

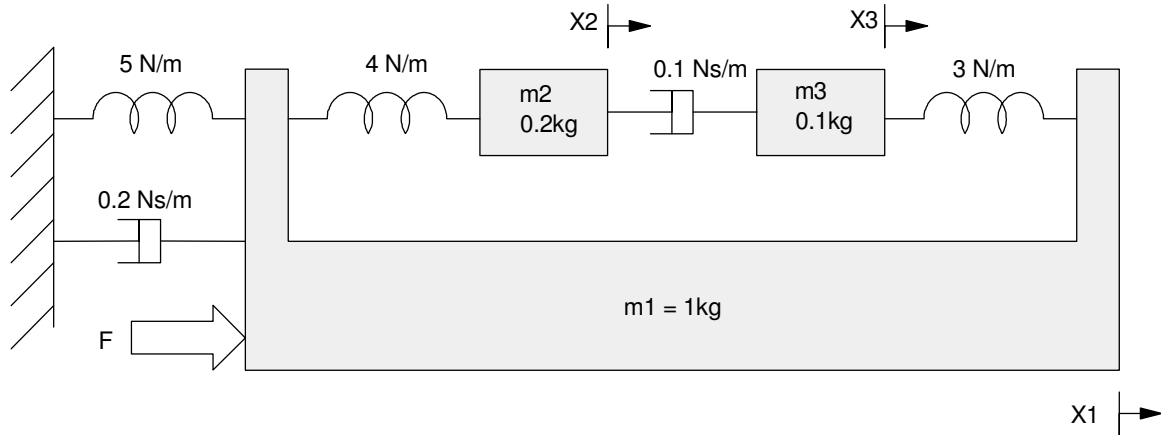
Homework #6: ECE 461/661

Mass-Spring Systems, Rotational Systems, DC Motors. Due Monday, September 26th

Mass Spring systems

1) (20pt) Draw the circuit equivalent for the following mass-spring systems.

- Express the dynamics in state-space form
- Find the transfer function from F to X_2
- Plot the step response from F to X_2

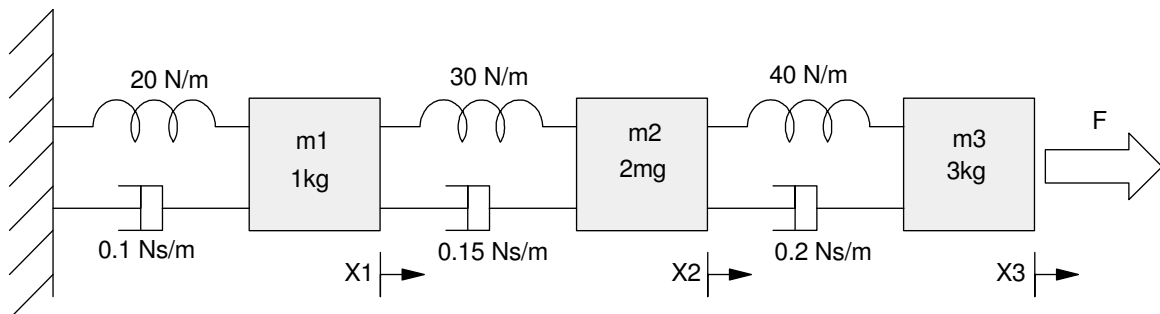


Problem 1

2) (20pt) Draw the circuit equivalent for the following mass-spring systems.

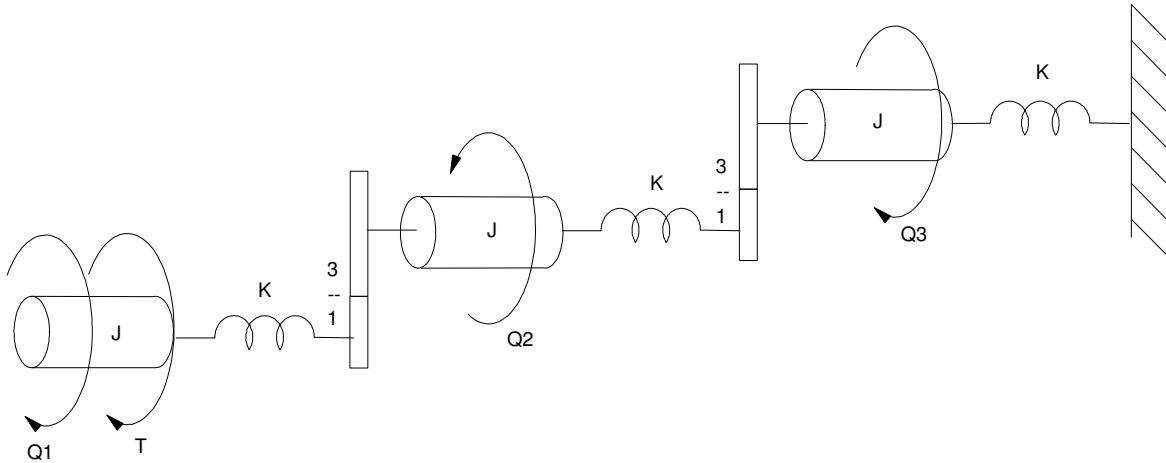
- Express the dynamics in state-space form
- Find the transfer function from F to X_3

Plot the step response from F to X_3



Rotational Systems

- 3) Draw the circuit equivalent for the following rotational system.
- Express the dynamics in state-space form
 - Find the transfer function from T to $Q1$
 - Plot the step response from T to $Q1$



Problem 3: $J = 0.5 \text{ Kg m} / \text{s}^2$. $K = 10 \text{ Nm/rad}$

Motors

- 4) Find the transfer function for the following DC servo motor

<http://www.baldor.com/catalog/CDP3335>

Allen Bradley CDP3335: 1/2 HP DC Servo Motor

- \$1243 ea
 - Armature Resistance = $R_a = 0.664 \text{ Ohms}$
 - Armature Inductance = $L_a = 5.119 \text{ mH}$
 - Armature Inertia = $J = 6.318 \text{ lb-ft}^2$
 - 4.6A @ 2426 rpm @ 1 ft-lb load
 - Weight 26.0 lb
- 5) Assume this motor is used to power an electric bicycle at 20mph
- Motor speed @ 20mph = 2426 rpm
 - Gear (wheel) used to convert 2426 rpm to 20mph
 - Bicycle weight = 100kg

What is the gear reduction (wheel diameter) to convert 2426rpm to 20mph?

What is the inertia relative to the DC servo motor (bring the 100kg mass back to the motor through a gear)

What is the transfer function (dynamics) for the bicycle / servo motor combination?