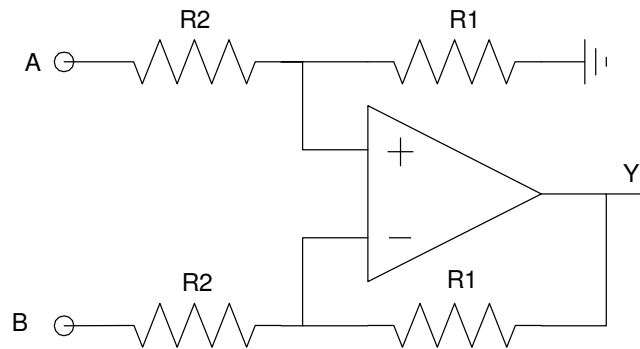


Instrumentation Amplifiers

Instrumentation Amplifiers

The transfer function for an instrumentation amplifier is



$$Y = \left(\frac{R_1}{R_2} \right) (A - B)$$

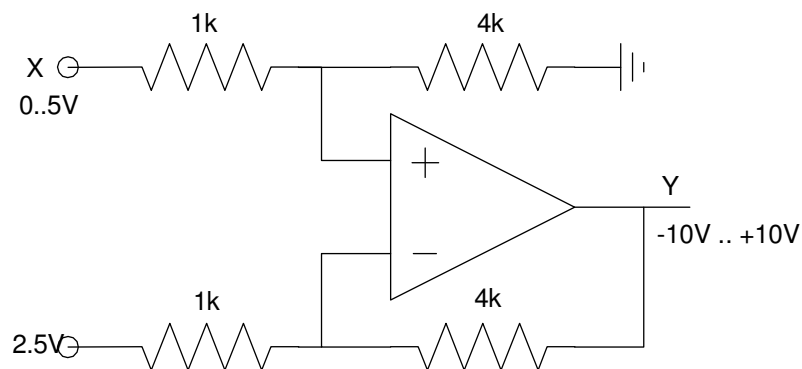
Case 1: Voltage Amplification

Design a circuit to convert a 0..5V signal in to a +/- 10V signal.

- $X = 0..5V$ analog
- $Y = -10 .. +10V$ analog
- $Y = 4X - 10$

Solution: Rewrite this as

$$Y = 4(X - 2.5)$$



Level Shifter: 0..5V signal is amplified to -10V .. +10V

Case 2: $V = f(R)$

Assume R varies from 2000 Ohms to 2200 Ohms. Design a circuit which outputs

- -10V when $R = 2000$ Ohms
- +10V when $R = 2200$ Ohms

Solution: Convert R to a voltage using a voltage divider. Assume a 2100 Ohm resistor

$R = 2000$ Ohms:

$$V_x = \left(\frac{2000}{2000+2100} \right) 10V = 4.878V$$

$$Y = -10V$$

$R = 2200$ Ohms

$$V_x = \left(\frac{2200}{2200+2100} \right) 10V = 5.116V$$

$$Y = +10V$$

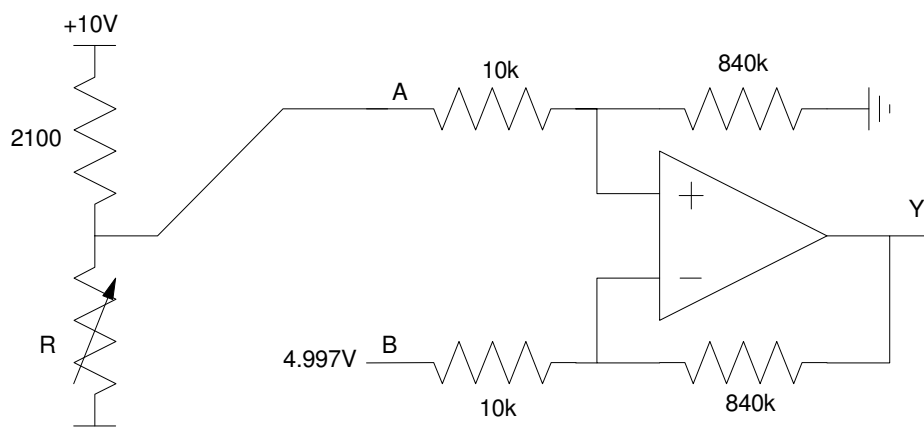
The gain you need is

$$gain = \left(\frac{\text{change in output}}{\text{change in input}} \right) = \left(\frac{10V - (-10V)}{5.116V - 4.878V} \right)$$

