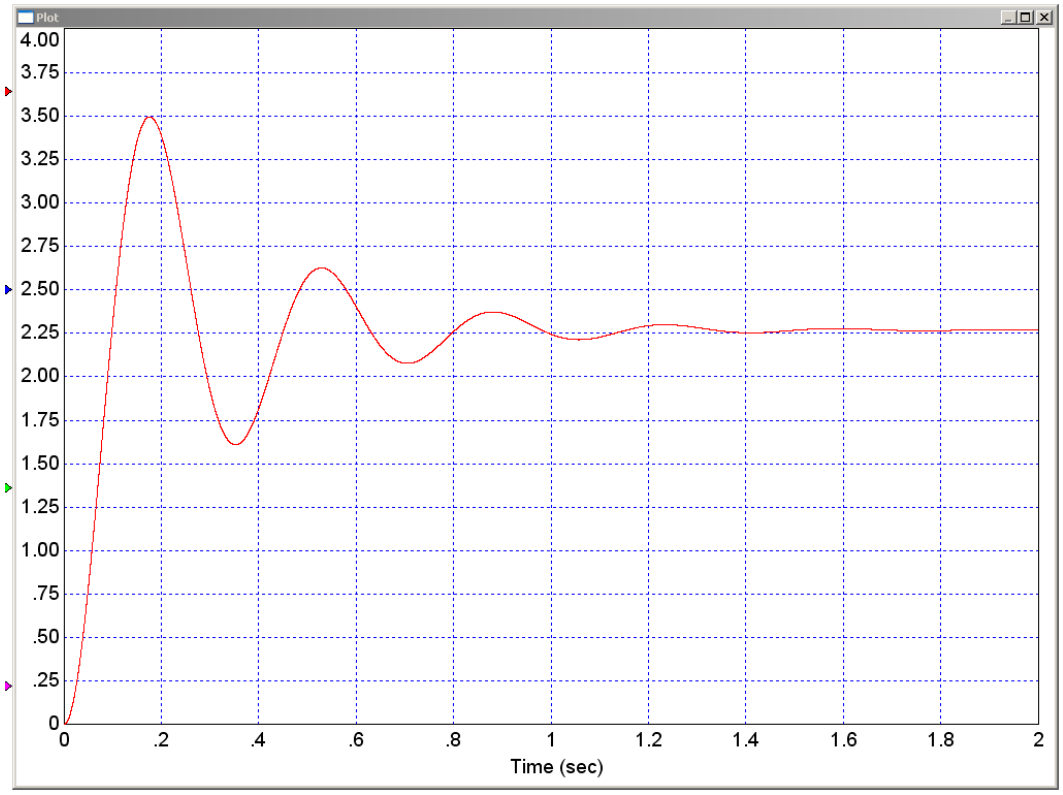
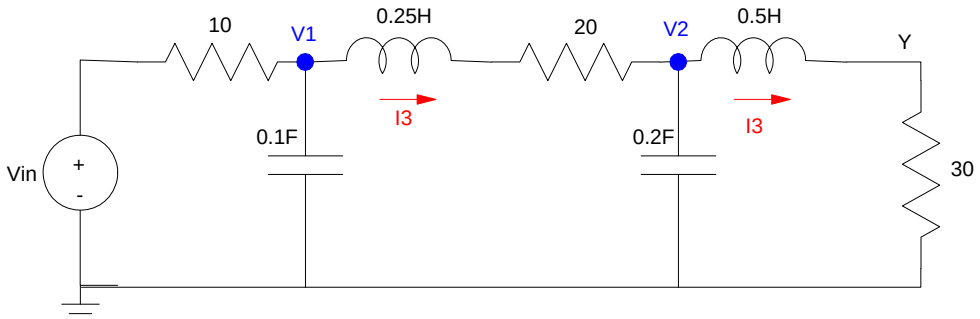
ECE 461/661 - Test #2: Name _____

October 19, 2018

1) Give the transfer function for a system with the following response to a unit step input:



2) For the following mass-spring system:



