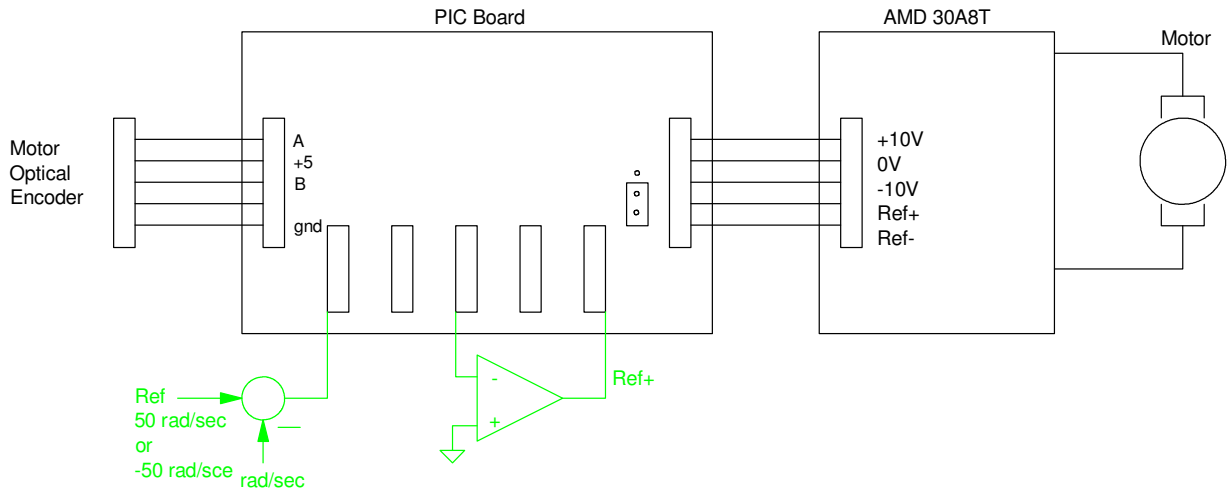


# ECE 761: Homework #17: Speed Control of a DC Servo Motor

Load the program SPEED.C onto your PIC board. This program

- Measures the speed of the DC servo motor,
- Make the reference input (Ref) equal to +50 rad/sec or -50 rad/sec when you press the step button, and
- Outputs a voltage equal to  $0.1 * (\text{Ref} - \text{Speed})$
- With a sampling rate of 50ms.

The serial port should be set up for 9600 baud, no hand shaking.



From homework #20, the transfer function of the DC motor should be approximately

$$\omega \approx \left( \frac{40}{s+6} \right) V_a$$

With a tachometer with a gain of 0.1, the open-loop system is

$$G(s) = \left( \frac{4}{s+6} \right)$$

# 1) Proportional Control: Dominant Pole = -20

Open-Loop System (tachometer includes a gain of 0.1)

