

Homework #2: ECE 461 / 661

State Transitional Logic - Counters - Timers:. Due Wednesday, September 7th

A stoplight is to be designed with four states:

| Present State | | Duration | Next State | Red | Yellow | Green | Blue <i>(left turn arrow)</i> |
|---------------|-----------|----------|------------|-----|--------|-------|----------------------------------|
| 00 | Stop | 5 sec | Left Turn | on | off | off | off |
| 01 | Left Turn | 4 sec | Go | off | off | off | on |
| 11 | Go | 5 sec | Caution | off | off | on | on |
| 10 | Caution | 2 sec | Stop | off | on | off | off |

1a) Use state transitional logic to design a ring counter which changes from state-to-state according to the above table. Change whenever a button is pressed.

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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| <table border="1" style="border-collapse: collapse;"> <tr> <td style="padding: 2px;">SA</td> <td colspan="4" style="padding: 2px;">AB</td> </tr> <tr> <td style="padding: 2px;"></td> <td style="padding: 2px;">00</td> <td style="padding: 2px;">01</td> <td style="padding: 2px;">11</td> <td style="padding: 2px;">10</td> </tr> <tr> <td style="padding: 2px;">0</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">x</td> <td style="padding: 2px;">x</td> </tr> <tr> <td style="padding: 2px;">CLK</td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> </tr> <tr> <td style="padding: 2px;">1</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">1</td> <td style="padding: 2px;">x</td> <td style="padding: 2px;">0</td> </tr> </table> | SA | AB | | | | | 00 | 01 | 11 | 10 | 0 | 0 | 0 | x | x | CLK | | | | | 1 | 0 | 1 | x | 0 | <table border="1" style="border-collapse: collapse;"> <tr> <td style="padding: 2px;">RA</td> <td colspan="4" style="padding: 2px;">AB</td> </tr> <tr> <td style="padding: 2px;"></td> <td style="padding: 2px;">00</td> <td style="padding: 2px;">01</td> <td style="padding: 2px;">11</td> <td style="padding: 2px;">10</td> </tr> <tr> <td style="padding: 2px;">0</td> <td style="padding: 2px;">x</td> <td style="padding: 2px;">x</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">0</td> </tr> <tr> <td style="padding: 2px;">CLK</td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> </tr> <tr> <td style="padding: 2px;">1</td> <td style="padding: 2px;">x</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">1</td> </tr> </table> | RA | AB | | | | | 00 | 01 | 11 | 10 | 0 | x | x | 0 | 0 | CLK | | | | | 1 | x | 0 | 0 | 1 | <table border="1" style="border-collapse: collapse;"> <tr> <td style="padding: 2px;">SB</td> <td colspan="4" style="padding: 2px;">AB</td> </tr> <tr> <td style="padding: 2px;"></td> <td style="padding: 2px;">00</td> <td style="padding: 2px;">01</td> <td style="padding: 2px;">11</td> <td style="padding: 2px;">10</td> </tr> <tr> <td style="padding: 2px;">0</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">x</td> <td style="padding: 2px;">x</td> <td style="padding: 2px;">0</td> </tr> <tr> <td style="padding: 2px;">CLK</td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> </tr> <tr> <td style="padding: 2px;">1</td> <td style="padding: 2px;">1</td> <td style="padding: 2px;">x</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">0</td> </tr> </table> | SB | AB | | | | | 00 | 01 | 11 | 10 | 0 | 0 | x | x | 0 | CLK | | | | | 1 | 1 | x | 0 | 0 | <table border="1" style="border-collapse: collapse;"> <tr> <td style="padding: 2px;">RB</td> <td colspan="4" style="padding: 2px;">AB</td> </tr> <tr> <td style="padding: 2px;"></td> <td style="padding: 2px;">00</td> <td style="padding: 2px;">01</td> <td style="padding: 2px;">11</td> <td style="padding: 2px;">10</td> </tr> <tr> <td style="padding: 2px;">0</td> <td style="padding: 2px;">x</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">x</td> </tr> <tr> <td style="padding: 2px;">CLK</td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> </tr> <tr> <td style="padding: 2px;">1</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">1</td> <td style="padding: 2px;">x</td> </tr> </table> | RB | AB | | | | | 00 | 01 | 11 | 10 | 0 | x | 0 | 0 | x | CLK | | | | | 1 | 0 | 0 | 1 | x |
| SA | AB | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 00 | 01 | 11 | 10 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | 0 | x | x | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| CLK | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 0 | 1 | x | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| RA | AB | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 00 | 01 | 11 | 10 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | x | x | 0 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| CLK | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | x | 0 | 0 | 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| SB | AB | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 00 | 01 | 11 | 10 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | x | x | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| CLK | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 1 | x | 0 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| RB | AB | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | 00 | 01 | 11 | 10 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | x | 0 | 0 | x | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| CLK | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 0 | 0 | 1 | x | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

