

# ECE 461 Handout #27

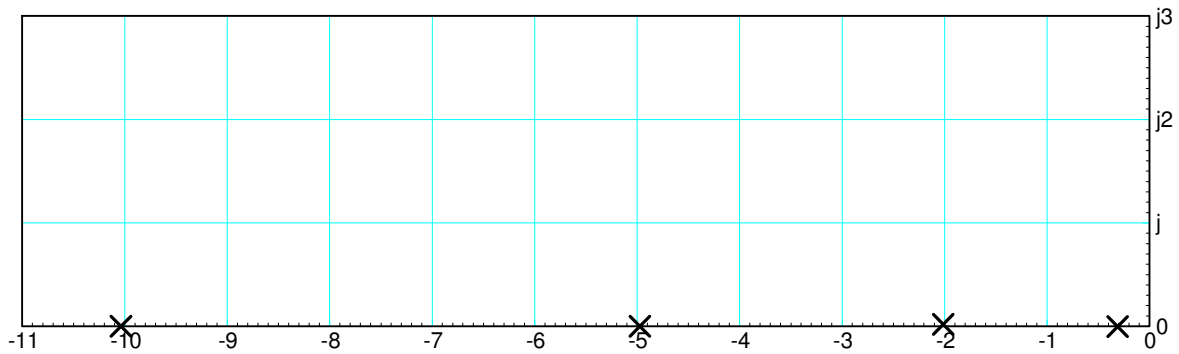
## Systems with Delays

Design a gain compensator,  $K(s)$ , so that the following system with a 100ms delay has

$$G(s) = \left( \frac{100}{(s+0.3)(s+2)(s+5)(s+10)} \right) e^{-0.2s}$$

to meet the following requirements:

- No error for a step input
- 2% settling time = 4 seconds
- Damping ratio = 0.707 (45 degrees)



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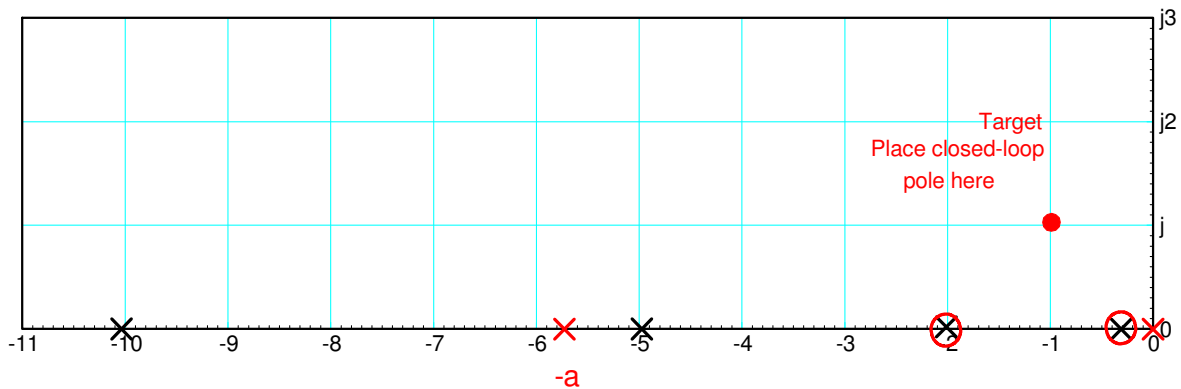
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Translating the specs:

- Make it a type-1 system
- Place the closed-loop dominant pole at  $s = -1 + j1$

Let

$$K(s) = k \left( \frac{(s+0.3)(s+2)}{s(s+a)} \right)$$



$$GK = \left( \frac{100k}{s(s+5)(s+10)(s+a)} \right) e^{-0.2s}$$

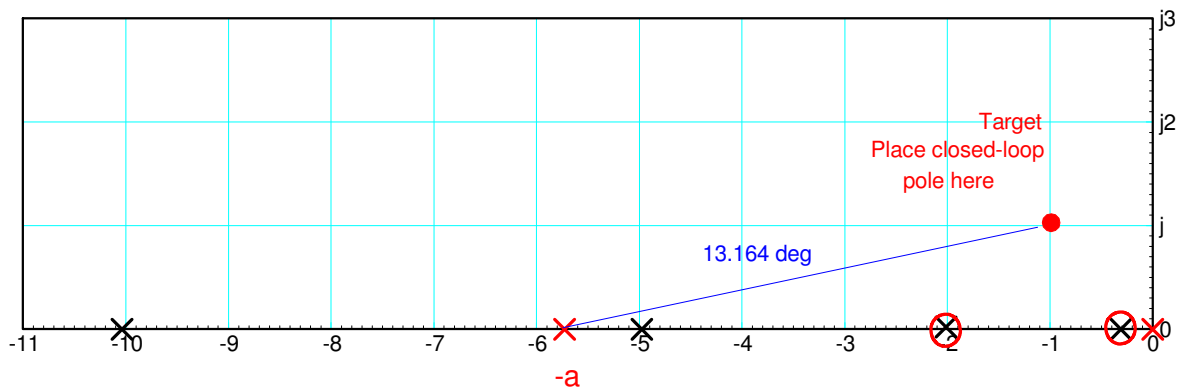
Evaluate what you know at  $s = -1 + j1$

$$\left( \left( \frac{100}{s(s+5)(s+10)} \right) e^{-0.2s} \right)_{s=-1+j1} = 2.313 \angle -166.836^\circ$$

To make the angle add up to -180 degrees

$$\angle(s+a) = 13.164^\circ$$

$$a = 1 + \frac{1}{\tan(13.164^\circ)} = 5.275$$



So now...

$$GK = \left( \left( \frac{100k}{s(s+5)(s+5.275)(s+10)} \right) e^{-0.2s} \right)_{s=-1+j1} = 0.527k \angle 180^\circ$$

$$k = \frac{1}{0.527} = 1.898$$

giving

$$K(s) = \left( \frac{1.898(s+0.3)(s+2)}{s(s+5.275)} \right)$$