$$gain = 83.95$$

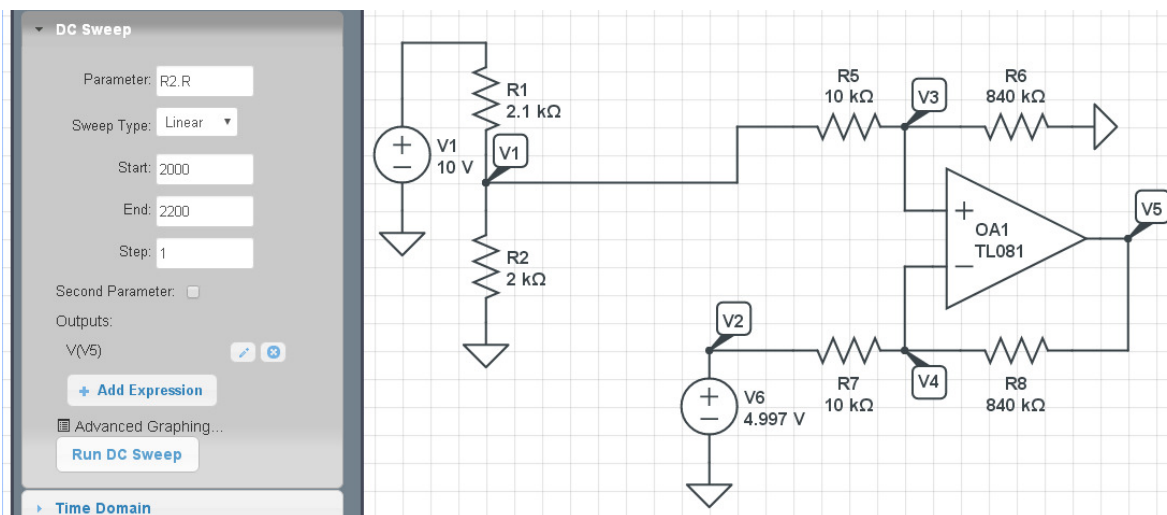
The output should be 0V (midband) when the input is midband