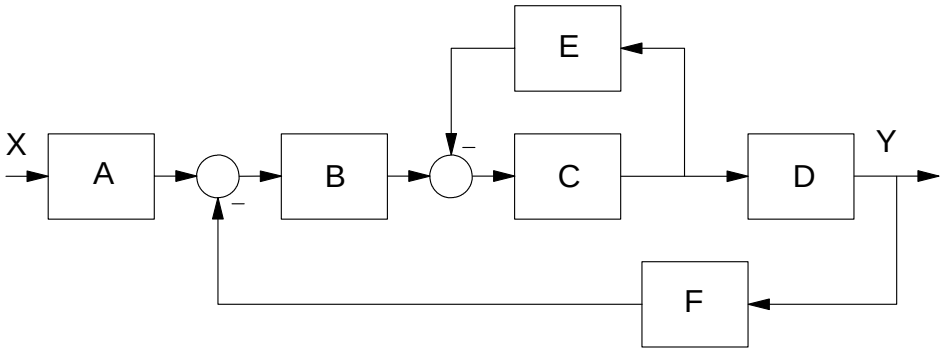
a) Write the dynamics of this system as four compled differential equations in terms of {Vin, V1, V2, I3, I4}

b) Express these dynamics in state-space form

$$\begin{bmatrix} sV1 \\ sV2 \\ sI3 \\ sI4 \end{bmatrix} = \begin{bmatrix} & & & \\ & & & \\ & & & \\ & & & \end{bmatrix} \begin{bmatrix} V1 \\ V2 \\ I3 \\ I4 \end{bmatrix} + \begin{bmatrix} \\ \\ \\ \end{bmatrix} Vin$$

$$Y = \begin{bmatrix} & & & \end{bmatrix} \begin{bmatrix} V1 \\ V2 \\ I3 \\ I4 \end{bmatrix} + \begin{bmatrix} \end{bmatrix} Vin$$

3) For the following block diagram, find the transfer funciton from X to Y

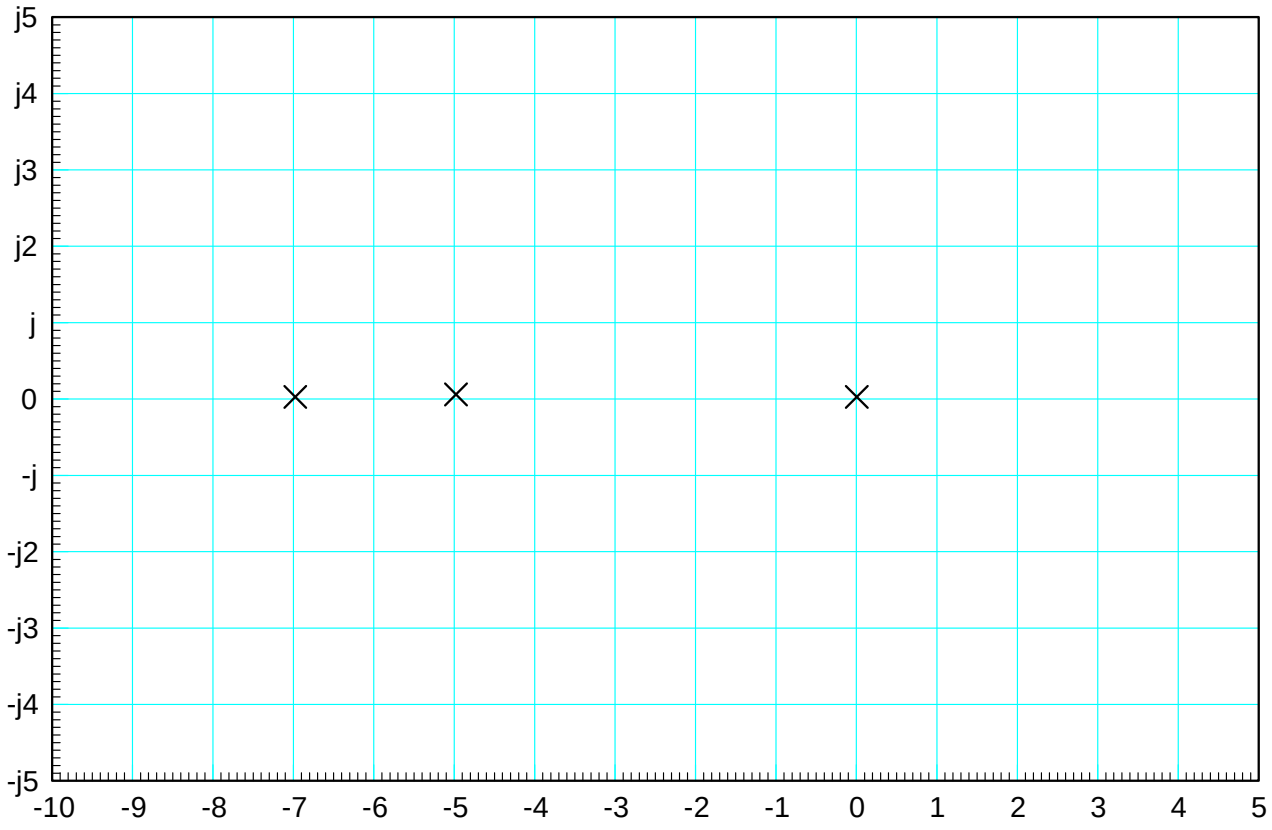


4) Sketch the root locus for

$$G(s) = \left(\frac{10}{s(s+4)(s+7)} \right)$$

Determine the following as well:

