## ECE 341 - Homework \#6

LaPlace Transforms, Continuous Probability Density Functions. Summer 2023

## LaPlace Transforms

1) Let $X$ and $Y$ be related by the following transfer function:

$$
Y=\left(\frac{10 s+20}{(s+3)(s+10)}\right) X
$$

a) What is the differential equation relating X and Y ?
b) Determine $y(t)$ assuming

$$
x(t)=2 \cos (4 t)+3 \sin (4 t)
$$

c) Determine $y(t)$ assuming $x(t)$ is the unit step function ( 0 for $t<1,1$ for $t>0$ )

$$
x(t)=u(t)
$$

2) Let $X$ and $Y$ be related by the following transfer funciton

$$
Y=\left(\frac{10 s+200}{(s+3+j 10)(s+3-j 10)}\right) X
$$

a) What is the differential equation relating X and Y ?
b) Determine $y(t)$ assuming

$$
x(t)=2 \cos (4 t)+3 \sin (4 t)
$$

c) Determine $y(t)$ assuming $x(t)$ is the unit step function ( 0 for $t<1,1$ for $t>0$ )

$$
x(t)=u(t)
$$

## Continuous Probability Density Functions

(over)

## Continuous Probability Density Functions


3) Determine the scalar so that the above function is a valid pdf (i.e. the total area is 1.000 )
4) Determine the corresponding cdf
5) Using Matlab, find 20 random values of $x$ for the above pdf
6) Find the moment generating function for $p(x)$