$$V_b = \left(\frac{4.878V + 5.116V}{2} \right) = 4.997V$$

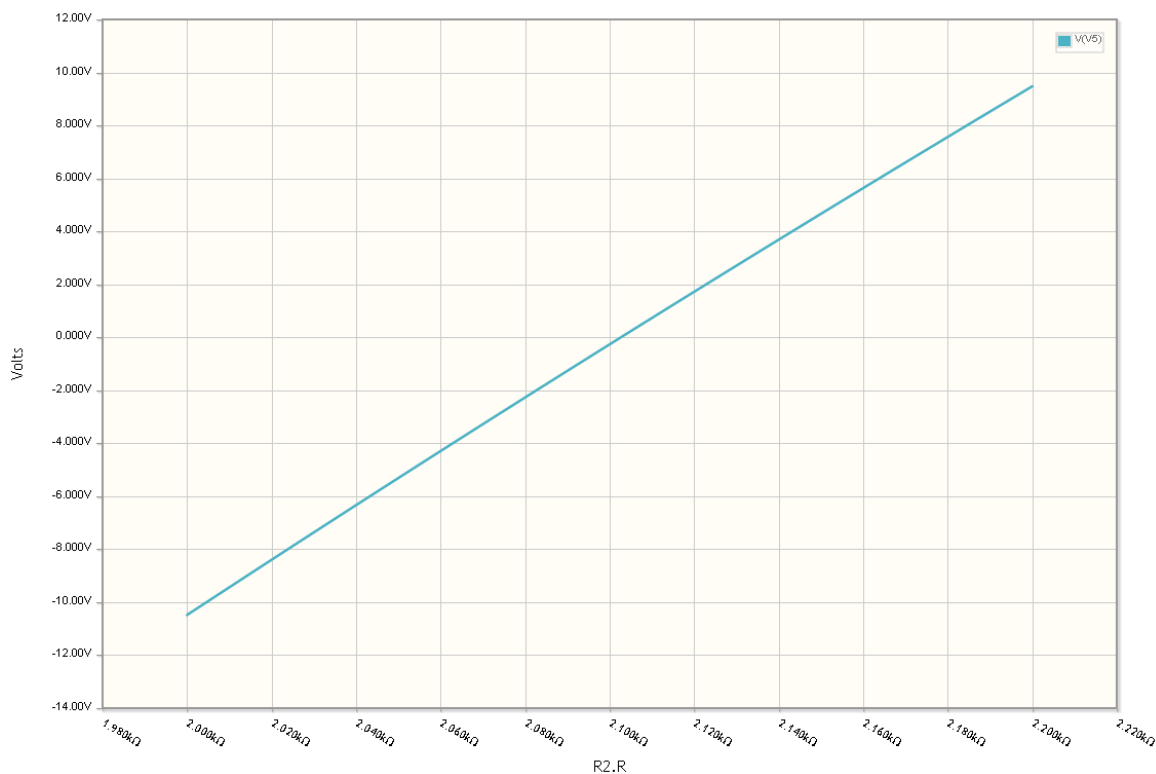


Instrumentation Amplifier: Y goes from -10V to +10V as R goes from 2000 to 2200 Ohms

In CircuitLab you can check by doing a DC Sweep on R2



This results in the output voltage shown below. Note that the range isn't *quite* 0V to 10V. This is due to the loading of R5 and R6 on V1 (the larger R5 and R6 are, the less the loading).



Output voltage as R sweeps from 2000 to 2200 Ohms

Case 3: RTD Temperature Sensor.

The temperature-resistance relationship of an RTD is

$$R = 1000 \cdot (1 + 0.0043T) \, \Omega$$

where T is the temperature in degrees celsius. Design a circuit which outputs

- 0V at 0C
- +10V at +100C

Solution: Assume a voltage divider with a 1000 Ohm resistor.

At 0C

- $R = 1000 \, \text{Ohms}$
- $V_a = 5.00 \, \text{V}$
- $V_y = 0.00 \, \text{V}$

At +100C

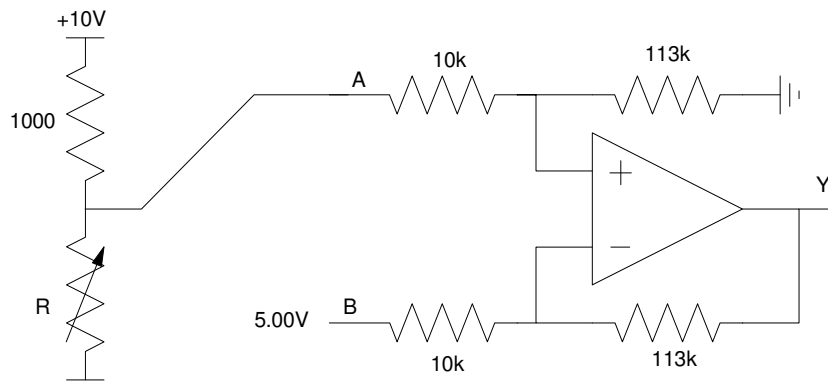
- $R = 1430 \, \text{Ohms}$
- $V_a = 5.885 \, \text{V}$
- $V_y = +10.00 \, \text{V}$

As the input voltage increases, the output voltage increases. Connect the voltage divider to A.

