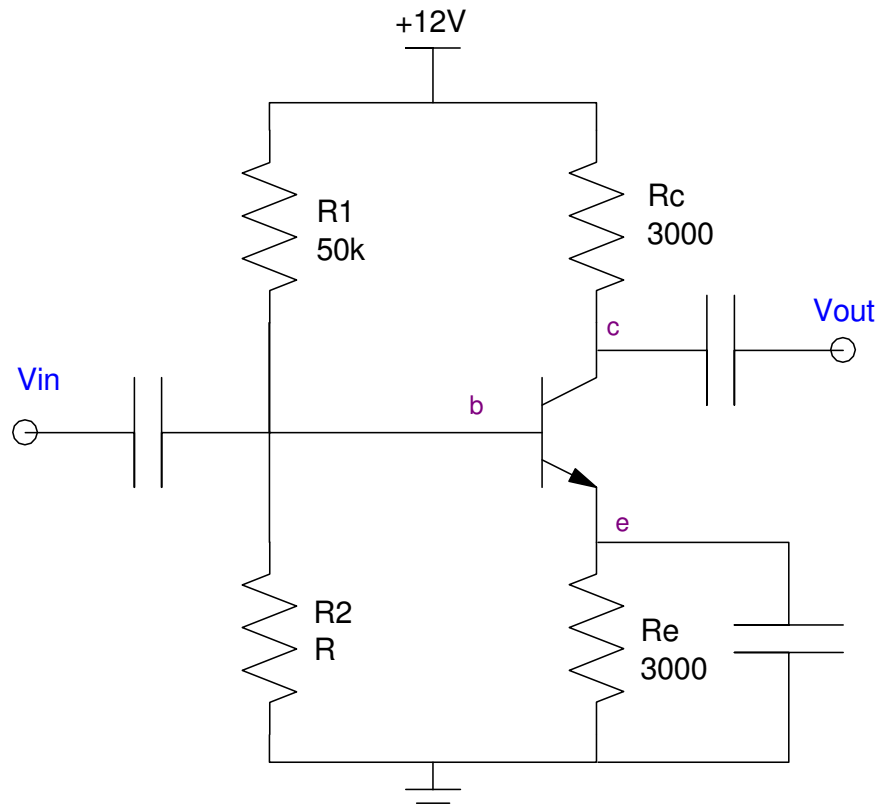
## 8) CE Amplifier (AC)

Draw the small signal model for this amplifier and the resulting 2-port model. Assume 3904 transistors

- $\beta = 200$
- $V_{be} = 0.7V$

R	R <sub>in</sub>	A <sub>i</sub>	R <sub>out</sub>	A <sub>o</sub>
<b>7140</b>	<b>5356</b>	<b>0</b>	<b>3000</b>	<b>-14.79</b>

R = birth month \* 1000 + birth day \* 10. For example, Feb 14th = 2140 Ohms



$$r_f = \frac{0.052}{I_b} = \frac{0.052}{1.2822\mu A} = 40.55k\Omega$$

$$R_{in} = 7140 || 50k || 40.55k = 5356\Omega$$

$$R_{out} = R_c = 3000$$

$$A_0 = -\frac{\beta R_c}{r_f} = -14.79$$