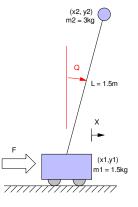
## ECE 463/663 - Homework #13

VSS & Saturating Control. Due Monday, May 5th

## **VSS Control**

1) For the cart and pendulum system of homework set #4:

$$s\begin{bmatrix} x\\ \theta\\ \dot{x}\\ \dot{\theta}\end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1\\ 0 & -19.6 & 0 & 0\\ 0 & 19.6 & 0 & 0\end{bmatrix}\begin{bmatrix} x\\ \theta\\ \dot{x}\\ \dot{\theta}\end{bmatrix} + \begin{bmatrix} 0\\ 0\\ 0.667\\ -0.444\end{bmatrix}F$$



Design a VSS control law so that the cart and pendulum system behaves like the following reference model:

$$\boldsymbol{y}_m = \left(\frac{4}{(s+2)\left(s^2+s+2\right)}\right)\boldsymbol{R}$$

2) Find the step response of your control law on the linear model

- Plot the output (x) vs time
- Plot the input (F) vs time

3) Find the step respone of your control law on the nonlinear simulation

## **Saturating Control:**

4) Design a saturating control law so that the cart and pendulum system behaves like the following reference model:

$$\boldsymbol{y}_m = \left(\frac{4}{(s+2)\left(s^2+s+2\right)}\right)\boldsymbol{R}$$

5) Find the step response of your control law on the linear model

- Plot the output (x) vs time
- Plot the input (F) vs time

6) Find the step respone of your control law on the nonlinear simulation