The output is 0V when $V_a = 5.00 \, \text{V}$. Make $B = 5.00 \, \text{V}$

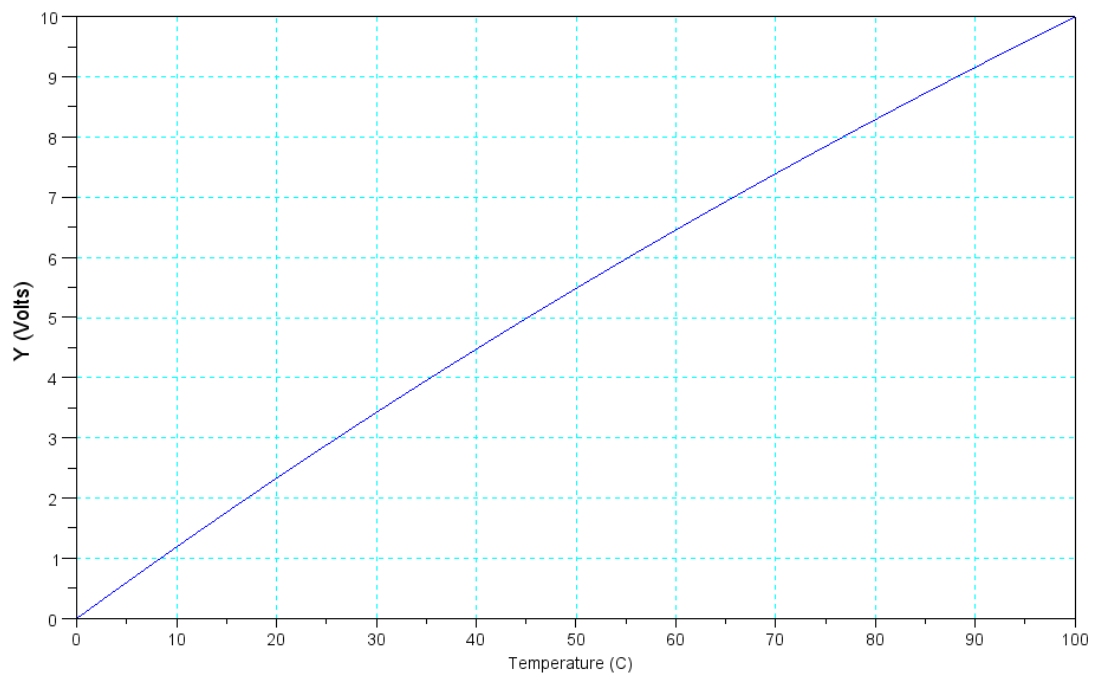
The gain needed is

$$\text{gain} = \left(\frac{\text{change in output}}{\text{change in input}} \right) = \left(\frac{10\text{V} - 0\text{V}}{5.885\text{V} - 5.00\text{V}} \right) = 11.30$$



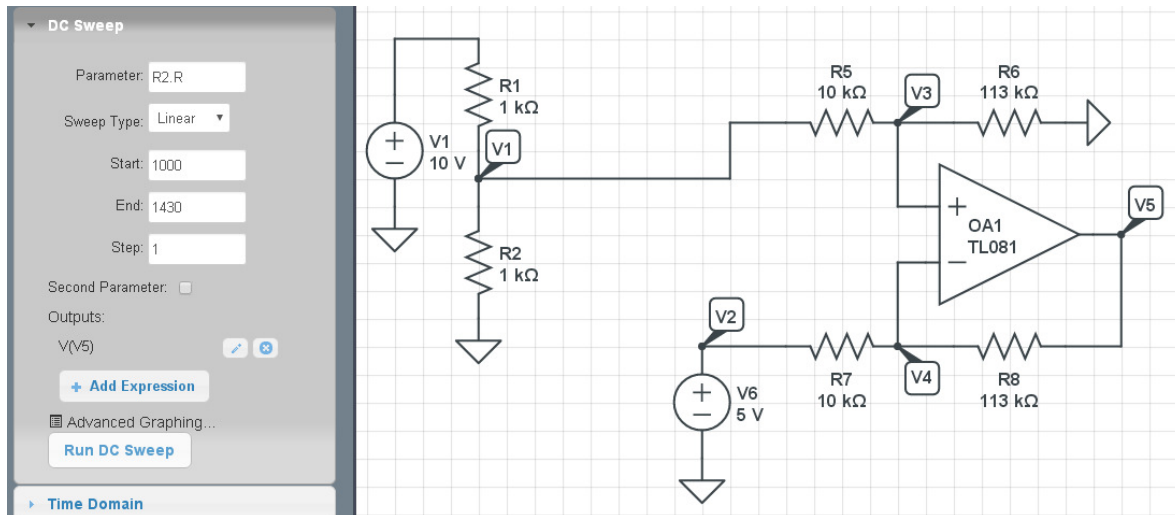
Checking the results in Matlab:

```
T = [0:0.1:100]';  
R = 1000 * (1 + 0.0043*T);  
Va = R ./ (1000 + R) * 10;  
Y = 11.3 * (Va - 5.00);  
  
plot(T,Y);  
  
xlabel('Temperature (C)');  
ylabel('Y (Volts)');
```

