ECE 321 - Homework #3

Calibration, Filter Circuits, and Frequency Response. Due Monday, April 20th

Please make the subject "ECE 321 HW#3" if submitting homework electronically to Jacob_Glower@yahoo.com (or on blackboard)

Calibration

Problem 1 & 2) Assume you are using a thermistor where the temperature - resistance relationship is

$$R = 1000 \, \exp\left(\frac{3905}{T} - \frac{3905}{298}\right) \, \Omega$$

along with a voltage divider (10V source, 2k resistor:

$$V = \left(\frac{R}{R + 2000}\right) \cdot 10V$$

1) Determine a calibration function of the form

$T \approx aV + b$

to estimate temperature over the range of (0C, +30C). What is the maximum error in this calibration function?

```
T = [0:0.1:30]';
R = 1000 * exp(3905 ./ (T + 273) - 3905/298);
V = R ./ (R + 2000) * 10;
B = [V, V.^0];
A = inv(B'*B)*B'*T
- 8.7698745
54.106726
max(T - B*A)
ans = 1.0738336 maximum error on the high side
min(T - B*A)
ans = - 0.4660400 maximum error on the low side
```



2) Determine a calibration function of the form

 $T \approx aV^3 + bV^2 + cV + d$

to estimate temperature over the range of (0C, +30C). What is the maximum error in this calibration function?

```
B = [V.^3, V.^2, V, V.^0];
A = inv(B'*B)*B'*T
- 0.1489113
2.4763568
- 21.769242
75.579249
max(T - B*A)
ans = 0.0353359
min(T - B*A)
ans = - 0.0151326
```



Filters

3) Assume X and Y are related by the following transfer function:

$$Y = \left(\frac{30}{(s+3)(s+8)}\right)X$$

a) What is the differential equation relating x and y?

$$(s^{2} + 11s + 24)Y = 30X$$
$$\frac{d^{2}y}{dy^{2}} + 11\frac{dy}{dt} + 24y = 30x$$

b) Determine y(t) assuming

$$x(t) = 5 + 6\cos(4t)$$

Use superposition

$$x(t) = 5$$

$$s = 0$$

$$X = 5 + j0$$

$$Y = \left(\frac{30}{(s+3)(s+8)}\right)_{s=0} (5 + j0)$$

$$Y = 6.25$$

$$y(t) = 6.25$$

$$x(t) = 6 \cos(4t)$$

$$s = j4$$

$$X = 6 + j0$$

$$Y = \left(\frac{30}{(s+3)(s+8)}\right)_{s=j4} (6 + j0)$$

$$Y = 0.720 - j3.960$$

$$y(t) = 0.720 \cos(4t) + 3.960 \sin(4t)$$

The total answer is then

 $y(t) = 6.25 + 0.720\cos(4t) + 3.960\sin(4t)$

Filter Design using fminsearch()

4) Design a filter of the form

$$Y = \left(\frac{a}{\left(s^2 + bs + c\right)\left(s^2 + ds + e\right)}\right)X$$

to give a gain vs. frequency as close to Gd(s) as possible over the range of (0, 10) rad/sec.

$$G_d(j\omega) = \begin{cases} 1 & 0 < \omega < 6 \\ 0 & otherwise \end{cases}$$

Plot your filter's actual frequency response vs. it's ideal response (given by Gd).

meaning

$$G(s) = \left(\frac{181.1933}{\left(s^2 + 3.2716s + 7.0623\right)\left(s^2 + 1.2414s + 27.4180\right)}\right)$$



Code:

```
function [J] = costF(z)
  a = z(1);
  b = z(2);
  c = z(3);
  d = z(4);
  e = z(5);
  w = [0:0.1:10]';
  s = j*w;
  Gd = 1 .* (w < 6);
  num = a;
  den = (s.^2 + b*s + c).*(s.^2 + d*s + e);
  Gs = num ./ den;
  e = abs(Gd) - abs(Gs);
  J = sum(e.^{2});
  plot(w,abs(Gd),'b',w,abs(Gs),'r');
  pause(0.01);
  end
```

5) Design circuit to implement the filter you designed in problem #4

$$G(s) = \left(\frac{181.1933}{\left(s^2 + 3.2716s + 7.0623\right)\left(s^2 + 1.2414s + 27.4180\right)}\right)$$

Put in polar form

$$G(s) = \begin{pmatrix} \frac{181.1933}{(s+2.657 \neq \pm 52.01^0)(s+5.2362 \neq \pm 83.19^0)} \\ \text{Stage 1:} & \text{Stage 2} \\ \begin{pmatrix} \frac{1}{RC} \end{pmatrix} = 2.657 & \begin{pmatrix} \frac{1}{RC} \end{pmatrix} = 5.2362 \\ C = 1\mu F & C = 1\mu F \\ R = 376k\Omega & R = 191k\Omega \\ 3 - k = 2\cos(52.01^0) & 3 - k = 2\cos(83.19^0) \\ k = 1.769 & k = 2.763 \end{cases}$$



Note: The DC gain of this filter is 4.58.

- Reduce the gain (add a voltage divider) to make the DC gain match, or
- Label the output as 4.58Y

The latter is better: you're probably going to add gain somewhere. This filter provides a DC gain of 4.58. The rest of the circuit adds the rest.

6) Check your filter using CircuitLab