$$S_A = CLK \cdot B$$

$$S_B = CLK \cdot \bar{A}$$

$$R_A = CLK \cdot \bar{B}$$

$$R_B = CLK \cdot A$$

1b) Use combinational logic so that the LEDs are on and off in the correct order based upon the present state.

$$Red = \bar{A} \cdot \bar{B}$$

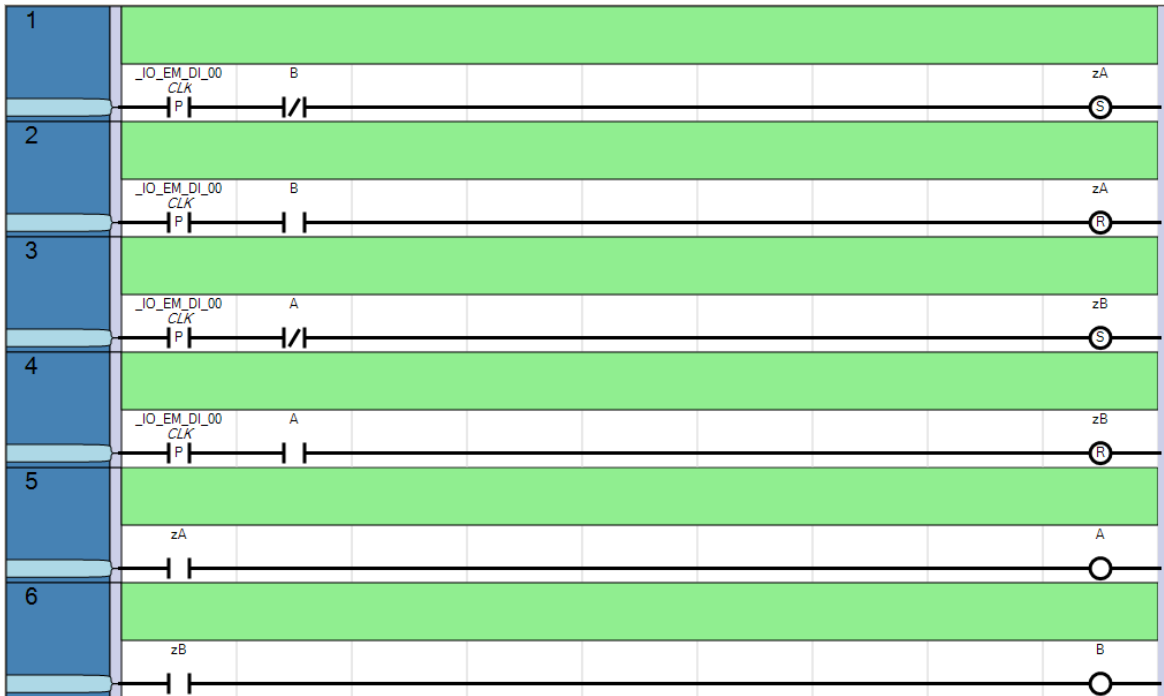
$$Yellow = A \cdot \bar{B}$$

$$Green = A \cdot B$$

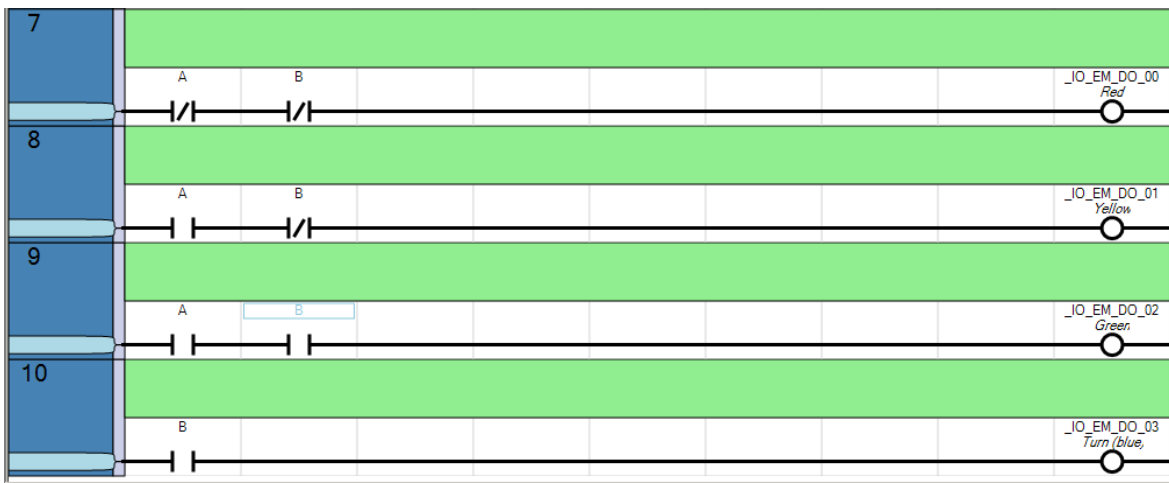
$$Blue = \bar{A} \cdot B + A \cdot B = B$$

Resulting Ladder Logic Program: With state-transition logic, this is a 10-line program. (note: you need additional logic to create the clock pulse if you want to automate the clock operator)

State Transition Logic:

