

# ECE 463/663 - Homework #4

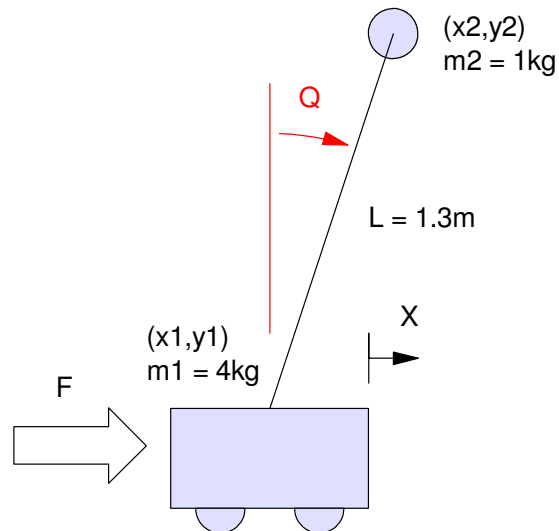
LaGrangian Dynamics. Due Monday, February 5th  
Please submit as a hard copy or submit on BlackBoard

## Cart & Pendulum

1) (30pt) Derive the dynamics for an inverted pendulum where

- $m_1 = 4\text{kg}$  (mass of cart)
- $m_2 = 1\text{kg}$  (mass of ball)
- $L = 1.3\text{m}$  (length of arm)

Find the linearized dynamics at  $x = 0, \theta = 0$



## Ball and Beam

2) (30pt) Derive the dynamics for a ball and beam system where

- $J = 2\text{ kg m}^2$  (the inertia of the beam)
- $m = 3\text{kg}$  (the mass of the ball)

Find the linearized dynamics at  $r = 1.0\text{m}, \theta = 0$

