

ECE 461/661 - Homework Set #8

Gain, Lead, PID Compensators - Due Monday, October 31st 20pt / problem

A 4th-order model for the 10-stage RC filter from homework #6 is

$$G(s) \approx \left(\frac{22}{(s+10.2)(s+5.539)(s+2.181)(s+0.4234)} \right)$$

1) Design a gain compensator, $K(s) = k$, which results in 20% overshoot for a step input. For this value of $K(s)$, give

- The resulting closed-loop dominant pole(s)
- The error constant, K_p
- The step response of the closed-loop system.

2) Design a lead compensator, $K(s) = k \left(\frac{s+a}{s+10a} \right)$, which results in 20% overshoot for a step input.

For this value of $K(s)$, give

- The resulting closed-loop dominant pole(s)
- The error constant, K_p
- The step response of the closed-loop system, and
- A circuit to implement $K(s)$

3) Design a I compensator, $K(s) = \left(\frac{k}{s} \right)$, which results in 20% overshoot for a step input. For this value of $K(s)$, give

- The resulting closed-loop dominant pole(s)
- The error constant, K_p
- The step response of the closed-loop system, and
- A circuit to implement $K(s)$

4) Design a PI compensator, $K(s) = k \left(\frac{s+a}{s} \right)$, which results in 20% overshoot for a step input.

For this value of $K(s)$, give

- The resulting closed-loop dominant pole(s)
- The error constant, K_p
- The step response of the closed-loop system, and
- A circuit to implement $K(s)$

5) Design a PID compensator, $K(s) = k \left(\frac{(s+a)(s+b)}{s} \right)$, which results in 20% overshoot for a step input. For this value of $K(s)$, give

- The resulting closed-loop dominant pole(s)
- The error constant, K_p
- The step response of the closed-loop system, and
- A circuit to implement $K(s)$