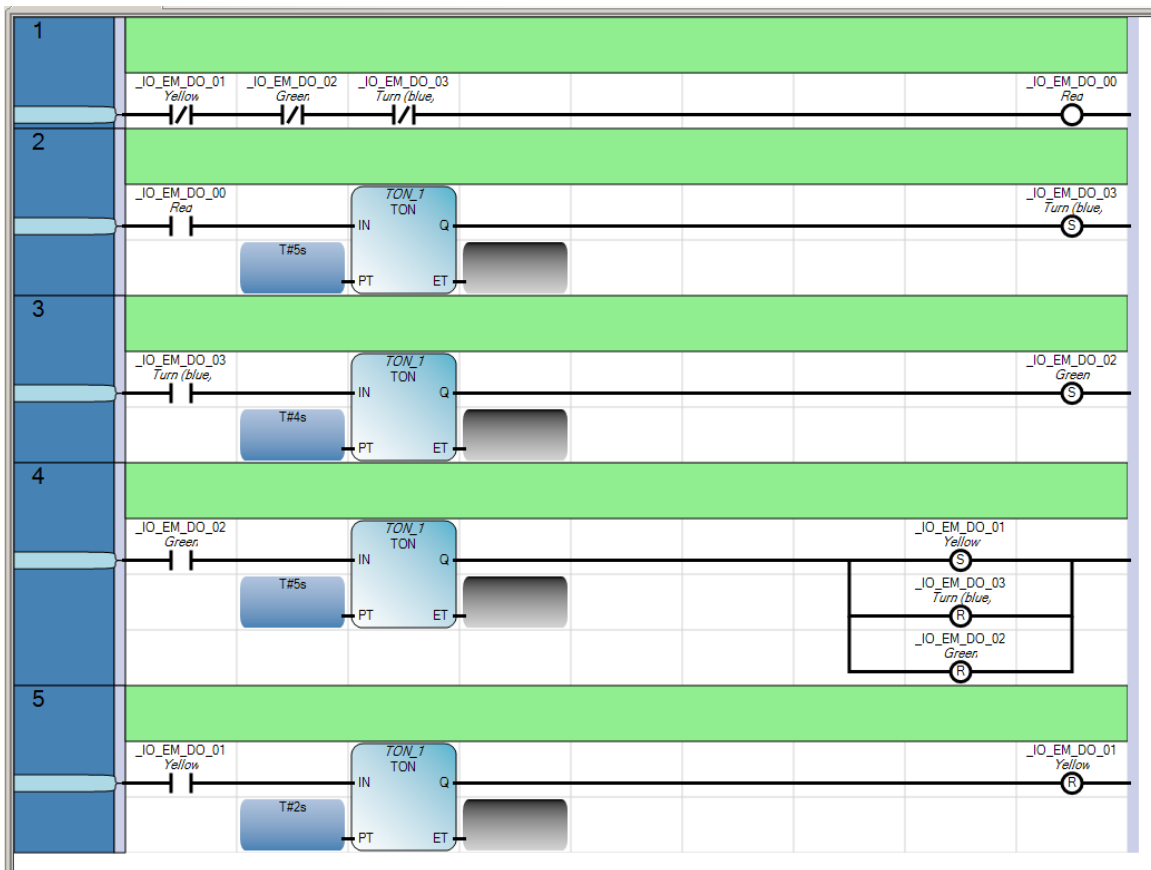


Outputs (lights)



2) Repeat problem #1 using timer blocks.

With timer blocks, this is a 5-line program. More if you want the left turn arrow to blink on green (more on this later)



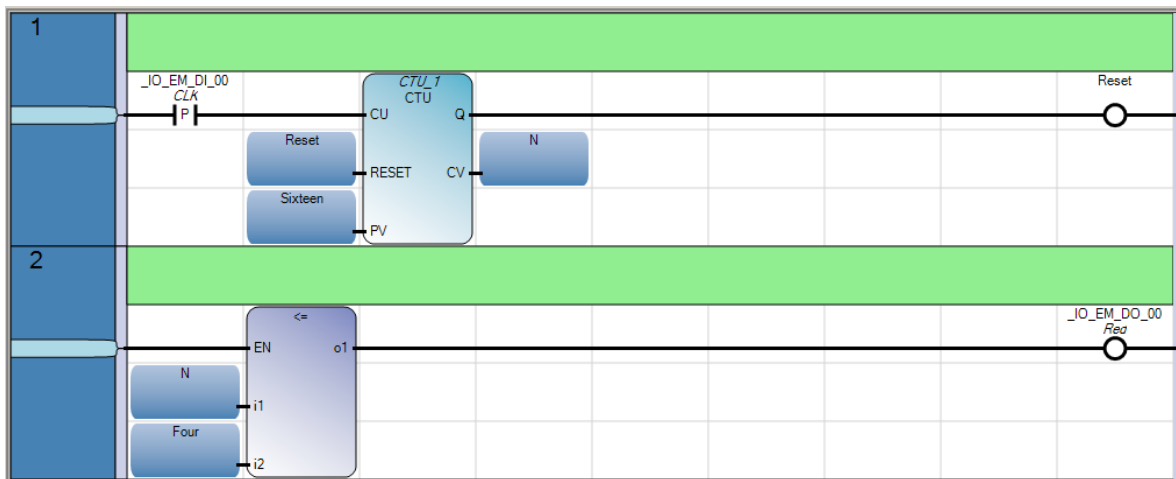
3) Repeat problem #1 using counter blocks with a count to 16 (seconds - one cycle):

| Time | Red | Yellow | Green | Blue |
|---------------------------------------|-----|--------|-------|------|
| Red Light (5 sec) | 0 | on | off | off |
| | 1 | on | off | off |
| | 2 | on | off | off |
| | 3 | on | off | off |
| | 4 | on | off | off |
| Left Turn (4 sec) | 5 | off | off | on |
| | 6 | off | off | on |
| | 7 | off | off | on |
| | 8 | off | off | on |
| Green Blink Left Turn (5 sec) | 9 | off | on | off |
| | 10 | off | on | on |
| | 11 | off | on | off |
| | 12 | off | on | on |
| | 13 | off | on | off |
| Yellow (2 sec) | 14 | off | on | off |
| | 15 | off | on | off |

Solution: With counters, this is a 5-line program. 6 if you want a clock pulse to happen every second.