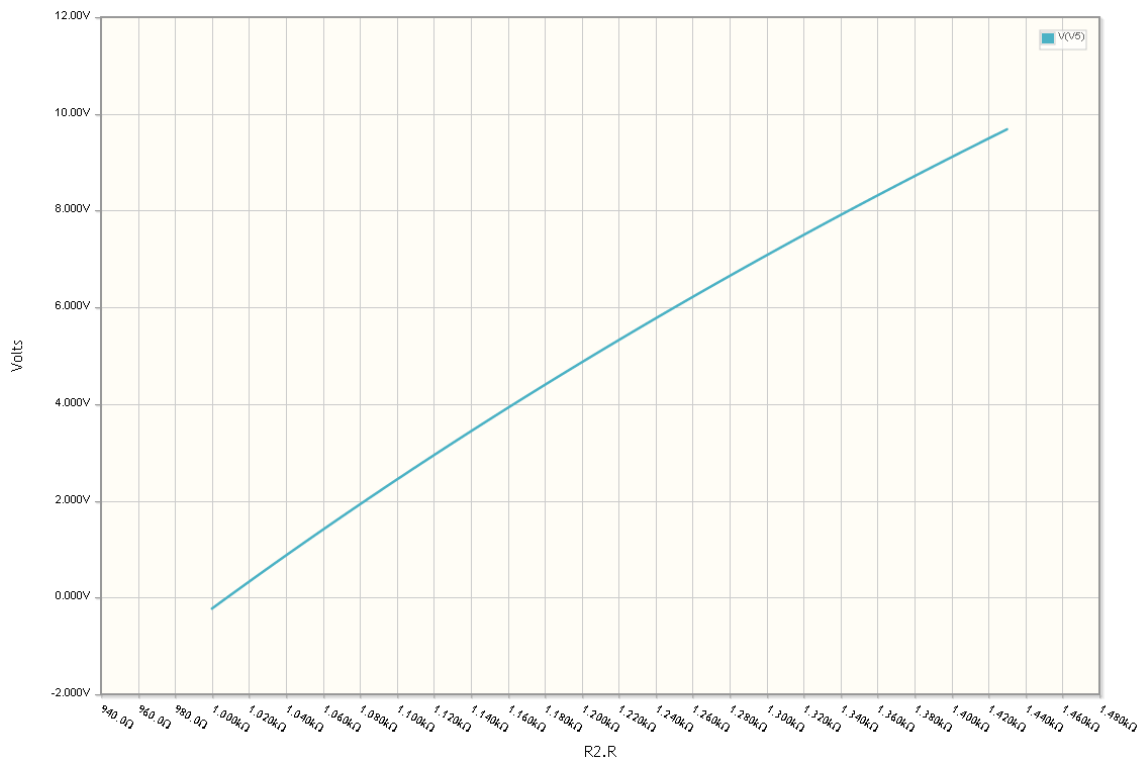


Checking the results in CircuitLab, note that

- The output voltage is slightly off
- This is due to the loading of R5 and R6 on V1



A DC Sweep was run with R2 varying from 1000 to 1430 Ohms ($0^\circ < T < 100^\circ\text{C}$)



Resulting Output Voltage as R varies from 1000 to 1430 Ohms

Case 4: Thermistor Temperature Sensor.

The temperature-resistance relationship of a thermistor is

$$R \approx 1000 \exp\left(\frac{3905}{T+273} - \frac{3905}{298}\right) \Omega$$

where T is the temperature in degrees celsius. Design a circuit which outputs

- 0V at 0C
- +10V at +40C

Solution: Assume a voltage divider with a 1000 Ohm resistor.

At 0C

- $R = 3320.125 \text{ Ohms}$
- $V_b = 7.6853 \text{ V}$
- $V_y = 0.00\text{V}$

At +40C

- $R = 533.664 \text{ Ohms}$
- $V_b = 3.4797\text{V}$
- $V_y = +10.00\text{V}$

As the input voltage decreases, the output voltage increases. Connect the voltage divider to B.