Real Axis Loci	
Breakaway Points (approx)	
jw Crossing (approx)	
Asymptotes	show on graph

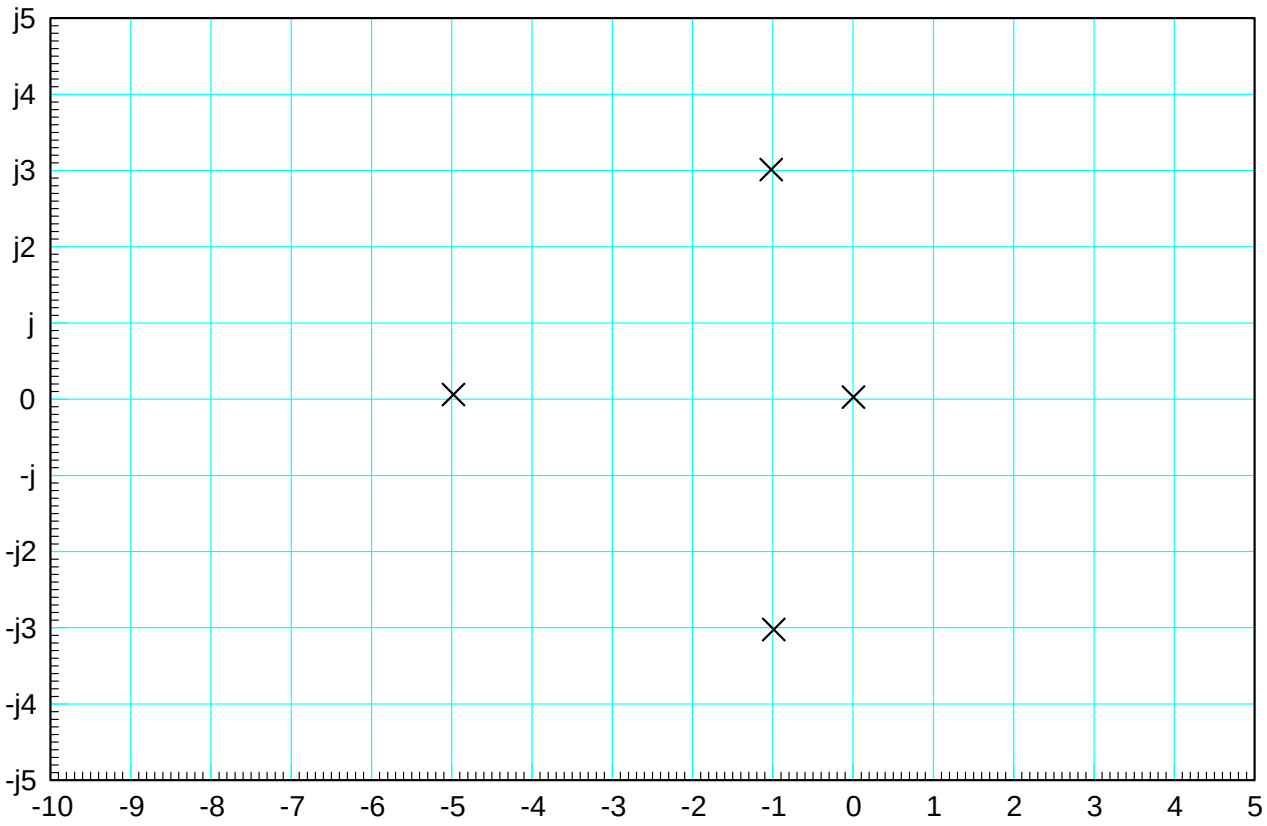


5) Sketch the root locus for

$$s(s+5)(s+1+j3)(s+1-j3)+5k=0$$

Determine the following as well:

Real Axis Loci	
Breakaway Points (approx)	
jw Crossing (approx)	
Departure Angle from pole at s = -2 + j3	
Asymptotes	show on graph