$$GK = \left( \frac{4k}{s+6} \right)$$

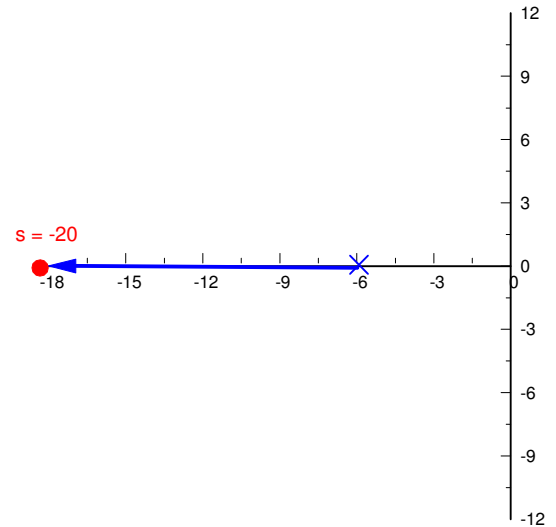
Feedback gain, k

$$\left( \frac{4k}{s+6} \right)_{s=-20} = -1$$

$$K(s) = k = 3.5$$

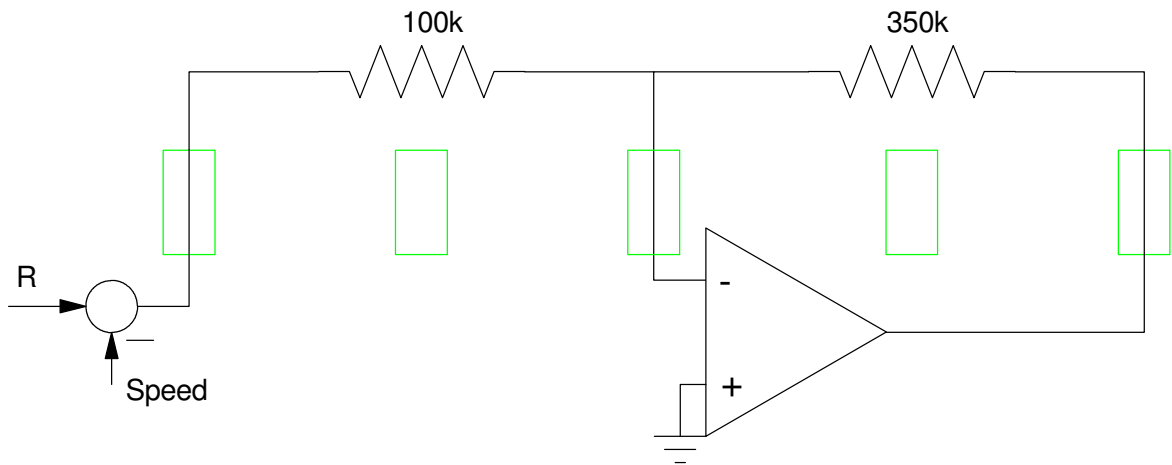
Closed-Loop System

$$\left( \frac{GK}{1+GK} \right) = \left( \frac{14}{s+20} \right)$$



- Build an op-amp circuit to implement a gain of 3.5
- Record the step respons.
- From the step response, determine the closed-loop dominant pole

DC Gain	2% Settling Time <i>(measured)</i>	Overshoot <i>(%)</i>	Dominant Pole <i>(measured)</i>



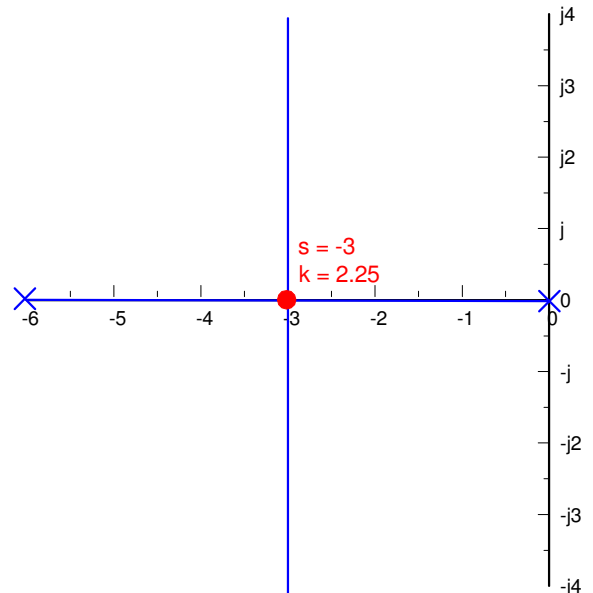
## Integral Control: Dominant Pole = -3

Open-Loop Gain:

$$\left( \frac{4k}{s(s+6)} \right)_{s=-3} = -1$$

$$k = 2.25 = \frac{1}{RC}$$

$$K(s) = \left( \frac{2.25}{s} \right)$$

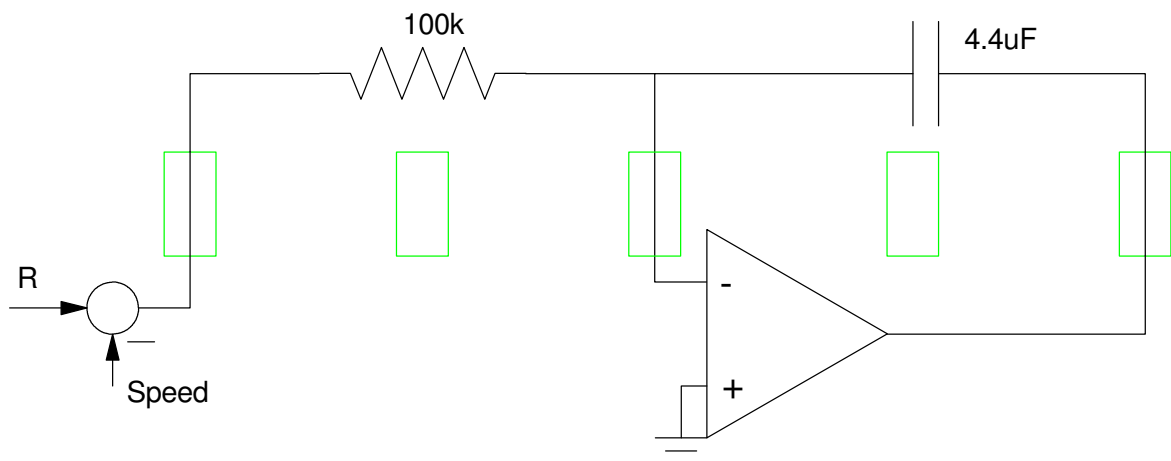


Closed-Loop System

$$\left( \frac{GK}{1+GK} \right) = \left( \frac{9}{s(s+6)+9} \right)$$

- Build an op-amp circuit to implement a gain of  $K(s)$
- Record the step respons.
- From the step response, determine the closed-loop dominant pole

DC Gain (5 rad/sec step)	2% Settling Time ( <i>measured</i> )	Overshoot (%)	Dominant Pole ( <i>measured</i> )