The output is 0V when $V_a = 7.6853\text{V}$. Make $A = 7.6853\text{V}$

The gain needed is

$$\text{gain} = \left(\frac{10\text{V}-0\text{V}}{3.4797\text{V}-7.6853\text{V}} \right) = -2.3778$$

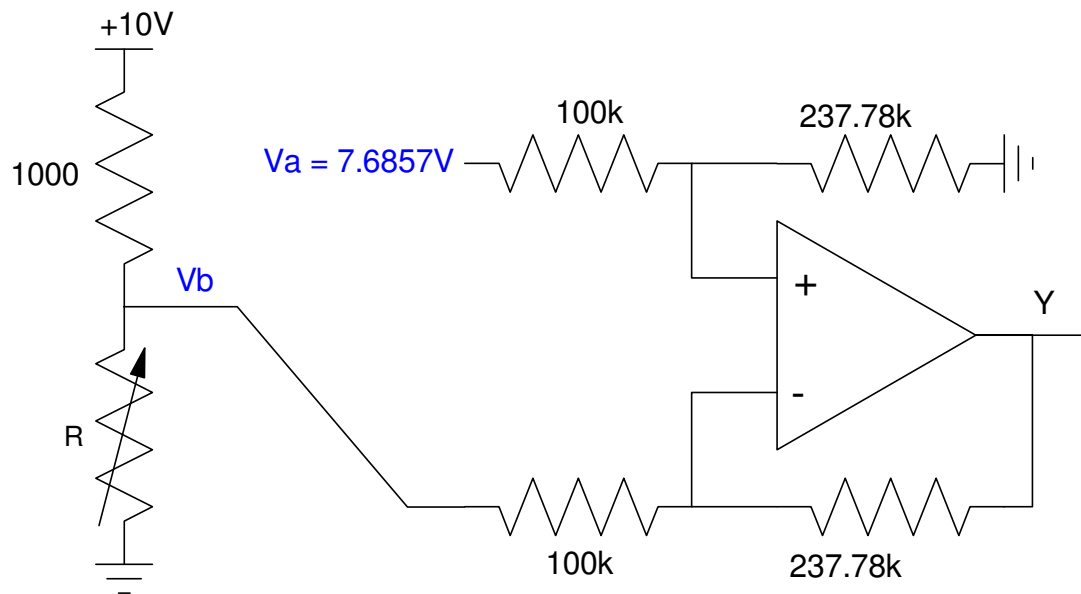
The minus sign is taken care of by connecting to the minus input (B).

The gain comes from the resistor ratio

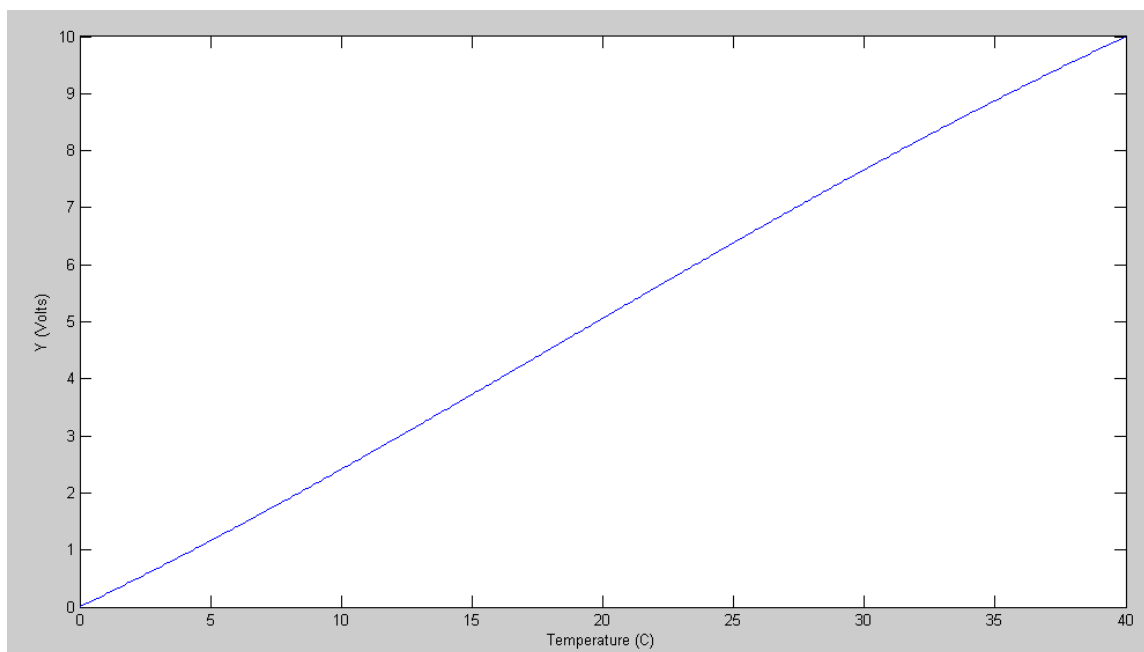
$$\text{Let } R_1 = 100\text{k}, R_2 = 237.78\text{k}$$