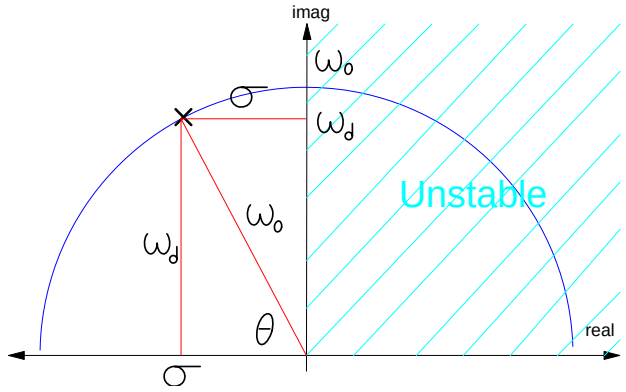


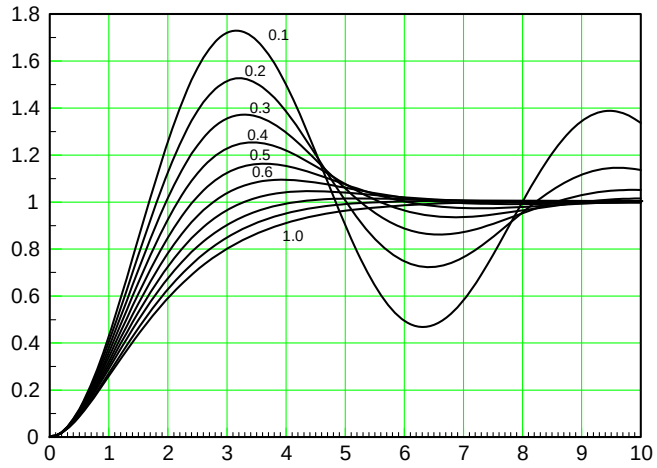
Bonus! Early voting in North Dakota Starts October 29th. What do you need to bring to the polls to vote?

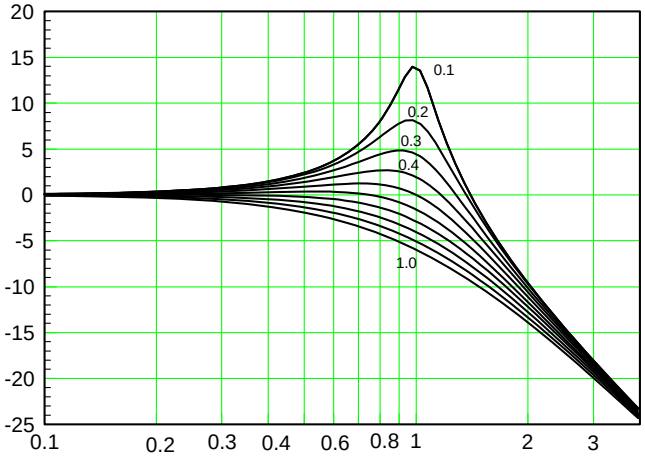
2nd-Order Approximations

$$G(s) = \left(\frac{k\cdot\omega_o^2}{s^2+2\zeta\omega_o s+\omega_o^2}\right) = \left(\frac{k\cdot\left(\sigma^2+\omega_d^2\right)}{(s+\sigma+j\omega_d)(s+\sigma-j\omega_d)}\right)$$

$$s = -\sigma \pm j\omega_d = \omega_o \angle \pm \theta$$







$\zeta = \cos\theta$ damping ratio

$\%OS = \exp\left(-\left(\frac{\pi\zeta}{\sqrt{1-\zeta^2}}\right)\right)$ % Overshoot

$\omega_m = \omega_o\sqrt{1-2\zeta^2}$ Max gain frequency

$T_p = \frac{\pi}{\omega_0\sqrt{1-\zeta^2}}$ time to peak

$T_s = T_{2\%} = \frac{4}{\sigma}$ 2% Settling Time

$M_m = \frac{1}{2\zeta\sqrt{1-\zeta^2}}$ Max gain

$\frac{1}{2\zeta}$ Gain at corner freq

ζ	Tp	%OS	ω_m	Mm	Mm (dB)
0.1	3.15	72.81	0.99	5.03	14.02
0.2	3.21	51.97	0.96	2.55	8.14
0.3	3.29	35.5	0.91	1.75	4.85
0.4	3.43	22.4	0.82	1.36	2.7
0.5	3.63	12.31	0.71	1.15	1.25
0.6	3.93	5.26	0.53	1.04	0.35
0.7	4.4	1.34	0.14	1	0
0.8	5.24	0.09	0	1	0
0.9	7.21	0	0	1	0
1.0	-	0	0	1	0