

# Homework #10: ECE 461

z-Transform. Converting  $G(s)$  to  $G(z)$ . Due Monday, November 13th

1) X and Y are related as follows:

$$Y = \left( \frac{400}{(s+10)(s+20)} \right) X$$

a) What is the differential equation relating X and Y?

b) Determine  $y(t)$  assuming

$$x(t) = 2 + 3 \sin(4t)$$

2) X and Y are related as follows:

$$Y = \left( \frac{0.1z}{(z-0.9)(z-0.8)} \right) X$$

a) What is the difference equation relating X and Y?

b) Determine  $y(t)$  assuming

$$x(t) = 2 + 3 \sin(4t)$$

3) Assume

$$G(s) = \left( \frac{4}{(s+1)(s+3)} \right)$$

a) Determine a filter,  $G(z)$ , which has approximately the same step response as  $G(s)$ . Assume  $T = 0.1$  sec

b) Plot the step response of  $G(s)$  and  $G(z)$

4) Assume

$$G(s) = \left( \frac{4}{(s+1+j4)(s+1-j4)} \right)$$

a) Determine a filter,  $G(z)$ , which has approximately the same step response as  $G(s)$ . Assume  $T = 0.1$  sec

b) Plot the step response of  $G(s)$  and  $G(z)$

5) Assume

$$G(s) = 5 \left( \frac{s+0.5}{s+2} \right)$$

a) Determine a filter,  $G(z)$ , which has approximately the same step response as  $G(s)$ . Assume  $T = 0.1$  sec

b) Plot the step response of  $G(s)$  and  $G(z)$