Note: You can check your results in Matlab.

```
T = [0:0.1:40]';
R = 1000 * exp( 3905 ./ (T + 273) - 3905/298 );
Va = R ./ (1000 + R) * 10;
Y = 2.3778 * (7.6853 - Va);
plot(T,Y);
xlabel('Temperature (C)');
ylabel('Y (Volts)');
```



Instrumentation Amplifier to output 0V @ 0C, 10V @ 40C

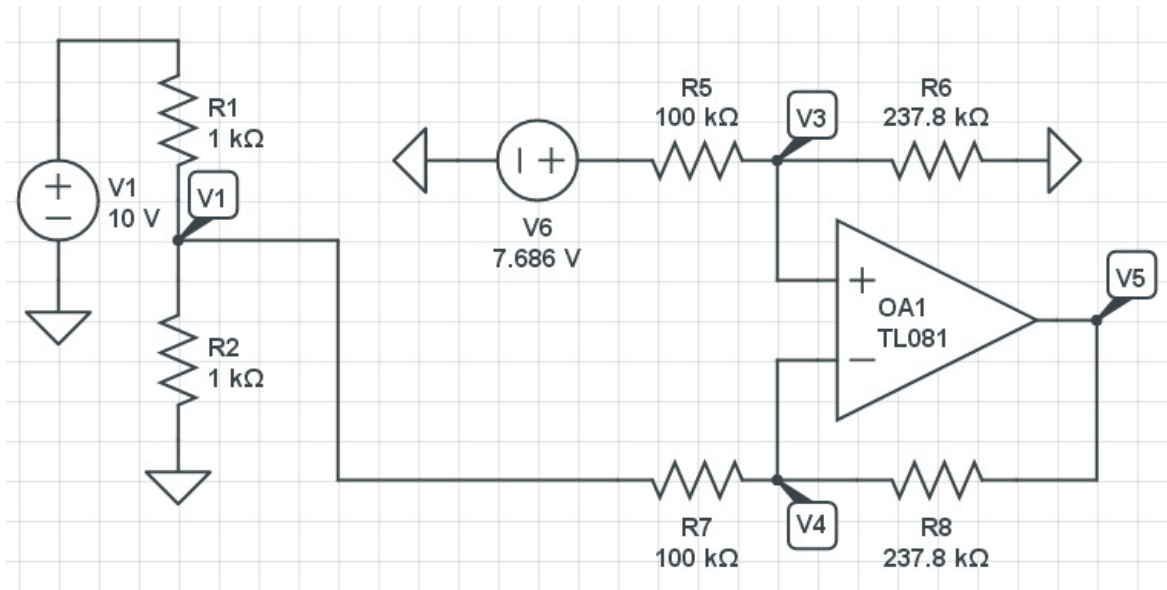


Output Voltages vs. Temperature

Note that the output goes from 0V to 10V as temperature goes from 0C to +40C as desired.

In CircuitLab, check

- The left endpoint (0C or $R_2 = 3320.125$ Ohms)
- The midpoint (20C or $R_2 = 1250.593$ Ohms)
- The right endpoint (40C or $R_2 = 533.664$ Ohms)



V(V1)	7.668 V		
V(V3)	5.410 V		
V(V4)	5.410 V		
V(V5)	42.32 mV		

Output (V5) at 0C = 0.04232V (0V ideally)

V(V1)	5.556 V		
V(V3)	5.410 V		
V(V4)	5.410 V		
V(V5)	5.064 V		

Output (V5) at +20C = 5.064V (5.000V ideally)

V(V1)	3.486 V		
V(V3)	5.410 V		
V(V4)	5.410 V		
V(V5)	9.985 V		

Output (V5) at +40C = 9.985V (10.000V ideally)