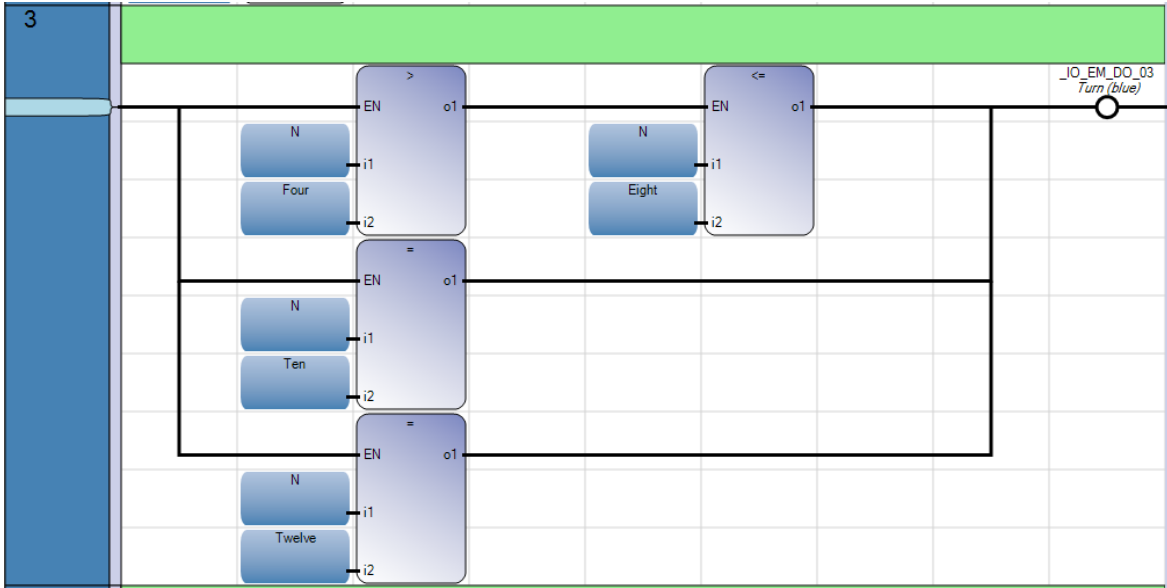
Rung 1: Count to 16 and repeat

Rung 2: The red light is on when the count is less than or equal to 4



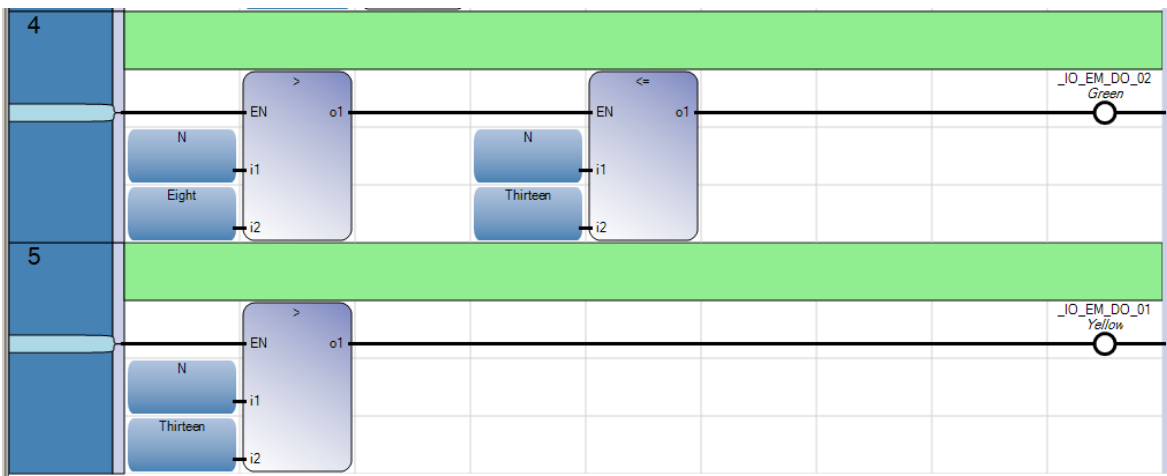
Rung 3: The turn arrow (blue) is on when the count is

- Between 5 and 8,
- or equal to 10
- or equal to 12



Rung 4: Green light is on if the count is between 9 and 13

Rung 5: Yellow light is on if the count is 14 or 15 (more than 13)



Rung 6: (optional) If you want to automate the clock so that it pulses once per second (rather than manually hitting it)

Manual clock is nice for debugging

Automate clock is nice for operation