## Integral Control: Dominant Pole = $-3 + j3$

Open-Loop Gain:

$$\left( \frac{4k}{s(s+6)} \right)_{s=-3+j3} = -1$$

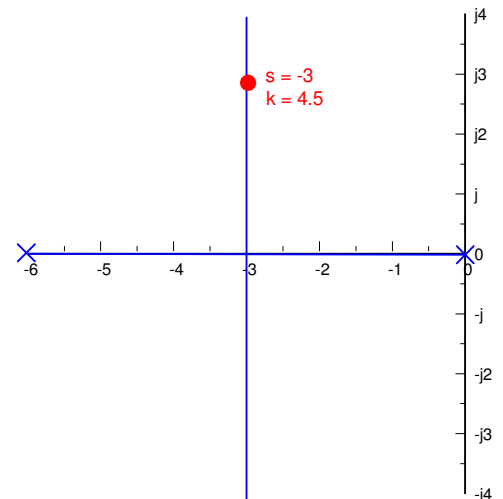
$$k = 4.5 = \frac{1}{RC}$$

$$K(s) = \left( \frac{4.5}{s} \right)$$

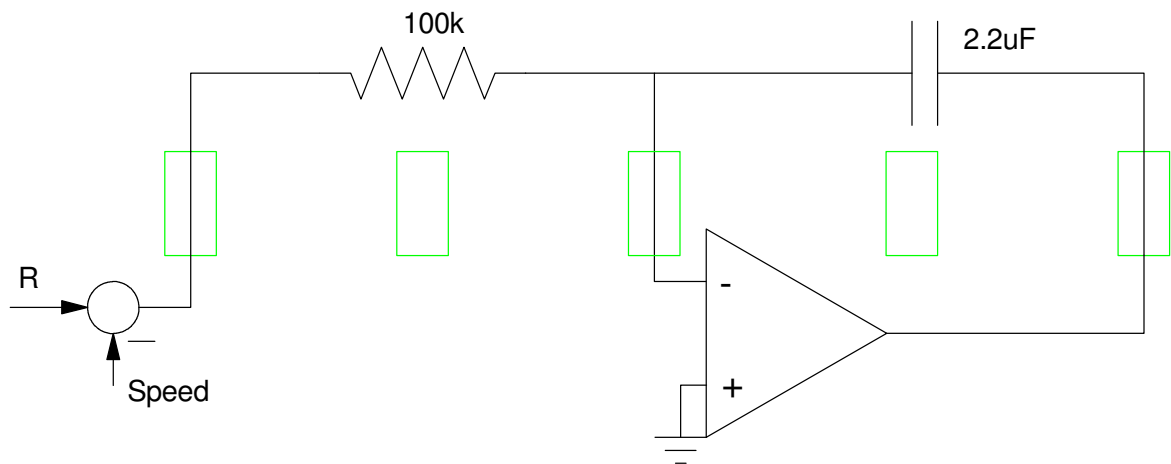
Closed-Loop System

$$\left( \frac{GK}{1+GK} \right) = \left( \frac{18}{s(s+6)+18} \right)$$

- Build an op-amp circuit to implement  $K(s)$
- Record the step respons.
- From the step response, determine the closed-loop dominant pole



DC Gain (5 rad/sec step)	2% Settling Time <i>(measured)</i>	Overshoot <i>(%)</i>	Dominant Pole <i>(measured)</i>



## PI Control: Dominant Pole = -10

Add a PI compensator of the form

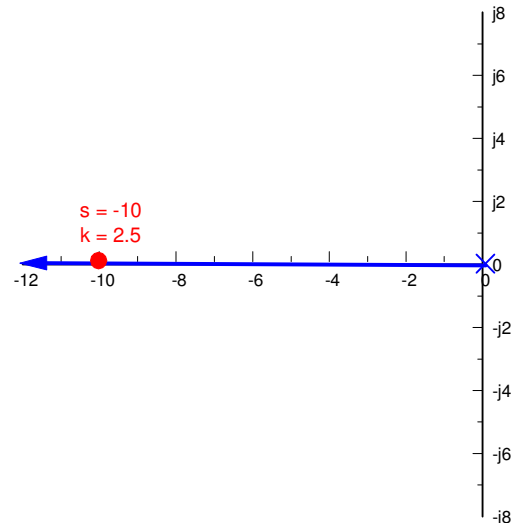
$$K(s) = k \left( \frac{s+6}{s} \right)$$

$$GK = \left( \frac{4k}{s} \right)$$

Pick 'k' to place the closed-loop dominant pole at -10

$$\left( \frac{4k}{s} \right)_{s=-10} = -1$$

$$k = 2.5$$



Closed-Loop System

$$\left( \frac{GK}{1+GK} \right) = \left( \frac{10}{s+10} \right)$$

- Build an op-amp circuit to implement  $K(s)$
- Record the step respons.
- From the step response, determine the closed-loop dominant pole

DC Gain (5 rad/sec step)	2% Settling Time <i>(measured)</i>	Overshoot <i>(%)</i>	Dominant Pole <i>(measured)</i>

