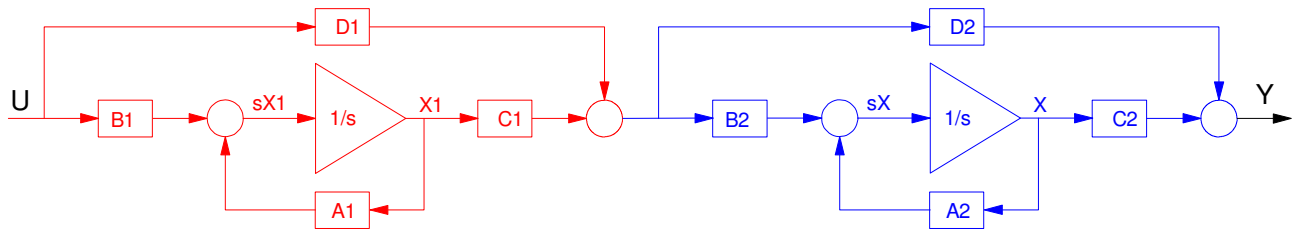


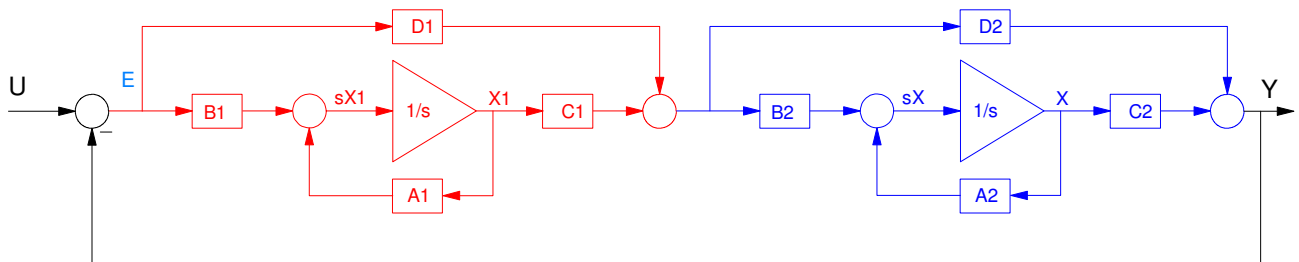
ECE 463/663 - Homework #4

Block Diagrams and LaGrangian Dynamics. Due Monday, February 10th

1) Determine the state-space model for two systems cascaded together:



2) Determine the state-space model for two systems in a feedback configuration:

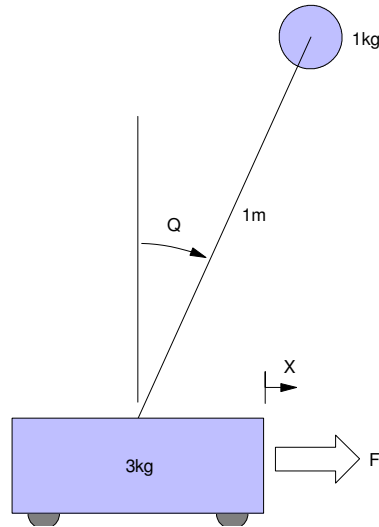


(over)

3) (30pt) Derive the dynamics for an inverted pendulum where

- $m_1 = 2\text{kg}$ (mass of ball)
- $m_2 = 3\text{kg}$ (mass of cart)
- $L = 1.0\text{m}$ (length of arm)

Find the linearized dynamics at $x = 0, \theta = 0$



4) (30pt) Derive the dynamics for a ball and beam system where

- $J = 0.5 \text{ kg m}^2$ (the inertia of the beam)
- $m = 2\text{kg}$ (the mass of the ball)

Find the linearized dynamics at $x = 1.0\text{m}, \theta = 0$

